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ELECTRICAL CONDUCTIVITY AND ELASTIC MODULI  
OF PRESSURE-SINTERED LITHIUM SUBSTITUTED  
NICKEL OXIDE

by

Michael Richard Notis

A Dissertation

Presented to the Graduate Faculty

of Lehigh University

in Candidacy for the Degree of

Doctor of Philosophy

in

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1969

CERTIFICATE OF APPROVAL

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## ABSTRACT

Polycrystalline nickel oxide and lithium substituted-nickel oxide alloys ranging from 0.12 to 8.23 atomic percent lithium were prepared by vacuum pressure sintering. Changes in particle texture and shape, increased relative density, larger final grain size and a shifting fracture mode were observed with increased lithium content. This sintering behavior was interpreted in terms of enhanced oxygen diffusion caused by either a decrease in the chemisorptive surface properties or by an increase in the "mobility" of a coupled anion vacancy-electron hole complex.

Pure nickel oxide was found to tend very close to stoichiometric proportions, deviations from stoichiometry being predominantly caused by the impurity-affected surface properties of the material. The composition of 99.999% pure nickel oxide used in this investigation was found to be  $\text{NiO}_{1.000003 \pm 0.0003\%}$ . Iodometric titration analysis showed the concentrations of  $\text{Li}^{+1}$  and  $\text{Ni}^{+3}$  to be equal in pure single phase  $\text{Ni}_{1-2x}^{+2} \text{Li}_x^{+1} \text{Ni}_x^{+3} \text{O}$ . Analysis also indicated the absence of any detectable metallic nickel and showed no detectable lithium loss during pressure sintering. The discrepancy between these findings and those previously

reported in the literature indicates previous difficulty in the careful preparation and characterization of these materials.

The measurement of Young's modulus as a function of temperature for the lithium-nickel oxide alloy system was found to be a very sensitive method for the determination of the variation of the Néel temperature with composition. The low temperature value of Young's modulus was found to increase with increased lithium content and the temperature of the modulus anomaly was found to decrease linearly with increased lithium content. This behavior was interpreted in terms of Van Vlecks'(1) localized-electron theory of antiferromagnetism.

Resistivity measurements made on well characterized pressure-sintered polycrystalline lithium-nickel oxide alloys agreed with the reported results on single crystal material. These include a break at the Néel temperature, a lower activation energy at higher temperatures than at lower temperatures, and a decrease in the low temperature activation energy with increasing lithium content. The combined trends in the modulus and resistivity as a function of temperature and impurity level were interpreted in terms of Toyozawa's(2) electron-acoustic mode interaction model which predicts an inverse relation between the elastic modulus and the energy difference between the self-trapped

and activated electron states. It was concluded that the success of a quantitatively correct localized electron model appears to depend on the development of a theoretical approach which would simultaneously account for both optical mode and acoustic mode interactions.

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1. "Recent Developments in the Theory of Antiferromagnetism" J. H. Van Vleck, J. Phys. Rad. 12, 262-274 (1951)
2. "Self-Trapping of an Electron by the Acoustical Mode of Lattice Vibration. I." Y. Toyozawa, Prog. Theo. Phys. 26, 29-44 (1961)

## I. INTRODUCTION

The transition metal oxides represent a group of high melting point materials which have electrical properties ranging from that of an insulator, such as pure stoichiometric nickel oxide (1), to excellent metallic conduction, such as is found in  $\text{TiO}$  and  $\text{V}_2\text{O}_3$  (2). In the years 1948 through 1950, Verwey and coworkers (3,4) demonstrated that the addition of suitably sized, fixed valence impurity ions to the oxide of a transition metal that possesses variable valence can cause extremely large changes in conductivity. These changes are accomplished without the creation of vacant lattice defects and thus, as a group, these materials represent electronic conductors of high stability. These authors noted that the resistivity as a function of temperature could be represented by an activated process, and they ascribed the activation energy to the ionization of the electron-hole and its removal from the vicinity of the trivalent cation-monovalent impurity source. Verwey proposed the use of these materials as thermistors, but further extension of the same approach to impurities which increase the resistivity, such as  $\text{Cr}_2\text{O}_3$  (5), could result in their use as stable balanced resistors over wide temperature ranges.

Heikes and Johnston (6) reasoned that if carrier generation was the activated process and if the activation energy was the work required to separate a trivalent transition metal ion ( $T^{+3}$ ) from a monovalent impurity ion ( $M^{+1}$ ), then the activation energy should vanish at approximately 10%  $M^{+1}$  (each transition metal ion having at least one impurity ion nearest neighbor). Because their experimental results indicated that the activation energy did not disappear, they concluded that the mobility, rather than the carrier generation, was the activated process. They expressed the resistivity as

$$\rho = \rho_0 T e^{\epsilon/kT} \quad \text{where}$$

$$\rho_0 = \frac{a k c}{q^2 v_0 X}$$

$a$  = lattice constant

$k$  = Boltzmann's constant

$q$  = charge on an electron

$v_0$  = lattice vibration frequency

$X$  = mole fraction impurity ion

$c$  = constant related to the entropy of activation

and  $\epsilon$  = mobility activation energy.

The trivalent cation has a smaller ionic radius and a higher effective charge than the divalent cation and, therefore, causes a localized collapse of the anion lattice. The trivalent cation is thus "self-trapped" by the lattice pol-

arization or the elastic lattice distortion. A qualitative description of the Seebeck effect in hopping conductors was provided by Heikes (7) by assuming one-half of the energy for a jump to be absorbed at the initial site and one-half at the final site. In order to obtain a more quantitative description of the transport properties of low mobility materials it has been found necessary to provide a more sophisticated model. If the lattice is assumed to remain perfect and the polarization or lattice distortion is instead "quantized" and associated with the electron-hole, then a hypothetical "polaron" may be used to obtain more rewarding information.

Polaron models based on electron-optical phonon interactions have been developed by Yamashita and Kurosawa (8), Sewell (9), and Holstien (10), while Toyozawa (11,12) and Schnackenberg (13) have treated electron-acoustic phonon interactions. At low temperatures the electron-optical phonon interaction models yield a picture of a heavy particle moving in a narrow band ("polaron band") while at higher temperatures, the models predict localization of the polaron and a thermally activated mobility. The development of the polaron theories also made possible the explanation of experimentally observed Hall effects which could not be explained by the simple hopping model. The difficulty with the polaron theories is that the necessary sim-

plifying assumptions (such as either only optical mode or acoustic mode interactions) yield incomplete results.

It is interesting to note that after almost thirty years of intense investigation the controversy as to the nature of the conduction mechanism in low mobility solids has still not been solved. In a recent volume of Solid State Physics, Adler (14) states that:

"Five years ago, a review of the electrical properties of the transition metal oxides would have concluded that the dominant mode of transport was by means of uncorrelated hopping of small polarons. It now appears that this is never the case..."

In the same volume, Appel (15) asks:

"Is there experimental evidence for localized small polarons and for their phonon-activated hopping motion? The answer to both parts of this question is yes!"

Part of the reason for this problem is the lack of a clear quantitative theoretical basis for all but the normal wide band semiconductors and part is the nature of the material itself. Many of the transition metal oxides have fairly large deviations from stoichiometry (16) and thus specimen preparation plays a large role in the ultimate magnitude of the electrical transport properties which they exhibit. The refractory nature of the oxides makes the growth of large stress-free perfect crystals very difficult and susceptible to contamination, while at the same time causing problems such as non-uniform segregation of

doping impurities during crystal growth. In addition, uniformly high alloy concentrations are almost impossible to achieve due to the nature of the growth process itself. Thus, many of the published works on transition metal oxides are based on the use of poorly characterized polycrystalline samples (17).

Recent advances in purification techniques such as zone refining (18,19) and in the fabrication of high density polycrystalline ceramics (20) offer the opportunity of producing polycrystalline oxide materials capable of being used as reliable and economic electronic materials. The purpose of this work is to elucidate the elastic and transport properties of lithium substituted nickel oxide and to show the capability of fabricating well characterized polycrystalline electronic materials.

## II. EXPERIMENTAL PROCEDURES

### A. Powder Preparation

The chemical composition of the materials used in this investigation are given in Table 1. Except where specifically noted, the Johnson-Matthey 99.999% pure nickel oxide powder was used for preparation of the alloy powders. The nickel oxide powder and the alloy doping additions were weighed out in 100 gram charges, mechanically mixed for ten minutes and then air fired at 900°C for 10 hours in a covered high purity alumina crucible. The porous slug was then ground in an alumina mortar and pestle until the powder passed through a 325 mesh sieve. The alloy powder was then washed in hot distilled and deionized water until the solution indicated a neutral pH. The powder was then dried for 24 hours at 140°C.

### B. Vacuum Pressure Sintering

Pressure sintering was performed in a Model 1-2300 vacuum pressure sintering furnace manufactured by Vacuum Industries, Somerville, Massachusetts (Figure 1). This unit consists of a cold wall vacuum furnace equipped with a 15 kw - 9600 cycle per second induction heating unit and is capable of reaching 1500°C. The pressure is supplied

through two vertical rams, the lower ram rigidly mounted to the frame and the upper ram connected to a hydraulic actuator that is mounted on the top of the frame.

The hydraulic pressure in the original system was controlled by a pneumatically-operated static pump which allowed the ram force to vary by  $\pm 1200$  pounds (21). Due to the high initial densification rates observed in this study during sintering, this variation caused the specimens to crack as the pressure control system would cause the pressure to surge in order to keep up with the densification rate. The static pumping system was replaced with a dynamic system (Greenlee Model 1721 Hydraulic Power Pump) having an oil flow capability of 30 cubic inches per minute at 10,000 psi. The oil flow was controlled by a stainless steel needle valve which was water cooled at  $13 \pm 4^\circ\text{C}$ . The water cooling was necessary in order to remove the heat generated as the oil was pumped through a large pressure differential and to keep the orifice size from expanding or contracting due to ambient temperature changes. This system provided very smooth pressure control within  $\pm 2$  percent of any given setting.

The major disadvantage of the system was the lack of any capability for hot ejection of the specimen and the resulting concern over the difference in thermal shrinkage rate of the specimen and the die. In addition, the high

pressures used in this study necessitated the use of high strength refractory metal dies. In turn, because the lithium additions in the specimen tended to react with the metal die, a compound die design similar to that of Moss and Stollar (22) had to be used. The final die design that was used for this study is shown in Figure 2. It consisted of a 1" I.D. X 1/4" wall high purity, high strength WEAROX (\*) alumina tube inserted within a 1-1/2" I.D. X 3" O.D. T.Z.M. (+) die, and a 1/8" thick X 1" diameter alumina spacer inserted between the specimen and each of the T.Z.M. plungers. The wall thickness of the alumina insert was chosen so that it would be thick enough to avoid cracking of the wall at an applied pressure of 20,000 psi, but thin enough so as to provide maximum T.Z.M. die wall thickness for coupling to the induction heating system and for safe operation of the die system at high pressures. In addition, two Pt-Pt 10% Rh thermocouples were inserted in the T.Z.M. die wall and graphite susceptors were placed around the T.Z.M. die and each of the plungers. The temperature difference between the two thermocouples was never greater than 10°C and previous radial temperature profiles with a similar die system (23) indicated a maximum temperature dif-

---

(\*) Trade name of Western Gold and Platinum Co., Belmont, Calif.

(+) Proprietary name of Climax Molybdenum Co., Coldwater, Mich. for a Mo-0.5% Ti-0.08% Zr wrought alloy.

ference of 15°C at 1300°C.

The operational sequence was such that approximately 25 grams of loose alloy powder was loaded into the die system and the powder was then compacted by the plungers at a pressure of 80 psi. The vacuum furnace was then closed, pumped down, and the temperature was raised to and held at 550°C ± 50°C for 30 minutes. The control temperature setting was then increased and pressure was slowly applied to the specimen so that the full operating pressure was reached before the temperature of the system reached 750°C ± 50°C. The temperature was then increased to the desired sintering temperature and held at that temperature for 90 minutes. The pressure was then released, the ram was raised, and the system was cooled at a rate of approximately 175°C per hour to 600°C and then all power was turned off and the system allowed to cool overnight. The specimen was unloaded and cut out of the alumina insert with a diamond blade by making two longitudinal cuts 180° apart along the axis of the insert.

The upper cross-frame of the pressure sintering unit was equipped with a linear variable differential transformer (Sandborn 7-DCDT). The core of the L.V.D.T. was attached to the upper ram and the signal from this system was fed to a Varian F-80A X-Y recorder. Thus a relative measure of the rate of densification was obtained from the

ram displacement. A time equal to twice the time when ram motion ceased, 90 minutes at temperature and pressure, was chosen for all of the remaining runs.

