

The Oxidative Coupling of Methane: a Kinetic Model

by
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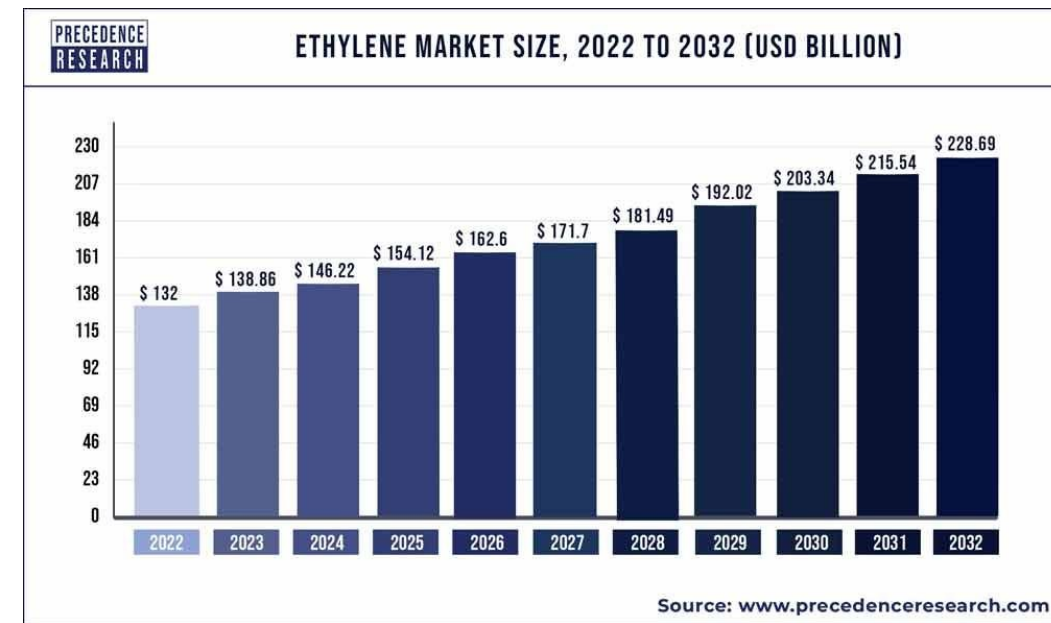
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Natural Gas and Ethylene Production

- Low-carbon solutions: conversion of natural gas to useful chemicals.
- Increasing natural gas production.
 - 2022: 28.6 trillion cubic feet (Tcf) shale gas produced in the U.S. (79% of total U.S. dry natural gas production).¹



1. U.S. Energy Information Administration. (accessed 2023-12-06)

Kinetic Model²

- 39 gas-phase reactions
- 14 surface reactions
- 33 species (gas-phase, surface, free radicals, inert gas)

2. SUN, J.; THYBAUT, J.; MARIN, G. Microkinetics of Methane Oxidative Coupling. *Catalysis Today* **2008**, 137 (1), 90-102. DOI:10.1016/j.cattod.2008.02.026.

Python Script

$$\bullet V \frac{dC_A}{dt} = \begin{bmatrix} S^{gas} \\ S^{surf} \end{bmatrix} \begin{bmatrix} r^{gas} \cdot V_{gas} \\ r^{surf} \cdot cat_SA \end{bmatrix}$$

$$\frac{d\theta}{dt} = S^{surf} r^{surf}$$

$$[*] = \sigma - \sum_i [\theta_i]$$

V = total volume [m³]

V_{gas} = gas volume [m³]

C_A = gas phase species concentration matrix [mol m⁻³]

S = reaction matrix (gas or surface)

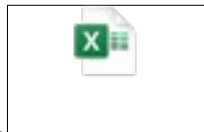
r = rate expression (gas or surface) [mol m⁻³ s⁻¹ or mol m⁻² s⁻¹]

σ = active site density [mol m⁻²]

cat_SA = catalyst surface area [m²]