The ambient vacuum level within the chamber was allowed to decrease to slightly less than 100 microns before initial heat was applied, was held to approximately 20 microns during heating to maximum temperature, and was held at approximately 0.1 micron during pressure sintering and the cooling part of the cycle. Some of the pure nickel oxide specimens were observed to have two phase structures (less than 1% metallic nickel). These specimens were fired in air at 1350°C for 24 hours, were then reexamined, and found to possess single phase structures near theoretical density.

### C. Chemical Analysis

Lithium was analyzed by using flame photometric methods. Lithium standards were prepared by drying reagent grade lithium carbonate (Table 1) at 120°C for 24 hours and then dissolving 4.945 grams of the dried powder in 300 ml of distilled and deionized water (\*). Carbon dioxide was then released by the addition of 15 ml. of concentrated HCl,

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(\*) All analyses and washing operations were carried out with distilled water passed through a mixed-bed ion-exchange resin column.

and the solution was then diluted to 1 liter. This provided a stock solution equivalent to 4,000 ppm Li. The stock solution was diluted to 1/4, 1/3, 1/16, 1/32 of the original stock concentration for calibration solutions. The sample solution was prepared by dissolving approximately 0.5 grams of unknown in 7.5 ml of hot concentrated HCl and then diluting to 25 ml (the sample weight or concentration was readjusted in a second run if the original sample did not fall approximately midway between the calibration solutions). Analyses were performed on a Beckman Model DU Flame Photometer using a Model 4030 Medium Bore Atomizer-Burner with gas pressures of 3.5 psig for the acetylene and 8.5 psig for the oxygen. The slit width was set at 0.15 mm and the 670.8 m $\mu$  lithium line was monitored (24). The standard calibration procedure for the instrument was modified in order to use the full width of the transmission scale. After adjusting the sensitivity and burner controls in the normal manner, the following sequence was used:

- (1) With the shutter closed, adjust the dark-current milliammeter to zero.
- (2) Place the highest concentration calibration solution in the burner, open the shutter, and vary the wavelength until maximum response is indicated. Set the transmission scale to 100 and balance the instrument by adjusting the sensitivity control.

- (3) Place a "blank" of deionized water in the burner and adjust dark current to zero.
- (4) Repeat steps (2) and (3) until "blank" reads zero and highest standard reads 100 on the transmission scale.

Previous reports have indicated anomalously high readings with  $H_2SO_4$  solutions (24, 25) and low lithium results in the presence of nickel (25). Prior to establishment of the above procedure, lithium standards were run in both HCl and  $H_2SO_4$  solutions and in the presence of nickel (as nickel chloride). No evidence of any change in the readings was indicated.

The lithium content in the nickel oxide alloy sample, expressed as mole fraction lithium, was calculated from the equation:

$$X = \frac{(W_L)(74.71)}{[(36.9455)(W_S) + (W_L)(51.77)]}$$

where  $W_S$  = Weight of sample per liter

$W_L$  = Equivalent weight per liter of  $Li_2CO_3$  for equal transmission.

Trivalent nickel was analyzed by iodometric titration. A schematic representation of the dissolution equipment is shown in Figure 3. Due to its extended length, the exact procedure is outlined in Appendix I. All of the analyses were performed with the same lot of concentrated (36.5 to

38 per cent) hydrochloric acid (\*). A "blank" run using this acid gave no indication of the formation of free iodine. In practice, a minimum amount (2 to 7 ml) of acid was used to dissolve the sample, and the sample weight was varied (0.1 to 0.5 grams) in order to maintain the volume of 0.01N standard sodium thiosulfate (†) titrating solution within reasonable working limits. The sample powders were passed through a #325 mesh (44 $\mu$ ) screen prior to analysis.

#### D. Modulus Measurements

Young's modulus as a function of temperature for both pure and doped nickel oxide specimens was measured using a three-part "composite oscillator" method. The furnace was constructed from a 3 inch I.D., 1/4 inch wall thickness, 10 inch long Norton "Alundum" refractory tube wound with 20 gauge Nichrome V wire, with six turns per inch over the central seven inches of the tube. The winding was coated with "Alundum" cement and then the assembly was placed inside a four inch I.D., 1/8 inch wall thickness type 304 stainless steel furnace shell. The gap was packed with

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(\*) A.C.S. Reagent Grade Hydrochloric Acid, Fisher Scientific Co., Lot 772438, Maximum Limits of Impurity: Free Cl - 0.0000%, Sulfites (SO<sub>3</sub>) - 0.00008%, Sulfates (SO<sub>4</sub>) - 0.00008%, Heavy Metals (as Pb) - 0.0001%, Residue on Ignition - 0.0004%, Fe - 0.00001%, As - 0.000001%, NH<sub>4</sub> - 0.0003%.

(†) Sodium Thiosulfate (Na<sub>2</sub>S<sub>2</sub>O<sub>3</sub>), Baker "Dilut-it", 0.01N  $\pm$  0.1%, Lot #000-15283-3594.

"Alundum" insulating powder and type 304 stainless steel end pieces were used to seal the powder in and to hold the refractory tube in place. A thin walled iron tube was placed inside the refractory tube in order to provide a more uniform temperature profile; electrical contact was maintained between the inner iron tube and the outer stainless shell both of which were grounded directly at the vertical input of the oscilloscope. A.C. line voltage was controlled by a 0 - 10 ampere Powerstat and monitored by a General Radio Type 1806-A Electronic Voltmeter connected across the furnace input terminals. Furnace profiles indicated that a temperature variation of  $\pm 2^{\circ}\text{C}$  was maintained in the central two inches of the furnace at intermediate temperatures (room temperature to  $250^{\circ}\text{C}$ ),  $\pm 5^{\circ}\text{C}$  at higher temperatures ( $250^{\circ}\text{C}$  to  $450^{\circ}\text{C}$ ) and that a temperature variation of  $\pm 1.5^{\circ}\text{C}$  was maintained in a one inch furnace length over the entire temperature range.

The driver and gauge transducers for the composite oscillator consisted of two "X-cut" piezoelectric quartz crystals (\*). Each of the quartz crystals had a  $1/4"$  X  $1/4"$  cross-section, its Y-axis oriented along the length of the crystal, and the X- and Z-axes perpendicular to the other faces. The X-cut faces were vapor plated (†) with chromium,

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(\*) Purchased from Piezo Co., Carlisle, Pa.

(†) Courtesy of Bell Telephone Laboratories, Allentown, Pa.

for good adherence, and gold, for good electrical contact under high temperature conditions. This orientation has been found to provide high intensity pure longitudinal vibrations with good temperature stability (26).

The "Lavite" (\*) holding fixture for the composite oscillator supported four 1/4 inch wide, 1-1/4 inch long, 0.015 inch thick stainless steel spring strips. A fine tungsten point with a 0.001" tip radius (†) was passed through a small hole in the upper end of each of the flat springs and was then silver-soldered to it. The spacing in between each set of points was set at 3/16" so that they would maintain a positive holding pressure on the 1/4" quartz crystals. Stainless steel wire leads were silver-soldered to the lower part of each of the spring strips. These leads emerged from the furnace through "Lavite" end pieces and provided electrical contact to the assembly. A 1/4" x 1/4" x 2" long "Lavite" bar with a 1/8" diameter x 1" deep hole along its length axis was cemented to the center of the top surface of the holding fixture. Temperature readings for all of the runs were read from a Pt-Pt 10% Rh thermocouple (#) placed inside this bar. Prior to any of

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(\*) American Lava Corp., Chattanooga, Tenn.

(†) Semimetals, Inc., Westbury, Long Island, New York.

(#) All thermocouples were calibrated in boiling distilled water and read  $100.375^{\circ}\text{C} \pm .000_{125}^{\circ}\text{C}$ .

the experimental runs, a second bar identical to that described above was placed between the tungsten points, and the temperature difference between the oscillator position and the "monitor" thermocouple position was determined over the temperature range 0 - 390°C. The "equilibrium" temperature gradient was found to be less than 1 °C over most of the range, and this value was reached within 15 to 20 minutes after temperature changes of 25 to 50 °C were made. An inert gas atmosphere of CO<sub>2</sub> or pre-purified N<sub>2</sub> was maintained within the furnace for these and all succeeding runs.

The quartz crystals were frequency matched within 0.7 per cent. Matching of the specimen and the crystals will be discussed in the Results and Discussion section. Calibration curves for the frequency versus temperature response of each of the crystals were determined by placing marked and identified crystals in the composite oscillator holder inside the furnace but without the specimen cemented between them. The composite oscillator was then prepared by cementing a specimen of similar cross section between the crystals with GA-60 (\*) epoxy strain gauge cement. Pressure was applied as the system was being cemented together in order to squeeze as much cement out of the joint as possible. A thin cemented joint was desired in order to produce good coupling between the various components of the oscillator.

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(\*) Automation Industries, Instrument Div., Phoenixville, Pa.

The assembly was baked in a drying oven at 120°C for one hour and then placed in the holding fixture so that the quartz crystals were in the same position as when they were calibrated. The assembly was positioned so that the center of the specimen fell directly over the center of the monitor thermocouple block and the tungsten points held the quartz crystals at their respective centers (nodes). The holder was then situated so that the center of the specimen fell at the center of the thermal flat within the furnace.

A schematic of the measuring equipment is shown in Figure 4. The signal from a 2c-2mc General Radio type 1310-A Variable Frequency Oscillator was monitored with a General Radio Type 1150-BPH Digital Frequency Meter which had an internal 100 kc test crystal. Frequency control of 1 cps in 200,000 cps was achieved by placing a three turn 1.5-5 picofarad variable capacitor across the main frequency control of the oscillator. The 600 ohm output of the oscillator was modified by the addition of a 0 - 2.5 megohm potentiometer so that the output could be controlled at 0.2 volts over the entire frequency range. The output was then fed to a 20c - 3 mc General Radio Type 1233-A Power Amplifier. The constant 0.2 volt input produced maximum output and no signal distortion from the power amplifier. The output from the amplifier was monitored by a General Radio Type 1806-A Electronic Voltmeter, and was connected to the

driving crystal of the composite oscillator. The signal from the gauge crystal of the composite oscillator was fed directly to the vertical input of a Hewlett-Packard Model 130-B oscilloscope. Electrical ground was maintained throughout the system by grounding the shielded cable at each input and output terminal, connecting the grounded side of both crystals together, and carrying this ground connection directly to the scope. A clear undistorted signal was then obtained, and resonance was determined by varying the oscillator until maximum peak height was achieved on the scope. The furnace temperature, resonant frequency, magnitude of the output signal from the amplifier, and the peak-to-peak voltage from the scope were recorded and used to calculate the modulus and relative acoustic loss.

#### E. Resistivity Measurements

Four point probe dc resistivity measurements as a function of temperature were made on the same samples as were used for the modulus measurements. A schematic diagram of the measurement circuit is shown in Figure 5. Measurements were made inside a platinum wire-wound vertical quartz tube furnace that was insulated with Johns-Manville "Min-K" high temperature quartz fiber. The specimen was cut into a rectangular bar approximately 0.1 inches thick, 0.15 inches wide and 0.5 inches long, and then placed on a fused quartz microslide at the end of an alumina multibore tube. The

physical arrangement of the fixturing is quite similar to that used for previous investigations and is adequately described in the literature (27, 28). Platinum leads were attached to the specimen with 80% Au-20% Pt alloy paste (\*), and the contacts were sintered at 800°C for one hour.

Measurements made with wide variations in the current indicated the contacts to be ohmic. A switching network was provided so that current flowed through the specimen only while a measurement was being made and current and voltage reversals made during each run indicated the absence of any measureable thermoelectric effects. A monitoring Pt-Pt 10% Rh thermocouple placed in contact with the quartz microslide and directly under the specimen indicated a temperature within 2 degrees of that indicated by the furnace control thermocouple placed 1/2 inch away from the specimen. The temperature was slowly increased from room temperature to 400°C over a six hour period and then allowed to cool at a similar rate (1.1°C/min).

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(\* ) Squeegee Gold Alloy Paste #A-1199, Engelhard Ind., East Newark, N.J.

### III. DISCUSSION AND RESULTS

#### A. The Ni-O System

The only known investigation of the Ni-O phase system was performed by Bogatskii (29) whose results are shown in Figure 6. There is a small region where solid solutions of  $O_2$  in Ni are formed at concentrations up to one weight per cent  $O_2$ . The liquidus curve drops from approximately  $1450^\circ C$  for the melting point of Ni to a eutectic at  $1438^\circ C$  and 1.5 weight per cent  $O_2$ , then rises to approximately  $1650^\circ C$  at the compound NiO. The curve then drops off almost vertically, levelling off at the melting point of  $Ni_2O_3$  and again at  $NiO_2$ .

In addition to being thermodynamically incorrect, the region between NiO and  $O_2$  points out the argument that has existed since the early 1900s as to the existence of anhydrous higher nickel oxides.

In 1926, LeBlanc and Sachse (30) gave the analysis of the products of  $NiCO_3$  calcination as NiO,  $Ni_2O_3$ , active oxygen and water, when calcined in air. They used an iodometric titration technique in order to find the concentration of  $Ni^{+3}$  present and then expressed this as  $Ni_2O_3$ . In another investigation (31), LeBlanc and Sachse attempted to

form  $\text{Ni}_2\text{O}_3$  or  $\text{NiO}_2$  but found only nickel oxide with up to ten per cent excess oxygen ( $\text{NiO}_{1.1}$ ). Lunde (32), in 1927, reported that slow heating of  $\text{Ni}(\text{NO}_3)_2$  produced a black powder having an analysis nearly that of  $\text{Ni}_2\text{O}_3$  but with the x-ray pattern of  $\text{NiO}$ . Commenting on Lunde's work, LeBlanc and Sachse (33) argued that his material was probably a mixture of  $\text{NiO}$ , active oxygen, water, with possibly only a maximum of ten per cent of higher nickel oxides. Lunde then proposed (34) that the material could also be a hydrated higher nickel oxide such as  $\text{NiO}_2 \cdot \text{XH}_2\text{O}$ .

Holtermann (35) reported that higher oxides were extremely unstable and that only the monoxide could be identified, while Bogatskii (29) reported that  $\text{NiO}_2$  was stable under "high pressure" and that  $\text{Ni}_2\text{O}_3$  had a crystal structure and unit cell very close to that of  $\text{NiO}$ . In 1954, Shimomura and coworkers (36) reported that nickel oxide with up to 20 per cent excess oxygen still had the  $\text{NiO}$  structure and that no higher compounds could be found. In 1956, Rode (37) observed nickel oxides with up to 32 per cent excess oxygen without any evidence of anhydrous  $\text{Ni}_3\text{O}_4$ ,  $\text{Ni}_2\text{O}_3$  or  $\text{NiO}_2$ , although hydrides of higher oxides were definitely thought to be present. Based on a very thorough study of reaction products from nickel cathodes in electrolytic cells, Briggs and Wynne-Jones (39) also concluded that no anhydrous higher oxides could be identified. In addition,

based on a study of x-ray fine structure, Tsutsumi (40) stated that compounds identified as  $\text{Ni}_2\text{O}_3$  were actually  $\text{NiO}$  plus  $\text{NiO}_2 \cdot \text{XH}_2\text{O}$ . However, in 1957, Finch and Sinha (41) identified a complex nickel spinel  $\text{Ni}_{28}\text{O}_{32}$ , and in 1959, Bogatskii and Mineeva (42) again identified both  $\text{NiO}_2$  and  $\text{Ni}_2\text{O}_3$  which decompose at  $50^\circ\text{C}$  and  $350^\circ\text{C}$  respectively.

Finally, Labat (43) made an extensive review of the conflicting information and concluded that although the existence of higher anhydrous nickel oxides was largely doubted, it seemed to be well established that their hydrates or combinations with alkali or alkali-earth oxides were well established. Tuomi (44) came to similar conclusions in 1965.

The extent of non-stoichiometry in nickelous oxide has also been the source of much controversy. In 1930, LeBlanc and Sachse (45), performing the first work with bulk material rather than powder, found that  $\text{NiO}$  dissolves only a "small" quantity of oxygen without forming higher oxides. In 1931 they measured the conductivity of these bulk samples (46) and found that "pure"  $\text{NiO}$  had a conductivity of  $10^{-8} \text{ (ohm-cm)}^{-1}$  while  $\text{NiO}$  with 5 per cent excess oxygen ( $\text{NiO}_{1.05}$ ) had a conductivity of  $10^{-3} \text{ (ohm-cm)}^{-1}$ . Klemm and Haas (47) noted a wide variation in magnetic susceptibility and the presence of metallic nickel in their work on powdered materials and proposed that stoichiometric nickel ox-

ide was unstable and would break down to  $\text{NiO}_{1.005}$  and metallic Ni. Baumbach and Wagner (48) found a maximum deviation from stoichiometry of  $\text{NiO}_{1.0005}$  to  $\text{NiO}_{1.005}$  working with oxidized nickel foil, and Boswell and Iler (49) found a maximum of  $\text{NiO}_{1.006}$  when working with sintered but porous specimens. Even with oxygen pressures up to 300 atmospheres, Holtermann (35) was able to obtain a maximum deviation from stoichiometry of  $\text{NiO}_{1.07}$  with powder material, while Shimomura and coworkers (36) obtained results between  $\text{NiO}_{1.02}$  and  $\text{NiO}_{1.2}$  at 0.21 atmospheres pressure. In 1962, Perakis (50) found a maximum deviation from stoichiometry of  $\text{NiO}_{1.0196}$  and a minimum of  $\text{NiO}_{1.0007}$  in equilibrium with metallic nickel. In 1964, Blaise and Lefevre (51) gave an analysis of  $\text{NiO}_{1.00098}$ . In 1965, Cherkashin (52) reported a range of  $\text{NiO}_{1.00013}$  to  $\text{NiO}_{1.0224}$ , and in 1966, Gravelle, Shobaky and Urbain (53) reported an analysis of  $\text{NiO}_{1.00016}$ , all on powdered materials. In 1968, Fender and coworkers (54) reported an analysis of  $\text{NiO}_{1.000 \pm 0.002}$  for spectrographically standardized powder obtained from Johnson-Matthey Chemicals (metallic impurities less than 15ppm).

The above discussion is summarized in Table 2. There appears to be a striking correlation between the nature of the sample (powder versus bulk material), the year of investigation (or realistically the purity), and the observed maximum deviation from stoichiometry. Gossel (55,56) has

made the observation that the nonstoichiometry of nickel oxide is mainly a surface property and that surface conditions affected the excess oxygen content to a much greater extent than did variations of temperature and atmospheric conditions. LeBlanc and Sachse (31) and Charman and co-workers (59) both found a rapid change in color from black to green when nickel oxide powder was placed in an acid-KI titration solution, which suggested that excess oxygen was present only at the surface. The surface properties and catalytic activity of nickel oxide have been quite extensively studied by many investigators (55-61) and since, in general, the study of the chemistry and physics of surfaces becomes a science unto itself, it will not be dealt with here except for one experimental observation in the next paragraph.

"Pure" reagent grade nickel oxide from Fisher Scientific or Baker Chemical Company having an olive green color, 99.9% pure nickel oxide from Atomergic Company having a grey color, and 99.999% pure nickel oxide from Johnson-Matthey Company having a bright "Kelly Green" color were all fired in cleaned high purity silica or alumina crucibles at temperatures between 800°C and 1000°C. While all the other powders tended to change to a lighter green color, the Johnson-Matthey powder remained the same green color. In addition, the same powders fired in crucibles contaminated

with small amounts of lithium all formed sintered "cakes" that were black on the outside but bright green towards the center. Keeping in mind that all previous investigations have associated the bright green color with nearly stoichiometric nickel oxide, it is concluded that the extent of deviation from stoichiometry (or the quantity of excess oxygen) is an impurity affected-surface controlled effect (see Table 1 for chemical analysis of powders).

The early development of the quantitative relationship between imperfections, the departure from stoichiometry, electrical conductivity, matter transport and chemical reactions in the solid state can largely be attributed to the work of Schottky (62), Wagner (63), Mott (64), Hauffe (65) and Kroger and Vink (66). Using the law of mass action as first applied to this type of system by Wagner, and the relationship between the self diffusion coefficient of  $\text{Ni}^{+2}$  and nickel vacancies as given by Mott, the concentration of vacancies has been given by Mitoff (67) as:

$$[V_{\text{Ni}}''] = 7.8 \times 10^{-3} P_{\text{O}_2}^{1/6} \exp(-11,400/RT) \text{vacancies per ion pair.}$$

Based on work by Eror (68) which indicated that a  $P_{\text{O}_2}^{1/4}$  dependence might be more appropriate, Price (69,70) has restated Mitoff's relationship as:

$$[V_{\text{Ni}}'] = 8.97 \times 10^{-3} P_{\text{O}_2}^{1/4} \exp(-11,400/RT) \text{vacancies per ion pair.}$$

Using Mitoff's approach, but with different diffusion data, Error (68) gives the concentration of nickel vacancies as:

$$[V_{Ni}] = 4.58 \times 10^{-5} \exp(+5000/RT) \text{ vacancies per ion pair}$$

in air ( $P_{O_2} = 0.209$ ). Recently, Sockel and Schmalzried (71), using a coulometric titration method with calcia stabilized zirconia as a solid electrolyte, have again found a  $P_{O_2}^{1/6}$  dependence of vacancy concentration, and extrapolation of their results at  $1200^\circ\text{C}$  to  $P_{O_2} = 0.209$  would give  $[V_{Ni}] \approx 3.1 \times 10^{-4}$ . Finally, Ormont (72), using binding energy theory and experimental data existing in the literature found  $[V_{Ni}] \approx 2 \times 10^{-11}$  at  $25^\circ\text{C}$ . A tabulation of the above results is given in Table 3 for  $1200^\circ\text{C}$  and  $25^\circ\text{C}$  where possible.

Comparison of these values with corresponding vacancy concentrations in  $\text{CoO}$  and  $\text{MnO}$  would also be indicative of the relative differences in magnitude for the three compounds. Carter and Richardson (73) found a value of  $8 \times 10^{-3}$  for  $[V_{Co}]$  at  $1150^\circ\text{C}$  and one atmosphere oxygen pressure during oxidation studies with cobalt foil, and Fisher and Tannhauser (74) reported a value of  $1 \times 10^{-2}$  under similar conditions. Error (68) also reported a value of  $1 \times 10^{-2}$  vacancies per ion pair, and extrapolation of Sockel and Schmalzried's work gives the same. As for  $\text{MnO}$ , Davies and Richardson (75) reported a range of stoichiometry from  $\text{MnO}_{1.000}$  to  $\text{MnO}_{1.045}$

at 1650°C with varying pressure, and Eror (68) reported a value of  $2 \times 10^{-3}$  vacancies per ion pair at 1200°C and a partial oxygen pressure of  $7 \times 10^{-10}$  atmospheres. Although Eror's work involved the thermogravimetric analysis of NiO, CoO and MnO, he presented no results for NiO because the change in weight was smaller than the sensitivity limit for his equipment.

The iodometric titration results of the present investigation (discussed in detail in a later section) show a precision of  $\pm 0.0003$  per cent (Table 4) for the lower Ni<sup>+3</sup> concentrations while the "blank" HCl run and both of the unalloyed 99.999% pure nickel oxide powders (as received, and fired) gave no indication of any reaction with KI solution. The analysis of the pure nickel oxide used for this investigation may thus be given as essentially NiO<sub>1.000003</sub>  $\pm 0.0003\%$ . This is in excellent agreement with Fender and coworkers' (54) results on the same powder but with a less accurate method. Comparison of this value with those given in Table 3 indicates good agreement, realizing that even under extremely slow cooling the powder would not be able to reach the equilibrium vacancy value but would rather have a "frozen-in" vacancy concentration corresponding to the higher temperature range. Referring back to the color change observations, it might now be stated that pure nickel oxide tends very close to stoichiometric proportions

and that deviations from stoichiometry are caused only by the impurity-affected surface conditions of the material.

Although electrical conductivity or conductivity type per se is not enough to successfully describe a transport mechanism, a knowledge of both permits some approximate judgments as to the relative position of phase boundaries and the stability of certain types of defects in the lattice. Thus the fact that wüstite in equilibrium with iron at 900°C was determined (76,77) as  $\text{FeO}_{1.05}$  and wüstite in equilibrium with  $\text{Fe}_3\text{O}_4$  was determined as  $\text{FeO}_{1.125}$  while the electrical conductivity has been shown to be p-type only (78,79) indicates that the wüstite phase field is shifted from the nominally stoichiometric compound and that conductivity involves the formation of cation vacancies and higher valence cation states. On the other hand, manganous oxide has been observed with either excess metal or excess oxygen (75,80) and possesses both n-type and p-type conductivity (68,81-83). The phase region for manganous oxide therefore overlaps the stoichiometric compound, has a fairly wide stoichiometry range (75) and conduction may be either by cation vacancies (p-type) or by cation interstitials (n-type) or by anion vacancies (n-type). Cobalt oxide has been reported (83) to have a sign reversal in the slope of the thermoelectric power vs. oxygen partial pressure curve, while neither the thermoelectric power nor conductivity have a sign reversal

themselves. Thus, as mentioned before, cobalt oxide has a fairly small compositional variation near the stoichiometric compound, and also possesses a conductivity type dominated by cation vacancies but with the possibility of small amounts of interstitial cobalt or anion vacancies at very low pressures or at high temperatures (74).