θ = adsorbed species concentration matrix [mol m⁻²]

- Solve a system of ODEs
- solve_ivp
- Method: 'BDF' (backward differentiation formula)
- Example input



Gas Phase Rate Constants

The forwards rate constant was calculated using the Arrhenius equation. The equilibrium constant relation was used in order to determine the backwards rate constant.

$$k_f = A_f \exp\left(-\frac{E_a^f}{RT}\right)$$

$$k_b = \frac{k_f}{K}$$

$$\Delta G^0 = \Delta H^0 - T\Delta S^0$$

$$\Delta G^0 = -RT \ln K$$

A_f = pre-exponential factor
[1/s or m³/mol s or m⁶/mol² s]

E_a^f = activation energy
[kJ/mol]

K = equilibrium constant

Surface Reaction Rate Constants

For adsorption steps, the following equation was used:

$$k = \frac{S_o}{\sigma^n} \sqrt{\frac{RT}{2\pi M}}$$

S_o = the initial sticking probability

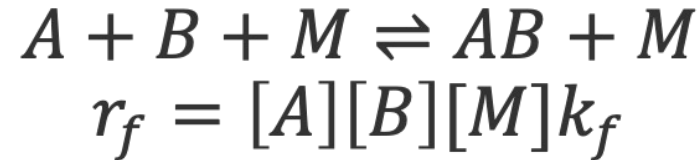
σ = the density of active sites
[mol/m²]

n = reaction order

M = the molar mass [kg/mol]

Third-Body Modeling

- Implemented third-body modeling using and inert (N_2) as the third body. Third body modeling is an integral part of this kinetic model.



Catalyst

Sn/Li/MgO

- BET surface area = $2800 \text{ m}^2/\text{kg}$
- Density = $2300 \text{ kg}/\text{m}^3$
- Porosity = 0.27
- Areal density = $1.14\text{e-}5 \text{ mol site}/\text{m}^2$

Assumed 100 mg of catalyst

- Catalyst surface area = 0.28 m^2

Conditions³

- $T = 750^{\circ}\text{C}$, $P = 130 \text{ kPa}$
- Runtime = 0.0124 seconds
- CH₄ initial fraction = 0.1
- $\text{CH}_4/\text{O}_2 = 2$
- $[\text{CH}_4]_0 = 1.54 \text{ mol/m}^3$
- $[\text{O}_2]_0 = 0.77 \text{ mol/m}^3$
- $[\text{N}_2]_0 = 12.5 \text{ mol/m}^3$
- Reactor volume = $3.27\text{e-}5 \text{ m}^3$
- Gas volume = $3.19\text{e-}05 \text{ m}^3$
- Weight of Catalyst/Flowrate = 2 kg s/mol

3. Couwenberg, P. M.; Chen, Q.; Marin, G. B. Kinetics of a Gas-Phase Chain Reaction Catalyzed by a Solid: The Oxidative Coupling of Methane over Li/MgO-Based Catalysts. *Industrial & Engineering Chemistry Research* **1996**, 35 (11), 3999–4011.
DOI:10.1021/ie9504617.