Despite the large number of investigations which have found nickel oxide to possess only p-type conduction, there are a few reports in the literature indicating n-type conductivity. However, due to conflicting experimental observations, all of these reports appear to be highly questionable. Takeuchi and Igaki (84) reported n-type conductivity, but later reported (85) this as "semimetallic conduction accompanied by ferromagnetic behavior." Schlosser (86) noted that nickel oxide doped with gallium was n-type for 0.6 atomic per cent gallium or greater, but Rooksby and coworkers (87) noted the formation of  $\text{NiGa}_2\text{O}_4$  spinel even with very small gallium additions, and El Shobaky and coworkers (88) have noted the increased tendency for the formation of metallic nickel with gallium additions. In 1965, Snowden and Saltzburg (89) reported n-type conductivity through Seebeck-coefficient measurements at room temperature but also reported a sign reversal at  $380 \pm 30^\circ\text{C}$  (the Curie point of nickel). Recent work (90, 91) on the Seebeck coefficient of nickel oxide single crystals as a

function of temperature and pressure indicated no change of sign from p-type conduction, but indirect experimental evidence does exist for an n-type component for the carrier mobility term (92 - 95). This component has, however, been interpreted as being related to an anomalous effect due to internal magnetic fields (92,93), rather than as caused by a second carrier component.

The above discussion thus provides a picture of nickel oxide as having an extremely small deviation from stoichiometry (narrow phase field) shifted to the oxygen excess side but including the nominally stoichiometric compound, NiO. The conductivity may be described as heavily dominated by the formation of cation vacancies and higher valence cations.

#### B. NiO-M<sub>x</sub>O<sub>y</sub> Alloy Systems

A tabulation of the extent of solid solubility of M<sub>x</sub>O<sub>y</sub> oxides in NiO at various temperatures and pressures is given in Table 5, along with known stoichiometric compounds, common valence and size deviation (in per cent) between  $R_{Ni}^{+2}$  and  $R_M$ . The ionic radii used for this tabulation were taken from Pauling (96) because they represent the most complete and consistent set of both divalent and trivalent empirical radii available. In particular, Pauling gives the following pertinent radii:

<u>Element &amp; Valence</u>	<u>Ionic radius, A°</u>
O <sup>-2</sup>	1.4
Li <sup>+1</sup>	0.6
Mg <sup>+2</sup>	0.65
Ni <sup>+2</sup>	0.72
Ni <sup>+3</sup>	0.62
Co <sup>+2</sup>	0.74
Co <sup>+3</sup>	0.63
Fe <sup>+2</sup>	0.76
Fe <sup>+3</sup>	0.64
Cr <sup>+3</sup>	0.69
Cu <sup>+2</sup>	0.69
Zn <sup>+2</sup>	0.74

Using Pauling's value of  $R_{O^{-2}} = 1.4A^{\circ}$ , and the average Ni<sup>+3</sup> - O<sup>-2</sup> interionic distance of  $2.02A^{\circ}$  in Li<sup>+1</sup>Ni<sup>+3</sup>O<sub>2</sub> given by Dyer and coworkers (97) a value of  $R_{Ni^{+3}} = 0.62A^{\circ}$  is obtained which is in excellent agreement with Pauling's tabulation. The observation that  $R_{Mg^{+2}}$  lies between both  $R_{Ni^{+2}}$  and  $R_{Ni^{+3}}$ , and  $R_{Co^{+2}}$  and  $R_{Co^{+3}}$ , might also be made. This fact has been used by Oakey (98) to hypothesize a "pre-relaxation" effect in  $Li_xMg_yCo_{(1-x-y)}O$  alloys.

The NiO-M<sub>x</sub>O<sub>y</sub> systems seem to provide excellent agreement with the Hume-Rothery solid solution rules (99,100). The oxides of Group IA, IIA, IB, IIB show a definite trend towards high solubility when the deviation between cation

radii is less than 20% (SIZE EFFECT). Solubility is generally restricted for almost all systems showing intermediate phase formation (ELECTRONEGATIVE VALENCY EFFECT) such as Group IA and IIIA, or for those oxides with much higher cation valence such as the oxides of the IIIB, IVB, and VB groups. The NiO-ZnO and NiO-CuO systems with up to 35 mole per cent CuO or ZnO soluble in NiO but with almost no NiO soluble in CuO or ZnO(101-103) seem to demonstrate an ELECTRON CONCENTRATION EFFECT ( $\text{Ni}^{++} = [\text{Ar}]^{18}3d^8$ ,  $\text{Cu}^{++} = [\text{Ar}]^{18}3d^9$ ,  $\text{Zn}^{++} = [\text{Ar}]^{18}3d^{10}$ ).

The seeming abnormality in the solubility of Cr(<1%), Mn(100%), Fe(<10%), Co(100%) oxides in NiO may be explained by referring to Figure 7 which is a plot of the free energy of formation (stable oxygen pressure) versus temperature for the compounds of interest. The stable phase field for NiO has wide overlap with the CoO and MnO phases and hence the large solubility, while there is no overlap for the Cr system and therefore low solubility. It may be observed that there is no overlap between the NiO and FeO phases but that the phase fields are fairly close. Indeed, for small additions of FeO to NiO (low activity) the upper stability limit would fall within the NiO stable phase field because of the higher allowed oxygen pressure, while the lower stability limit for FeO would fall even lower because of the lower allowed oxygen pressure before the appearance of

a metallic iron phase. Thus, the stable FeO phase field is wider and overlaps the NiO phase field for low iron concentrations and therefore enables some solubility of the two components.

The first work with the NiO-Li<sub>2</sub>O system was published in 1948 by Verwey and coworkers (3) who found lithium to be soluble in nickel oxide in amounts as great as ten mole per cent and then later (4,104) to be soluble to less than 40 per cent. Kohler and Jamison (105) reported the solubility limit at 28 atomic per cent lithium in thin nickel oxide films, and Heikes and Johnston (6) found difficulty in dissolving more than 15 per cent lithium in the lattice. The compound LiNiO<sub>2</sub> was identified by Dyer, et al (97) and again later by Johnston and coworkers (106). Perakis and coworkers (50,107-109) reported various degrees of ferromagnetism for the system but Fensham (110) working with single and two phase alloys with up to 50 atomic per cent lithium found metallic nickel present whenever ferromagnetic behavior was exhibited. In addition, Janusz, et al (111) and Johnston, Heikes and Sestrich (112) duplicated the sample preparation technique of Perakis but found no evidence of ferromagnetism down to liquid nitrogen temperature.

In 1958, a thorough investigation of the magnetic and crystallographic properties of the system was made by Goodenough and coworkers (113,114) and then essentially con-

firmed by Bronger, et al in 1964 (124) and by Bade, et al in 1965 (125). Their results show that, for values of  $x$  between zero and 0.3 in  $\text{Li}_x\text{Ni}_{1-x}\text{O}$ , the material is a random solid solution possessing a sodium chloride type structure (MnO magnetic cell). For  $0.3 < x < 0.5$  the material possesses a rhombohedral  $\alpha\text{-NaFeO}_2$  structure with a definite ferrimagnetism caused by ordering of  $\text{Li}^{+1}$  and  $\text{Ni}^{+3}$  on alternate 111 planes. The strongest ferrimagnetic effect is found for  $x \approx 0.38$  (Bronger) and corresponds quite well with the ordering parameters given by Goodenough (zero ordering for  $x=0.3$ , maximum order for  $x=0.5$ ) predicting maximum magnetization in the middle of the phase region. At  $x=0.5$  the ordered compound  $\text{LiNiO}_2$  is formed and for  $0.5 < x < 0.67$  the material is paramagnetic and possesses a monoclinic structure.

The Japanese literature seems to indicate a parallel development of the knowledge concerning the solid solution region of the  $\text{NiO-Li}_2\text{O}$  system but from a more chemical viewpoint. Takeuchi (25) obtained alloys containing up to 8 mole per cent lithium oxide at  $700^\circ\text{C}$  (kinetically limited) and made a very careful study of the flame spectroscopy methods for analyzing lithium. Iida and coworkers (126-129) investigated the kinetics of the solid state solution reaction for 4 weight per cent lithium (18 atomic per cent) and found that solution formation started at temperatures as low as  $300$  to  $500^\circ\text{C}$  and then reached a maximum solubility at  $800-$

1000°C because of the volatility of lithium oxide. These same authors later combined their chemical techniques with x-ray methods (115-117) in order to determine the variation of lattice constant with lithium content and then established the limiting solubility at 25-28 atomic per cent. Many other investigators (112-114, 118-123) have determined the lattice parameter variation with composition and these are shown as the volume of the chemical cell versus composition in Figure 8. The data of Goodenough and coworkers (113,114) covers the widest concentration range, is fairly linear and falls midway in the range.

The NiO-MgO system exhibits complete solid solubility (130-132) and has been shown by Hahn and Muan (133) to be an ideal solid solution following Vegard's law. It is interesting to note, however, that even though the  $\text{Li}^{+1}\text{-Mg}^{+2}$  cation size deviation is only 7.7 per cent as opposed to 17 per cent for  $\text{Li}^{+1}\text{-Ni}^{+2}$ , less than one per cent lithium oxide is found to be soluble in MgO. (139, 140, 142, 143) Inspection of the following ionization potentials for Li, Mg, and Ni,

	I	II	III
Li	5.4	75.6	122.4
Mg	7.6	15.0	80.1
Ni	7.6	18.2	35.2

shows the second ionization potential of lithium to be ap-

proximately the same as the third ionization potential of magnesium but much higher than the third ionization potential of nickel. If the charge neutrality condition is looked upon as an additional degree of freedom for the system, it might be proposed that the high solubility of lithium in nickel oxide and the low solubility in magnesium oxide are the expected results. In effect, this combination of small deviation of cation size in conjunction with ease of ionization of one of the component cations is the cause of the formation of the group of materials called "controlled valence" compounds. (4)

### C. The Ni-NiO Phase Equilibria

Various experimental observations have been made in the literature (47,50,53,58,88,110,144-149) that indicate the presence of metallic nickel in nickel oxide. Almost all of these studies report the use of very high surface area oxides (150-300 m<sup>2</sup>/g) prepared by thermal dehydration of Ni(OH)<sub>2</sub> at 200-300°C under a pressure of 10<sup>-6</sup> mm Hg as originally developed by Teichner and coworkers (144,145). These reports seem to be in conflict with studies of thermochemical equilibrium for the Ni-NiO system (133-138) as shown in Figure 9. Alternatively, investigations using lower surface area powders prepared at high temperatures in air (146) do not show the presence of metallic nickel, while

those prepared at high temperatures in vacuum (110) do show the presence of nickel, both observations being in agreement with simple thermochemical considerations.

Using a value of  $\Delta G^\circ = -46,500$  cal/mole NiO at 250°C (Figure 7),  $P_T = 10^{-6}$  mm Hg,  $P_{O_2} = 0.21 P_T$  (in atmospheres),  
 $\Delta G_{BULK} = \Delta G^\circ - \frac{RT}{2} \ln P_{O_2} = -35,000$  cal/mole NiO = -470 cal/gram NiO.

If a value of  $\gamma = 10^3$  erg/cm<sup>2</sup> is chosen for the surface energy of nickel oxide (150) and 225 m<sup>2</sup>/gram for the surface area, then

$$\Delta G_{SURFACE} = \frac{10^3 \frac{\text{erg}}{\text{cm}^2} \cdot 225 \frac{\text{m}^2}{\text{gram}} \cdot 10^4 \frac{\text{cm}^2}{\text{m}^2}}{4.185 \times 10^7 \frac{\text{erg}}{\text{cal}}} = 53.8 \text{ cal/gram NiO.}$$

Thus the surface energy effect cannot be neglected when considering very high surface area powders. A second possible explanation for the appearance of metallic nickel at low temperatures would be the presence of retrograde solubility as has been demonstrated for the PbS system (151), but no evidence of such behavior has been reported for any of the transition metal oxide systems.

The conditions of temperature and pressure under which the present pressure sintering investigation was carried out (approximately 1100°C at 0.1 micron Hg total pressure) would indicate that they fall close to the Ni-NiO phase boundary (Figure 9). The presence of metallic nickel

(1 to 2 per cent) as shown by metallographic inspection for the as pressed 99.999 per cent nickel oxide specimens indicates that they were on the nickel side of the boundary. However, under similar conditions, the lithium doped specimens did not show evidence of a two phase structure. An initial explanation of this behavior might be given by considering the variation of the activity of nickel oxide with lithium doping level. As lithium oxide is added, the mole fraction of nickel oxide and therefore its activity should decrease. If the activity of nickel oxide decreases, the equilibrium oxygen partial pressure for equilibrium between nickel and nickel oxide decreases, or the doped nickel oxide is stable at a lower oxygen pressure.

The difficulty with the above explanation lies in the realization that despite experimental variations in pressure and temperature around the "nominal" conditions, all of the pure 99.999 per cent nickel oxide specimens gave two phase structures, while even extremely small lithium additions (0.1 mole per cent) eliminated the presence of metallic nickel. The fairly large (28 to 30 mole per cent) solubility of lithium in nickel oxide would seem to predict either adherence to or a slightly positive deviation from Raoult's law for the nickel oxide solvent phase for small lithium additions (152). Thus, for an alloy with  $N_{NiO} = 0.999$  (0.1 per cent lithium) the activity,  $a_{NiO}$ ,

would be equal to or greater than 0.999. The resulting shift in the Ni-NiO phase boundary for  $\text{Ni}_{0.999}\text{Li}_{0.001}\text{O}$  would be small in comparison with the variation of experimental conditions and a two phase structure might still be expected for this alloy and possibly  $\text{Ni}_{0.995}\text{Li}_{0.005}\text{O}$  as well. The single phase structures obtained with pressure sintered sub-micron 99.9 per cent pure nickel oxide (Atomergic Cl435) eliminate the possibility of a kinetic effect related to the surface area (300 fold difference in the particle size between the two powders) and point to an effect related to sample purity.

The widening of the stable phase field for pure and doped non-stoichiometric binary semi-conductor compounds such as PbS, PbSe, and PbTe has been investigated by R.F. Brebrick (153,154). Brebrick extended the qualitative approach to imperfection chemistry developed by Kroger and Vink (66) into a quantitative theory through the application of a simple non-degenerate band type semiconductor model. The assumptions made during his theoretical development are:

1. The predominant point defects present in the two sublattices are vacancies,
2. Clustering of point defects is unimportant,
3. Each M or N vacancy is associated with an acceptor or donor level,

4. Non-degenerate statistics may be used, and
5. The phase coexisting with solid MN compound is one or the other of the pure elements.

The net electron or hole concentration,  $n-p$ , is used to express composition because experimental results are usually expressed in these terms rather than as mole fraction of either of the components. For an N rich, pure compound, the net relative hole concentration,  $n-p$ , is given as:

$$2RT \left[ \sinh^{-1} \frac{n-p}{2\sqrt{k_s}} + \sinh^{-1} \frac{n-p}{2n_i} \right] = \Delta G_{MN}^* + A$$

where

$n_i$  = intrinsic carrier concentration

$k_s$  = Schottky constant =  $[V_M] [V_N]$

$\Delta G_{MN}^*$  = Gibbs free energy change of formation of one mole of compound from the elements.

$A$  = Bond strength parameter.

This equation indicates that the magnitude of  $(n-p)$  will be larger (the stability range is wider) the larger the free energy of formation of the compound.

Although this analysis has been applied mainly to IV-VI semiconducting compounds, there is very good reason to believe that the approach is directly applicable to the transition metal monoxides (155). As a group, they tend to

favor singly or doubly ionized cation defects with no evidence of clustering. In particular, pure nickel oxide tends close to stoichiometry, has a eutectic system with almost pure nickel and vaporizes primarily by dissociation to the elements (135). Investigators that have adopted a band approach for pure nickel oxide variously give the band gap as 2 - 5 electron volts in width with the Fermi level 0.5-1 electron volt above the valence band (86,58,156,157). Comparison of the free energy of formation of each of the divalent transition metal oxides (Figure 7) with the experimentally determined maximum deviations from stoichiometry gives good qualitative agreement with Brebrick's analysis. Kroger (158) has recently used the same approach to explain the assymetry in the stable phase field for both divalent and trivalent transition metal oxides.

Brebrick (159) gives the chemical potential of the metal component, M, as:

$$\mu_M - \mu_M^i = RT \sinh^{-1} \left[ \frac{(n-p) - (N_D - N_A)}{2\sqrt{k_S}} \right] + (E_f - E_f^i)$$

where  $N_D, N_A$  = concentration of ionized donors or acceptors

$\mu^i, E_f^i$  = chemical potential and Fermi level of intrinsic material

Whether a hopping model (where each  $\text{Li}^{+1}$  ion produces a  $\text{Ni}^{+3}$  mobile hole) or an exhaustion region extrinsic band model is chosen makes no difference in the applicability of the previous analysis to the present work. For a pure

p-type semiconductor such as nickel oxide,  $n \approx N_D \approx 0$  and  $p \approx N_A$ . The first term in the above equation therefore goes to zero, and the result is simply

$$\mu_M - \mu_M^i = E_f - E_f^i.$$

The reported drop of Fermi level to 0.2 - 0.3 electron volts with even the smallest lithium doping concentrations (86) thus causes a very sharp drop in the chemical potential of Ni in NiO, decreases the activity precipitously and rapidly widens the stable phase field for nickel oxide. This results in a large negative deviation from Raoult's law (as opposed to a slight positive deviation proposed initially) and gives a good qualitative explanation of the present experimental observations.

#### D. Chemical Analysis

The iodometric titration method (Bunsen-Rupp Technique) was first used (38,141,160-163) in order to measure the quantity of "excess oxygen" or "oxidizing power" of chromium and manganese oxides. Verwey and coworkers (3,4) used the method to show that "within certain limits of Li content, the  $Ni^{+3}$  content is equivalent to the amount of Li added to the system." In 1961, Deren (164), and in 1962, Bielanski and coworkers (165) showed approximate equivalence of  $Ni^{+3}$  and  $Li^{+1}$  up to 0.8 atomic per cent lithium and er-

ratio results between 1.4 and 2.5 atomic per cent lithium. In 1965, Hayashi and Iida (116-117) showed approximate equivalence over the range 0 - 28 atomic per cent lithium. However, in 1966, Gravelle and coworkers (53,166), using a modified method similar to that of Charman (59) (combined HCl and KI solutions in same flask), found large discrepancies between  $\text{Li}^{+1}$  and  $\text{Ni}^{+3}$  for the range 2 - 10 atomic per cent lithium. Many of the above investigators have shown that partial dissolution of the sample or vacuum baking of the sample prior to analysis indicates a non-homogeneous distribution of  $\text{Ni}^{+3}$ . These results have been attributed to either a non-homogeneity in the lithium distribution, or to a tendency for the "excess oxygen" to remain at the powder surface. More accurate methods for the chemical analysis of surface layers, such as surface reduction by aqueous hydrazine (167), indicate that the amount of surface excess oxygen decreases monotonically with increasing calcining temperature and with increasing lithium concentration.

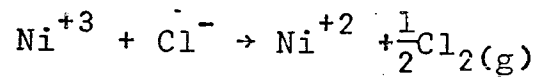
The iodometric titration method used for this work is similar to the improved technique developed by Panthony and Siddiqi (168) and has been described earlier. The major advantages of the present arrangement (Figure 3) over previous techniques is that the HCl feed system allows the introduction of HCl after the system has been purged of air,

and permits continuous gas flow throughout the system after the gas inlet tube in the reaction flask has been clogged by the dried residue.

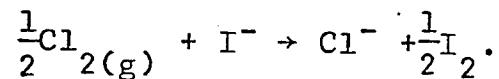
The combined results of  $\text{Ni}^{+3}$  iodometric and  $\text{Li}^{+1}$  photometric analyses are given in Table 4. Inspection of the table shows a consistently larger difference between  $\text{Li}^{+1}$  and  $\text{Ni}^{+3}$  (in both the starting powder and the pressure sintered samples) for the unwashed 5% Li alloy than for any of the other samples. The pH of this powder was found to be basic, and therefore all further analyses and pressure sintering work was performed on washed powders. This indication of incomplete solution of lithium in nickel oxide is the most likely explanation of previously reported discrepancies between  $\text{Li}^{+1}$  and  $\text{Ni}^{+3}$ .

A comparison of the lithium and  $\text{Ni}^{+3}$  content for the starting alloy powders and the pressure sintered samples indicates that there was little or no lithium loss during vacuum pressure sintering. This is quite surprising since many reports of lithium loss during sintering in air exist in the literature (4,98). These reports of lithium loss might be related to small amounts of second phase material, which would not be detectable by standard x-ray techniques, but which were removed by the extended washing process of the present investigation.

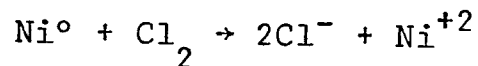
The dissolution of nickel oxide powder is a result of the reaction



and the formation of free iodine is a result of the displacive reaction



The presence of metallic nickel in the reaction flask would also cause the reaction



and therefore the quantity of  $\text{Cl}_2(\text{g})$  entering the KI solution will be a function of the difference in  $\text{Ni}^{+3}$  and free nickel. Thus, in addition to showing the equivalence of  $\text{Li}^{+1}$  and  $\text{Ni}^{+3}$  concentrations, the present results indicate the lack of detectable metallic nickel.

## E. Sintering of Pure and Doped Nickel Oxide

The first extensive investigation of the sintering behavior of pure and doped nickel oxide was performed by Iida (169) and Iida and Ozaki (170). They observed that the sintering rate of nickel oxide was greater in vacuum than in air. Because an increased vacuum level should decrease the number of cation vacancies and hence decrease the sintering rate, these authors concluded that densification is not predominantly affected by a lattice defect mechanism. However Blackman (171) observed the sintering rate of nickel oxide to be greater in oxygen than in nitrogen and in 1965, Brown (172) noted that normal grain growth was always observed during the sintering of nickel oxide. Brown proposed that the departure from stoichiometry and hence the occurrence of lattice vacancies make the movement of ions so facile that it is impossible for either impurities or pores to build up on the grain boundaries and thus prevent discontinuous grain growth. In 1966, Wang (173) investigated the low temperature (549 - 993°K) sintering behavior of nickel oxide by monitoring resistivity versus sintering time. Through the use of Coble's intermediate stage sintering model (174) he identified the diffusion of  $\text{Ni}^{+2}$  to be the rate-determining step during sintering. On

the other hand, initial sintering studies with nickel oxide spheres (175) indicate the presence of a higher activation energy (73.3 k cal/mole) than either the activation energy for self-diffusion of  $\text{Ni}^{+2}$  cations (45.6 k cal/mole) given by Choi and Moore (176) or the activation for oxygen anion self-diffusion (57.5 k cal/mole) given by O'Keefe and Moore (177). In addition, the observation of high creep rates in nickel oxide films (178) at temperatures as low as 850°C (well below  $0.5 T_M$  where diffusion controlled creep is normally expected to become operative) indicates the possibility of a plastic flow contribution to sintering behavior. It is extremely likely that a multi-mechanism approach such as that recently proposed by Johnson (179) will be more fruitful in describing the early stage sintering behavior of this type of material.

Optimum final relative densities obtained by normal sintering methods are 89% (Iida [169]), 93% (Harrison [180]), and 95% (Herbst and Friedberg, [181-182]) while the literature abounds with reports of poorer density materials. Pressure sintering (20) makes practical the study of the more controllable later-intermediate and final stages of sintering, and affords the possibility of both increased density and increased strength through finer final grain size. Harrison (183) reported a relative density of 96.4% for hot pressed nickel oxide, and Spriggs and coworkers

(184,185) reported the achievement of nearly theoretical density in very short times.

The relative final density of pure nickel oxide and of each of the alloys used in this investigation are shown in Figure 10 as a function of lithium content. Transmission electron micrographs of representative starting powders are presented in Figure 11, and a carbon-chrome replica of a fractured surface of each of the same pressure sintered samples is presented in Figure 12. The range of final grain sizes is given in Table 6. It is interesting to note that while there is little or no particle growth during the solid state alloying treatment, there is a definite change in the surface texture and particle shape. The surface changes from a rough hackled texture for pure nickel oxide to an increasingly smooth appearance with increasing lithium content, while at the same time the shape appears to shift from a somewhat rounded geometry to a definitely angular structure. A similar comparison of the fractographs indicates the fracture mode to shift from predominantly transgranular for pure nickel oxide, to predominantly intergranular with increased lithium content; at the same time there is a definite increase in the final grain size (Figure 12 and Table 6).

A consistent qualitative explanation of all of the observed results may be gained by interpretation of the sintering behavior with respect to the lattice defect struc-

ture of the material. As previously described, nickel oxide is a p-type, oxygen excess (cation vacancy) compound that has a strong tendency to chemisorb oxygen at a free surface. Deren and coworkers (57) have found that the quantity of oxygen which can be removed by desorption increases with increasing lithium content and Keier (186) has found the  $O^{18}$  isotopic exchange rate to increase rapidly with lithium additions. Keier proposed that lithium additions decrease the chemisorptive tendency of nickel oxide, thus making possible the formation of anion vacancies at the surface. These vacancies increase the isotopic exchange rate at the surface because they permit anion bulk diffusion. However, for a simple defect model it is illogical that electroneutrality could be maintained by the simultaneous addition of lithium ( $M^{+1}$ ) and the formation of an anion vacancy,  $V_O$ , which would have an effective positive charge. Hoch and Szwarc (187 - 188) have proposed that the defect responsible for oxygen self-diffusion is a coupled anion vacancy-electron hole complex. In their model, although the anion vacancy concentration is constant, the "mobility" of the complex is increased by lithium additions because of the corresponding increase in the concentration of electron holes.