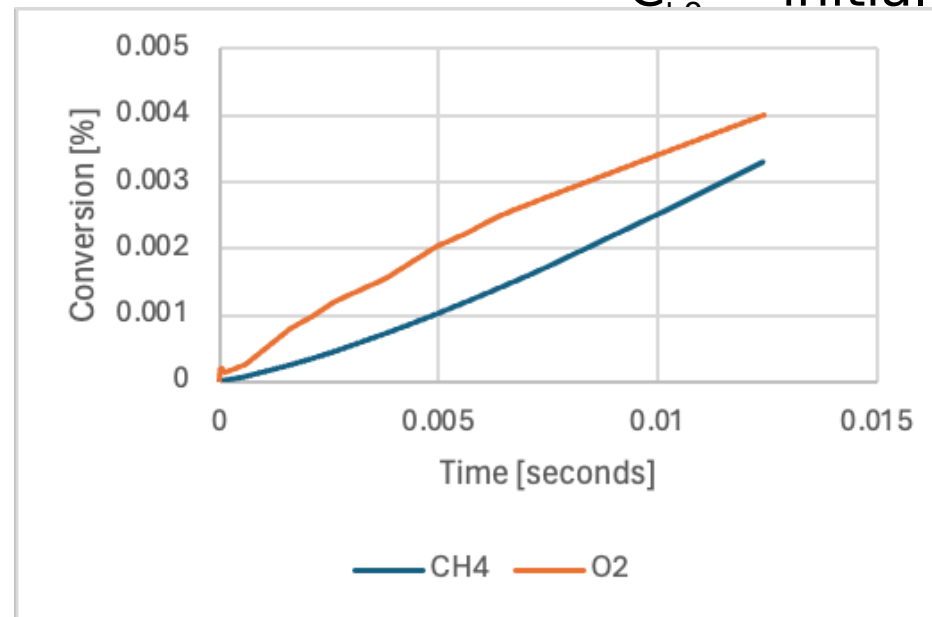
Conversion

- Very little conversion of both CH₄ and O₂
 - Maximum conversion of CH₄ = 3.31e-5%
 - Maximum conversion of O₂ = 4.01e-5%

$$\text{Conversion} = \frac{C_{i,o} - C_{i,t}}{C_{i,o}} \times 100$$

$C_{i,t}$ = concentration of species i at time t

$C_{i,o}$ = initial concentration of



Yield

- Very little yield for all species

$$yield = \frac{num_mol_CH4 \times C_{i,t}}{C_{CH4,0}} \times 100$$

num_molCH4 = moles of CH4 required to produce species i

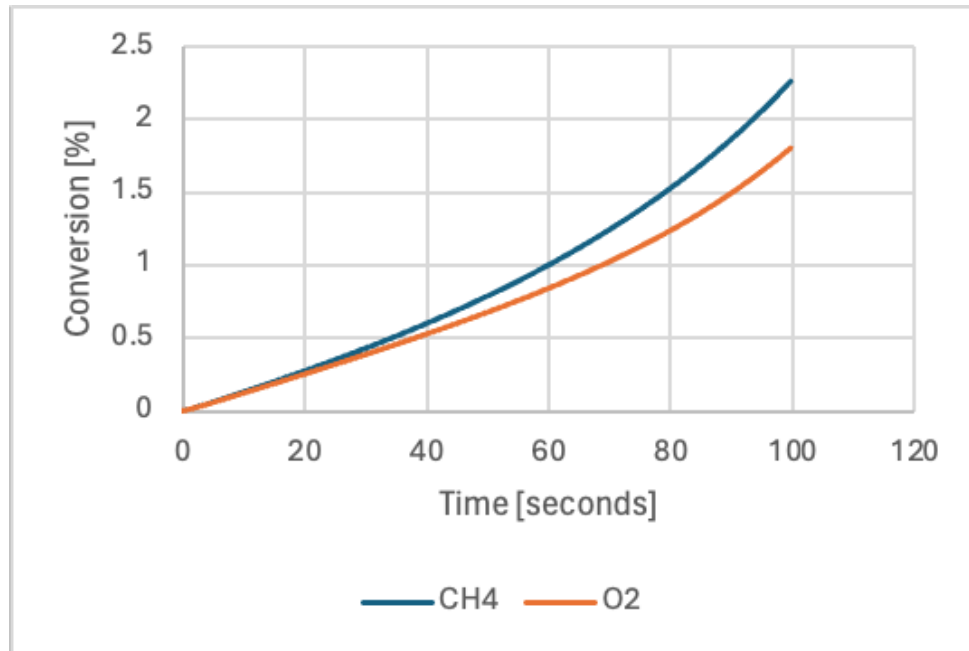
$C_{i,t}$ = concentration of species i at time t