With respect to the present investigation, the addition of small quantities of lithium to the nickel oxide

lattice fills the available cation vacancies in the pure material and thus decreases the sinterability by removal of a possible diffusion mechanism (Figure 10). The conditions under which pressure sintering was carried out (Figure 9) were such as to place the material near the Ni/NiO phase boundary. Under these conditions the pressure and temperature dependent equilibrium defect concentration relation (Schottky defects)

$$[V_{Ni}][V_O] = K(T,P)$$

would cause the concentration of anion vacancies to be maximized. Thus, whether lithium additions enhance anion diffusion by reducing the chemisorption at the surface or by increasing the "mobility" of a complex defect, the result of increasing the lithium content should be an increase of the lattice diffusion contribution to the sintering rate. The increase of relative density with substantial lithium additions (Figure 10), the change in particle texture and shape (Figure 11) and the increasing grain size (Figure 12 and Table 6) may all be interpreted in terms of this approach. The changing fracture mode may be attributed to the loss of high chemisorption tendency (strong free surface bonds) with lithium additions.

A similar diffusion enhancement mechanism to that described above has been proposed by Rovner (189) to ex-

plain enhanced oxygen diffusion in magnesium oxide single crystals, and may be applicable to the interpretation of enhanced grain boundary anion diffusion in  $Al_2O_3$  (190), MgO (191) and CoO (192).

#### F. Electron Microprobe Analysis

Microprobe analysis was performed on both pure and doped nickel oxide specimens. The samples were mounted without heating by using a low-level exothermally setting potting compound (\*). They were then slowly ground on number 240,320,400 and 600 grit silicon carbide papers (under kerosene in order to prevent surface heating), lapped on a short nap felt cloth with 15 micron and 6 micron diamond abrasive and then polished on a silk cloth with 1/4 micron (maximum diameter) diamond abrasive (†) without pressure, for three hours. This procedure produced a good surface for microprobe work and held grain pullout to a minimum. The specimen was then ultrasonically cleaned with acetone and immediately placed in the microprobe. The probe was always focused adjacent to the area of interest and then shifted for the scan sequence in order to prevent prior contamination of the area analyzed. The instrument used

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(\*) Klearmount, Vernon-Benshoff Co., Inc., Albany, New York

(†) 1/4 Micron Geonite Diamond Compound, Geoscience Inst., Mount Vernon, New York

was an ARL Co. Model EMX-SM (Electron Microprobe X-ray Scanning Microscope) with a 0.2 micron beam size, and all photographs were taken at the slowest electronic scan rate (5 sec/cm).

Figure 13A shows the area scanned for the 99.999 per cent nickel oxide specimen. The trace made by the beam clearly indicates the beam location. Figure 13B shows the same area after etching for ten minutes in boiling concentrated HCl. It is evident that the beam passed through a large pore and two grain boundaries. The pore may be used as the reference point for the microprobe photographs. Figures 14, 15, and 16 show both area and line scan displays for specimen current, secondary electron and back-scattered electron images. The secondary electrons are low energy electrons (less than 200 ev) and therefore respond to surface conditions and topography. The lack of response shown by the secondary electron scans (Figure 15) thus indicates the absence of a topography effect, and therefore, the positive response demonstrated in the specimen current scans (Figure 14) may be interpreted in terms of enhanced grain boundary conduction. The peak height at the grain boundary (Figure 14B) is only 4 per cent above the baseline current. A similar analysis was performed on an 8.23 atomic per cent lithium sample. Figure 17 shows both a specimen-current area and line scan display for this alloy.

The specimen-current peak at the grain boundary is only 1-1/2 per cent above the base line current.

A Ni-K $\alpha$  X-ray scan of the 8.23 atomic per cent lithium sample is shown in Figure 18A. For comparison, Bickelhaupt's (140) photograph of a Mg-K $\alpha$  scan for a 5 atomic per cent lithium doped MgO specimen is shown in Figure 18B. Because of its low atomic mass, lithium cannot be directly detected with the microprobe, and therefore the absence of nickel (or magnesium in Bickelhaupt's work) must be used in order to indicate a variation in the lithium level. Although no quantitative data were taken, in comparison to the work performed with lithium in magnesium oxide, there appears to be no significant segregation of lithium in nickel oxide.

The possible effects of grain boundary or pore conduction in polycrystalline materials have long been a troublesome barrier to the use of these materials for reliable electronic applications. For example, Goodman (193) has found an increase in resistivity of four orders of magnitude in barium titanate at its ferroelectric Curie temperature. Hutson (17) has reviewed the possible idiosyncracies of polycrystalline materials in general, and Morin (194) has suggested the possible presence of grain boundary conduction in nickel oxide caused by higher concentrations of excess oxygen at the grain boundary than within the bulk

material. This excess oxygen causes a higher concentration of holes and hence a higher p-type conductivity. Similar results have also been reported by Nachman and coworkers (195). However, both of these investigations were performed on specimens with relative densities only 75 to 87 per cent of theoretical density and would therefore be very prone to such effects. Boseman and Crevecoeur (196) report an order of magnitude difference between dc and ac resistivities for an  $8.8 \times 10^{-2}$  atomic per cent lithium alloy, 93 per cent dense, cooled in nitrogen, and identical dc and ac resistivities for the same alloy cooled in air. Boseman and Crevecoeur suggested that this was due to a grain boundary effect, but recent work by Kabashima and Kawakubo (197) shows similar discrepancies between ac and dc measurements in single crystals with similar doping concentrations and similar measurement temperature ranges. In addition to the above, Thornton (198) has reported grain boundary conduction in nickel oxide bicrystals to be caused by the presence of a discontinuous metallic nickel phase at the boundary. The preparation techniques used in this work are questionable.

Microprobe analysis of the grain boundary diffusion of  $\text{Ni}^{+2}$  in  $\text{MgO}$  (199), oxygen self-diffusion in polycrystalline alumina (200), and sintering studies in alumina (201) show that the grain boundary width in oxide materials is of the order of 1 micron rather than 10 to 100 angstroms

as would be expected in most metals. Therefore, the present microprobe results on both pure and doped nickel oxide specimens, using very slow scan rates (5 sec/cm) and a small beam size (0.2 microns), give good indication that significant grain boundary effects are absent in the materials used in this investigation. This might also be expected from the high density and high purity of these samples in comparison with the polycrystalline materials used in previous investigations.

#### G. The Elastic Moduli and Electrical Conductivity

Various attempts have been made in the literature to relate the electrical, magnetic and elastic properties of pure and substituted transition metal oxides. Heikes and Johnston (6), who observed a higher activation energy for electrical conduction above the Néel temperature than at low temperatures for a variety of sintered transition metal oxide alloys, related the major portion of the activation energy to the localized lattice distortion which surrounds a positive hole as it jumps, or "hops", through the lattice. Since the magnitude of the lattice distortion is related to the elastic properties of a material, and because of experimental observations (202) which indicated a large increase in Young's modulus for NiO and CoO as temperature is increased through the Néel point, Heikes and Johnston argued

that the activation energy should likewise increase. Similarly, they explained the observed decrease in activation energy with increased lithium additions as caused by a decrease in the elastic constants with increased impurity concentration.

Toyozawa (11,12) proposed that, in polar materials, there should be an interaction between electrons possessing high effective mass and the acoustic (†) vibration modes of the lattice (as opposed to the simple "polaron" models which consider only optical mode interactions). Toyozawa showed that there is a sharp transition from a "band" state ( $M^* \approx M_0$ ) to a "localized" state ( $M^* > 10^4 M_0$ ) when the electron-acoustic phonon coupling constant reaches a critical value,  $g = g_c \approx 1$ . The coupling constant may be expressed as

$$g = \frac{1}{6} \frac{E_d^2 M^*}{\hbar^2 C a}$$

where  $E_d$  = Bardeen-Shockley deformation potential constant  
 $\approx 2$  ev.

$C$  = effective elastic constant

$a$  = nearest neighbor distance.

Adler (14) has recently given a more usable equivalent

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(†) The acoustic mode is defined as both the cation and anion moving in phase or as the center of mass of the two ions moving with them, while the optical mode is defined as both the cation and anion moving out of phase or as the center of mass remaining stationary.

expression as

$$\left[ \frac{E_d^2}{(Mv^2) \Delta} \right] \approx 1$$

where M = mass per unit cell

v = velocity of sound

$\Delta$  = "band width".

Koide (122) investigated the electrical conductivity of  $\text{Li}_x\text{Ni}_{(1-x)}\text{O}$  single crystals and found a lower activation energy above the Néel temperature than at lower temperatures. This experimental work was interpreted in terms of Toyozawa's interaction theory, and the "band width",  $\Delta$ , was equivalent to the energy difference,  $\epsilon_m = E_a - E_s$ , between the self trapped state ( $E_s$ ) and the activated state ( $E_a$ ). Koide gives the expression for resistivity as

$$\rho = \frac{k a B}{T e^2 v_l x} \exp \left[ -\frac{\epsilon_c}{kT} \right] \exp \left[ \frac{\epsilon_m}{kT} \right]$$

where k is the Boltzmann constant, a is the lattice constant, T is the absolute temperature, e is the electronic charge,  $v_l$  is the lattice vibrational frequency, x is the mole fraction of impurity, and B is a constant. The  $\epsilon_c$  term is associated with the ionization of holes and is important at low impurity concentrations, while the  $\epsilon_m$  term is associated with an "activated" mobility. The lower activation energy observed by Koide above the Néel temperature is consistent with Toyozawa's model and the experi-

mental increase of the modulus at the Néel temperature.

With reference to Adler's expression for Toyozawa's model, three observations may be made:

- (1) If there is a change of modulus at the Néel temperature then a change in the slope of resistivity versus temperature curve should occur at the same temperature. This change should occur at a different temperature for each composition.
- (2) If the modulus increases at the Néel temperature then the activation energy should decrease above the Neel temperature ( $E_{LT} > E_{HT}$ ).
- (3) If the low temperature modulus increases with increased impurity content then the difference between the low temperature and high temperature activation energies should decrease (the modulus above the Néel temperature is normally expected to decrease with temperature for a paramagnetic material and is therefore a poor indicator).

The Néel temperature of nickel oxide was first measured by Foex (203) using dilatometric methods and was found to be 525°K. Many other measurement methods have been used, and the results are given in Table 7. The best value for the Néel temperature, obtained from more recent data in the table, appears to be 523°K. Because of the relatively broad susceptibility peak (50) as opposed to the sharp modulus change (202), and because of the interest in the vari-

ation of the low temperature modulus with lithium concentration, measurements for this investigation were performed using the modulus technique.

The difficulties encountered in measuring elastic moduli of small samples are outlined in Appendix 2. Careful investigation was made of the accuracy and experimental difficulties associated with each of the available methods before a specific method was adopted. The Forster free vibration method was ruled out (230) because of the need for a long specimen, while the "pulse-echo", "Phase Comparison" and "Pulse Superposition" methods were eliminated (231) due to the inaccuracy of velocity measurements associated with small samples. Although the "Pulse Transmission" and "Sphere Resonance" methods were found to give good accuracy for small specimens (232), they were similarly eliminated because of the difficulties associated with measurements at elevated temperatures. The composite oscillator method was adopted because of its applicability to small specimens, lack of complicated electronic equipment, and adaptability for high temperature measurements. However, the room temperature Young's modulus measurements were standardized against "Pulse Transmission" and "Sphere Resonance" measurements for both the pure nickel oxide and the highest lithium alloy investigated (\*). A description of the mathematical

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(\*) These measurements were made by Messrs. M. Notis and J. Snyder at the Lamont Geological Observatory of Columbia University with the kind permission of Dr. O.L. Anderson.

basis for the composite oscillator method and a tabulation of the data are presented in Appendix 3. A description of the experimental and associated calculation procedures for the "Sphere Resonance" and "Pulse Transmission" methods is given in Appendix 2. The experimental "Sphere Resonance" data for pure nickel oxide at room temperature are given in Table 8, and all of the room temperature modulus results for each of the methods are given in Table 9.

Observations made from the data given in Table 9 might be summarized as:

- (1) The shear velocity of the 8.23 per cent lithium alloy is 50 per cent higher than that for pure nickel oxide (Pulse Transmission data) while the longitudinal velocities are nearly identical.
- (2) The Young's modulus values from Sphere Resonance and composite oscillator methods agree within 0.2 per cent, and Pulse Transmission and composite oscillator within 22 per cent, for pure nickel oxide. Pulse Transmission and composite oscillator measurements agree within 10 per cent for the 8.23 per cent lithium alloy.
- (3) The value of Poisson's ratio, 0.443 from Pulse Transmission, and 0.416 from Sphere Resonance, for pure nickel oxide is extremely high. The value of Poisson's ratio for the 8.23 per cent lithium alloy is 0.35, and repre-

sents a very substantial decrease from the value for pure nickel oxide.

The values obtained for the room temperature moduli of nickel oxide may be compared with the pre-existing experimental work in the literature and with theoretically derived moduli. Street and Lewis (202) give the room temperature value of Young's modulus for 68 per cent dense nickel oxide (240) as  $5.1 \times 10^{11}$  dyne/cm<sup>2</sup>, Belov (217) gives the Young's modulus for unidentified nickel oxide as  $3.24 \times 10^{11}$  dyne/cm<sup>2</sup> ( $3.3 \times 10^3$  kg/mm<sup>2</sup> in the original paper), and Slack (241) has given the value of  $C_{11}$  as  $10.0 \times 10^{11}$  dyne/cm<sup>2</sup>. Wakabayashi and coworkers (242) have measured the effect of pressure on the lattice parameter of NiO and have expressed this as:

$$\frac{\Delta V}{V_0} = -5.4 \times 10^{-7} P + 0.6 \times 10^{-12} P^2$$

where P is the applied pressure in bars. The bulk compressibility,  $B_T$ , may be expressed as

$$B_T \equiv - \frac{1}{V} \left( \frac{\partial V}{\partial P} \right)_T \approx - \frac{1}{V} \left( \frac{\Delta V}{\Delta P} \right)_T = - \frac{\Delta V}{V} \left( \frac{1}{P - P_0} \right) \bigg|_{\substack{V=V_0 \\ P_0=0}} = - \frac{\Delta V}{V_0} \left( \frac{1}{P} \right)$$

and since the bulk modulus is just the inverse of the compressibility,

$$K \Big|_{P=1} = - \frac{V_0}{\Delta V} (P) = - \left[ \frac{1}{-5.4 \times 10^{-7} (1) + 0.6 \times 10^{-12} (1)^2} \right] \quad (1)$$

$$= 1.85 \times 10^6 \text{ bars} \times \frac{10^6 \text{ dyne/cm}^2}{\text{bar}} = 18.5 \times 10^{11} \text{ dyne/cm}^2.$$

The mean sound velocity may be derived from the Debye temperature (243) using the relation

$$v_m = \frac{k}{h} \left[ \frac{3PN_A \rho}{4\pi M} \right]^{-1/3} \theta_D$$

where  $k = 1.38 \times 10^{-16} \text{ erg/}^\circ\text{K}$

$h = 6.6 \times 10^{-27} \text{ erg}\cdot\text{sec}$

$P = \text{Number of atoms per molecule} = 2$

$N_A = 6.023 \times 10^{23} \text{ molecules/gram atomic weight}$

$\rho = \text{density} = 6.806 \text{ g/cm}^3$

$M = \text{molecular weight} = 74.71.$

Seltz and coworkers (244) give  $\theta_D = 404^\circ\text{K}$  and Wenner (245) gives  $\theta_D = 415^\circ\text{K}$ . Using the average value of  $410^\circ\text{K}$ , the value of  $v_m$  is  $2.9 \times 10^5 \text{ cm/sec}$ , and the Debye frequency,  $v_D = \theta_D \frac{k}{h}$ , is  $8.6 \times 10^{12} / \text{sec}$ .

If the infrared reflection spectra for a diatomic substance is known, the bulk modulus can be determined (reference 243 equation 10) from the Szigeti (246) relation:

$$K = \frac{4\pi^2 C^2 \pi}{6R_0 \lambda_0^2} \left( \frac{\epsilon_0 + 2}{\epsilon_\infty + 2} \right)$$

where  $C$  = speed of light =  $3 \times 10^{10}$  cm/sec

$R_o$  = interatomic spacing =  $\frac{a_o}{2} = 2.09 \text{ \AA} = 2.09 \times 10^{-8}$  cm

$\bar{m}$  = effective mass per ion pair =

$$\left[ \frac{M_O M_{Ni}}{M_O + M_{Ni}} \right] \frac{1}{N_A} = \frac{(16)(58.71)}{(74.71)(6.023 \times 10^{23})} = 20.8 \times 10^{-24} \text{ g}$$

$\epsilon_o$  = dielectric constant

$\epsilon_\infty$  = square of the index of refraction ( $n$ )

$\lambda_o$  = "Reststrahlen" wavelength.

Marshall and coworkers (247) give these last three values

as  $\epsilon_o = 11.9$ ,  $\epsilon_\infty = 4.75$  and  $\lambda_o = 24.5 \mu$  ( $v_t = 408 \text{ cm}^{-1}$ ,  $\lambda_o =$

$\frac{10^4}{v_t}$ ). The above equation then gives a value of  $K = 20.2 \times 10^{11}$

dyne/cm<sup>2</sup>.

The mean sound velocity,  $v_m$ , may be related to (243)

Poisson's ratio and the bulk modulus according to the expression

$$v_m = \left[ \frac{3}{\left[ \frac{1+\sigma}{3(1-\sigma)} \right]^{3/2} + 2 \left[ \frac{2(1+\sigma)}{3(1-\sigma)} \right]^{3/2}} \right]^{1/3} \cdot \left[ \frac{K}{\rho} \right]^{1/2}$$

The experimental and derived values of  $v_m$  and  $K$  are sum-

marized in Table 10. Where necessary, the conversion from

$v_m$  to  $K$  was performed using the Poisson's ratio of  $\sigma = 0.416$

obtained from the Sphere Resonance method. The agreement of

these values is excellent, except for the Debye value.

Young's modulus as a function of temperature for pure nickel oxide is shown in Figure 25. The two curves represent measurements made with two different sets of crystals, 92.5 kc and 118.5 kc. The specimen matched the 92.5 kc crystals at room temperature and the 118.5 kc crystals at 245°C. The maximum deviation of  $f_{s(o)}$  and  $f_{s(f)}$  (equation A3.4 and equation A3.3) for the 118.5 kc crystal measurements occurred at 250.5°C and was 0.57 per cent. Although the effect of sample and crystal matching is pronounced for the high temperature modulus, the low temperature modulus values agree very well and the curves overlap in the region of the anomalous modulus increase. Below the anomaly, the slow increase in modulus is caused by a decrease in spin ordering, while above the anomaly, the decreasing modulus is caused by the normal thermal decrease found in paramagnetic materials. The Néel temperature was therefore defined as the point of maximum slope in the modulus curve. This choice of Néel temperature was found to be independent of crystal-sample frequency matching for both pure nickel oxide and all alloy compositions measured with different sets of crystals. The high and low temperature modulus measurements obtained for pure nickel oxide using the 118.5 kc crystals, and the low temperature moduli for the alloy specimens represent good modulus values because of good crystal-sample matching. The high temperature modulus values obtained for the alloy com-

positions should not be taken as being representative of the absolute modulus because of poor matching of specimen and crystals in that region.

Figure (26) shows the effect of using equation (A3.3) as an approximation of equation (A3.2) for pure nickel oxide measured with 118.5 kc crystals (i.e. ignoring the  $\tan^2$  term). There is a slight decrease of the low temperature modulus and an increase of the high temperature modulus, but again there is no change of Néel temperature with either choice of solution. Table 11 gives the appropriate data for the same specimen and indicates the value of the modulus obtained at room temperature and the Néel point for each solution method. Although equation (A3.2) provides a slight correction to the modulus value for reasonable deviations from matched conditions, the original starting assumptions (which were made in order to obtain an analytical expression) produced an incomplete solution. Thus, as the  $\tan^2$  term approaches 1,  $1 - \tan^2$  approaches zero and the value of  $f_s$  obtained from equation (A3.2) increases rapidly. For this reason and in order to be consistent with other published experimental work using this method, the  $\tan^2$  term was ignored.

The explanation of the anomalous modulus increase at the Néel temperature has been the source of much argument. Street and Lewis (202) originally proposed that the modulus effect was caused by changes in spin orientation, but later

(248) these same authors ascribed the anomaly to domain motion. Fine (249,250) measured Young's modulus and internal friction of CoO and explained his results in terms of domain changes related to crystal distortion. It seems logical however that the Néel temperature represents the point at which critical fluctuations in the spin system are reached, causing an interaction between acoustic lattice vibrations and the spin system. This type of interaction qualitatively accounts for the modulus change and the sharp increase in sound attenuation at the Néel point. Slack (251) observed that stresses of approximately  $10^5$  to  $10^6$  dyne/cm<sup>2</sup> were required to cause domain wall motion in nickel oxide single crystals. Yevtushchenko and Levitin (252) measured the moduli of MnO, CoO, and Cr<sub>2</sub>O<sub>3</sub> under dynamic stress conditions of  $10^4$  dyne/cm<sup>2</sup> or less, and consequently concluded that the anomaly is attributable to either the rotation of magnetic moments within a domain or to spin rotation. Belov (253) and coworkers came to similar conclusions for NiO.

Difficulties also exist as to the correspondence of the Néel temperature and the observed crystallographic distortion. A slight rhombohedral distortion ( $a_0 = 2.9518\text{\AA}$ ,  $\alpha = 60^\circ 4.2'$  at 18°C) below the Néel temperature was first observed by Rooksby (254,255), and the correspondence of the Néel temperature and lattice distortion was observed in CoO and Cr<sub>2</sub>O<sub>3</sub> by Greenwald and Smart (256). General agreement

with these observations was noted by Slack (251) in 1960. However, thermal expansion measurements made by Gillam and Holden (257) indicate no observable distortion until 90°C below the Néel temperature. Vernon and Lovell (258) have explained anomalies in resistivity measurements on nickel oxide single crystals as being caused by the non-correspondence of the Néel temperature and the onset of distortion. The most recent evidence (259) based on high temperature observation of domain structure in annealed nickel oxide crystals indicates correspondence of the magnetic and crystallographic transformations.

Young's modulus versus temperature data for pure nickel oxide and for five lithium alloys ranging from 0.12 to 8.23 atomic per cent lithium are presented in Figures 27 and 28. The relative acoustic loss corresponding to each of these specimens is given in Figure 29. Young's modulus versus temperature for a nominal  $\text{Li}_{0.01}\text{Mg}_{0.115}\text{Ni}_{0.875}\text{O}$  alloy is presented in Figure 30. Comparison of Figures 27, 28 and 30 demonstrates the excellent repeatability of the measurement method. Inspection of Figure 27 or 28 shows a definite decrease in Néel temperature with increased lithium content and a fairly large increase of low temperature modulus with increased lithium content. Comparison of Figures 27 or 28 and Figure 29 shows that the maximum in each acoustic loss curve corresponds very closely to the anomalous modulus in-

crease. The Néel temperature for each of these alloys, obtained from the modulus curves, is plotted in Figure 31. A similar curve can be obtained from the acoustic loss.

Shimomura and Tsubokawa (213) observed that the temperature of the anomaly in the specific heat of nickel oxide-copper oxide alloys decreased with increasing copper content. Perakis (107), Bielanski (260), and Mehandjeev (121) and coworkers have all investigated the magnetic susceptibility of powdered lithium-nickel oxide alloys as a function of temperature. The susceptibility curves all show a broad maximum and, although there is a general decrease in Néel temperature with lithium content, the results indicate very erratic behavior. On the other hand, Richardson and Milledge (207) indicate a very large decrease of Néel temperature with decreasing particle size for pure colloidal nickel oxide. They attribute this behavior to a decrease in the number of spin-opposed nearest neighbors caused by the influence of increased amounts of excess oxygen as the surface area is increased. Akiyama and coworkers (261,262) report a general decrease in Néel temperature with increased lithium content but give neither composition nor  $T_N$  for any of the alloys. No other reports on the effect of impurity additions on the Néel temperature could be found.

The linear relation between Néel temperature and lithium content observed on bulk material in this investigation

can be explained in terms of a localized electron approach to antiferromagnetism. Van Vleck (263) has shown that the Néel temperature, for antiferromagnetic compounds having a sodium chloride type structure and spin alignment such as that possessed by MnO or NiO (264), may be expressed as

$$T_N = \frac{1}{4} \alpha C_M$$

where  $C_M$  = Curie constant per gram·mole =  $N\mu^2/3k$

$\mu$  = absolute value of the magnetic moment =

$$\mu_B g \sqrt{S(S+1)} \quad (\text{reference 265})$$

$g$  = Landé factor = 2 for pure spin magnetic moments  
(reference 265)

$S$  = Spin angular momentum (in Bohr Magnetons) = 1  
(reference 265)

$\mu_B$  = Bohr Magnetron =  $9.2733 \times 10^{-21}$  ergs/gauss.