$C_{CH4,t}$ = initial concentration of CH4

Species	Maximum Yield [%]
Ethane (C ₂ H ₆)	2.69e-3
Ethylene (C ₂ H ₄)	5.71e-7
Acetylene (C ₂ H ₂)	3.23e-11
Propane (C ₃ H ₈)	5.32e-12
Propylene	4.92e-11

Increase Runtime

- Modify rate constants to create a less stiff reaction network
- Increased the runtime to 100 seconds



Maximum conversion of CH₄ =
2.27%

Maximum conversion of O₂ =
1.82%

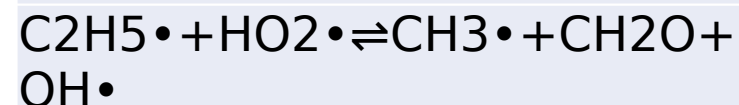
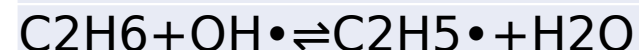
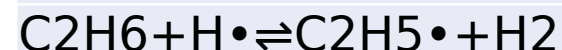
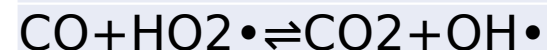
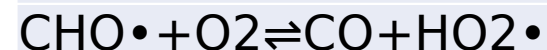
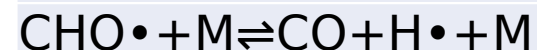
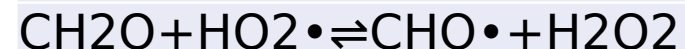
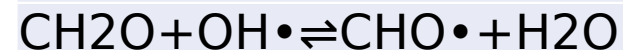
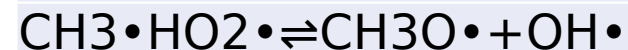
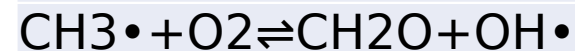
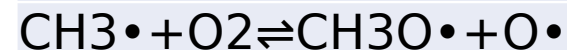
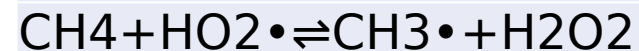
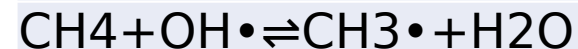
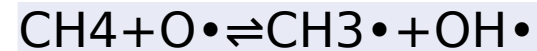
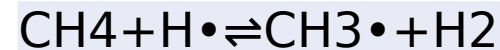
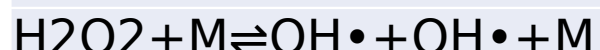
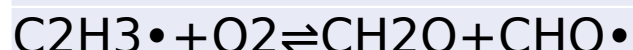
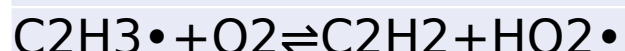
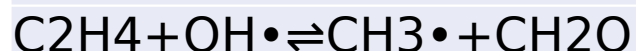
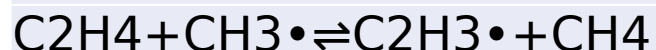
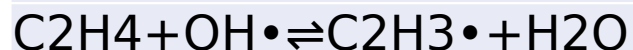
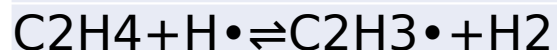
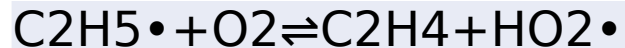
Species	Maximum Yield [%]
Ethane (C ₂ H ₆)	1.46
Ethylene (C ₂ H ₄)	0.346
Acetylene (C ₂ H ₂)	6.30e-4
Propane (C ₃ H ₈)	1.53e-9
Propylene (C ₃ H ₆)	0.029

Future Directions

- Increase the amount of catalyst
- Model different types of reactors (PFRs, CSTRs, etc.)\
- Model UV-PIMS
- Compare to experimental data

Thank you!

Gas Phase Reactions



Catalytic Reactions