The proportionality factor,  $\alpha$ , is given by

$$\alpha = \frac{-2[Z][A_{EX}]}{N\mu_B^2 g^2}$$

where  $Z$  = number of nearest neighbors with opposite spin

$A_{EX}$  = "Exchange Integral."

For pure nickel oxide, each  $Ni^{+2}$  ion has six nearest neighbors of like spin and six of opposite spin so that  $Z = 6$ .

If one of these thirteen  $Ni^{+2}$  ions is replaced by a  $Li^{+1}$ , a

second  $\text{Ni}^{+2}$  ion changes valence to  $\text{Ni}^{+3}$  in order to maintain charge neutrality and, then  $Z = 5$ . For this situation the lithium content would be  $(1/13) \times 100 = 7.7\%$ , or

$$\frac{\Delta Z}{\Delta(\% \text{Li})} = \frac{6-5}{0-7.7} = -0.13$$

If a divalent element such as Mg were added the change of nearest neighbors would be only one-half of that for lithium since no  $\text{Ni}^{+3}$  would be produced. Thus if  $Z$  is a simple monotonic function of impurity concentration (as should be the case for a random solid solution) and if the magnitude of the "exchange integral" is constant (as should be the case for a localized electron model), the Néel temperature should be a simple decreasing linear function of impurity content.

Using the values given above,  $C_M$  for nickel oxide is found to be equal to 1, and if  $Z = 6$  and the Néel temperature of nickel oxide is set at  $523^\circ\text{K}$  then the "exchange integral" is found to be

$$(A_{\text{EX}})_{\text{NiO}} = -3.6 \times 10^{-14} \text{ ergs.}$$

This agrees fairly well with a theoretically derived value of  $1.17 \times 10^{-14}$  ergs given by Nesbet (266). If the experimentally determined value of  $C_M = 3.1$  obtained by Perakis (50) is used, then the value of the "exchange integral" would be  $-1.16 \times 10^{-14}$  ergs. Although the agreement is excellent, it may be somewhat fortuitous because of the simple

cubic lattice used by Nesbet. If

$$Z = Z_{\text{NiO}} + \% \text{Li} \frac{\Delta Z}{\Delta(\% \text{Li})} = 6 - 0.13 (\% \text{Li})$$

then for a 10% lithium alloy  $Z = 4.7$ ,

$$(T_N)_{\text{THEORETICAL}} = \frac{-(Z)(A_{\text{EX}})}{2N\mu_B^2 g^2} C = 409^\circ \text{K}$$

or  $\Delta T_N / \Delta(\% \text{Li}) = \frac{523-409}{0-10} = -11.4^\circ \text{K}/(\% \text{Li})$ . This compares very well with the observed value of  $-9.1^\circ \text{K}/(\% \text{Li})$  obtained from Figure 31. A similar calculation for Mg additions would give

$$\Delta T_N / \Delta (\% \text{Mg}) = -5.7^\circ \text{K}/(\% \text{Mg}).$$

If the localized approach is correct then the total change in Néel temperature should just be the arithmetic sum of all the  $\Delta T$ 's from each impurity addition. This may be expressed, for lithium and magnesium additions, as

$$\Delta T_N = \Delta T_{N(\text{Li})} + \Delta T_{N(\text{Mg})}.$$

The experimental value of the Néel temperature of the ternary alloy  $\text{Li}_{0.01}\text{Mg}_{0.115}\text{Ni}_{0.875}\text{O}$  was  $461^\circ \text{K}$  (Figure 30), while the contribution to the Néel temperature decrease caused by a one per cent lithium addition should have been  $9.1^\circ \text{K}$ . The decrease of  $T_N$  attributable to the magnesium addition is then

$$\Delta T_{N(\text{Mg})} = \Delta T - \Delta T_{N(\text{Li})} = (523-461) - 9.1 = 52.9^\circ\text{K}$$

or  $\Delta T_N/\Delta(\% \text{Mg}) = -4.6^\circ\text{K}/(\% \text{Mg})$ . Again the agreement between this value and the theoretical value of  $-5.7^\circ\text{K}/(\% \text{Mg})$  seems good. It might also be noted that the value of the experimentally observed  $\Delta T_N/\Delta(\% \text{Li})$  is almost exactly twice that of the value of  $\Delta T_N/\Delta(\% \text{Mg})$  as was predicted by the localized model.

The resistivity of each of the lithium-nickel oxide alloys as a function of temperature is given in Figure 32. The break in each curve shifts to lower temperatures with increasing lithium content, and the magnitude of the shift from pure nickel oxide to the 8.23 atomic per cent lithium alloy corresponds to the Néel temperature change shown in Figure 31. The slope of each curve (the activation energy) is lower in the high temperature region, and the slope in the low temperature region decreases with increasing lithium content. All of these trends are in qualitative agreement with the electron-acoustic phonon interaction proposed by Toyozawa(11,12) and the measurements made on lithium doped single crystals by Koide(122). The pure nickel oxide specimen shows an additional break at approximately  $100^\circ\text{C}$ . Similar results have recently been observed in nickel oxide single crystals and have been attributed to

ionization of localized acceptor impurity levels and inter-acceptor "hopping" (267), crystal distortion (258), thermally activated impurity tunnelling (268) and to normal band-type acceptor ionization (269). A schematic resume of the experimentally observed behavior of the resistivity of pure nickel oxide as a function of temperature is shown in Figure 33.

Resistivity measurements alone are not conclusive or even sufficient criteria upon which to base a conduction mechanism. However, the interpretation of the linear decrease in Néel temperature with increasing lithium in terms of localized-electron magnetic theory, and the interpretation of the inter-relation between the elastic modulus and the conduction activation energy in terms of an acoustic coupling effect both give support to some type of "hopping" mechanism. Experimental investigations on the optical properties of nickel oxide yield similar conclusions. Morin (157) found the spectral response of the  $\text{Ni}^{+2}$  ion in the isolated, octahedrally bound,  $\text{Ni}(\text{H}_2\text{O})_6^{+2}$  hydrated complex to be the same as in  $\text{NiO}$ ; other investigators (270-272) found identical response for  $\text{Ni}^{+2}$  in  $\text{MgO}$  and  $\text{Ni}^{+2}$  in  $\text{NiO}$ . Photoelectric emission and optical reflectance work (273) show the various band models not to be applicable to the outer electron shells of nickel oxide. Finally, recent work (274) with the infra-red optical absorption spectra and

high-frequency conductivity of lithium doped nickel oxide single crystals has been interpreted in terms of the small polaron theory of Bogomolov and coworkers(275-276). One of the major difficulties with the description of localized-electron transport properties in terms of optical mode ("polaron") interactions still appears to be the explanation of abrupt changes in conduction properties across critical points (such as the Néel temperature).

To summarize the results and discussion presented in this section, it has been found that

- (1) the low temperature value of Young's modulus increases with increasing lithium content and the temperature of the modulus anomaly decreases in a similar manner.
- (2) The temperature of the modulus anomaly is equivalent to the Néel temperature for each of the alloys, and the linear decrease in Néel temperature with lithium content was interpreted in terms of Van Vlecks'(263) localized-electron theory of antiferromagnetism.
- (3) Resistivity measurements made on well characterized pressure-sintered polycrystalline lithium-nickel oxide alloys agree with the reported results on single crystal material. These include a break at the Néel temperature, a lower activation energy at higher temperatures than at lower temperatures, and a decrease in the low temperature activation energy with increasing lithium content.
- (4) The combined trends in the modulus and resistivity as a function of temperature and impurity level were interpreted in terms of Toyozawa's electron-acoustic mode interaction model which predicts an inverse relation between the elastic modulus and the energy difference between the self-trapped and activated electron states.

- (5) Although more direct techniques such as resistivity, Hall effect and thermoelectric power measurements have not yet provided clarification of the conduction mechanism (primarily because of the unavailability of adequately prepared and well characterized materials) optical studies have provided strong indirect evidence for a localized model.

The success of a quantitatively correct localized electron model appears to depend on the development of a theoretical approach which would simultaneously account for both optical mode and acoustic mode interactions. Close kinship between the theoretical work and the careful preparation and characterization of materials is equally needed in order to realize critical interpretation of observed behavior.

## CONCLUSIONS

1. Pure nickel oxide tends very close to stoichiometric proportions. Deviations from stoichiometry are predominantly caused by the impurity-affected surface properties of the material. The composition of 99.999% pure nickel oxide used in this investigation was found to be  $\text{NiO}_{1.000003 \pm 0.0003\%}$ .
2. The qualitatively observed shift in the Ni/NiO phase boundary with lithium doping additions was explained in terms of a sharp decrease in the Fermi energy level. In turn, this shift causes a very sharp drop in the chemical potential of Ni in NiO, decreases the activity precipitously, and rapidly widens the stable phase field of NiO.
3. The concentrations of  $\text{Li}^{+1}$  and  $\text{Ni}^{+3}$  are equal in pure single phase  $\text{Ni}_{1-2x}^{+2} \text{Li}_x^{+1} \text{Ni}_x^{+3} \text{O}$ . The iodometric titration results indicate the absence of any detectable metallic nickel in the oxides used for this investigation, and show no detectable lithium loss during pressure sintering. The discrepancy between these findings and those previously reported in the literature indicates previous difficulty in the careful preparation and characteriza-

tion of these materials.

4. The sintering behavior of lithium substituted nickel oxide (change in particle texture and shape, increased relative density, increased grain size and change of fracture mode) was interpreted in terms of enhanced oxygen diffusion caused by either a decrease in the chemisorptive surface properties or by an increase in the "mobility" of a coupled anion vacancy-electron hole complex.
5. Electron microprobe results on both pure and doped nickel oxide specimens indicate that significant grain boundary conduction effects are absent in the samples used in this investigation.
6. The measurement of Young's modulus as a function of temperature for the lithium-nickel oxide alloy system was found to be a very sensitive method for the determination of the variation of the Néel temperature with composition. For the lithium-nickel oxide system this variation was explained in terms of a simple localized-electron approach to magnetic properties.

7. For each of the polycrystalline alloys, the trends in the variation of resistivity as a function of temperature agree with previously reported work on single crystal material. These trends, in combination with the modulus results, were interpreted in terms of a localized electron-acoustic mode interaction.

## Appendix I

### Procedure for Determination of Ni<sup>+3</sup>

1. Set up the apparatus as shown in Figure 3.
2. Coat all joints with Dow Corning Silicone Lubricant Stopcock Grease.
3. Before coating the joints of the reaction flask (A), weigh out sample directly into the flask.
4. Pipette 10 ml of conc. HCl into pressure equalizing funnel (B)
5. Pipette 50 ml of 20 weight per cent KI solution (\*) into flask #1 and 25 ml into flask #2.
6. Cool both KI flasks in ice baths.
7. All joints are positively sealed with commercial spring clips.
8. Open all stopcocks, except stopcocks (C) and (D), and slowly pass dry CO<sub>2</sub> through the apparatus for 5 minutes to purge system of air (rapid flow will blow sample powder out of reaction flask).
9. Close stopcock (E), open stopcock (C) and allow 2.5 ml HCl to enter reaction flask. Close stopcocks (C) and (F).
10. Open stopcock (D) and allow CO<sub>2</sub> to bubble through reaction flask.
11. Heat reaction flask with boiling water until the sample dissolves. The solution will be dark green in color and should show no residue at the bottom of the reaction flask. If dissolution is incomplete, repeat steps 9 through 11.

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(\*) Potassium Iodide, Baker Lot 31640, Reagent Grade.

12. Remove boiling water from reaction flask and heat with a direct, but gentle, flame until the sample has been evaporated to dryness.
13. Heat glass ware between reaction flask and flask #1 to dryness.
14. Bubble CO<sub>2</sub> through apparatus for 5 minutes and then close stopcock (G).
15. Remove flasks #1 and #2. Test flask #2 with 2.5 ml starch solution (\*\*). If there is a color change save the solution as it will be added to flask #1 later.
16. Wash gas diffusion tubes into their respective flasks to insure no loss of iodine.
17. The iodine in flask #1 is then titrated with 0.01N Na<sub>2</sub>S<sub>2</sub>O<sub>3</sub> until the solution is pale yellow. Add 5 ml of starch solution. (If flask #2 indicated the presence of a color change it should now be added to the contents of flask #1). The solution should be dark blue.
18. Slowly add Na<sub>2</sub>S<sub>2</sub>O<sub>3</sub> until the end point (blue to clear) is reached.
19. The weight percent Ni<sup>+3</sup> is calculated from the following equation:

$$\text{weight \%Ni}^{+3} = \left( \frac{\text{ml} \times N \times \frac{58.71}{1000}}{\text{sample wt}} \right) \times 100$$

20. The atomic per cent Ni<sup>+3</sup> is calculated from the following equation:

$$\text{atomic \%Ni}^{+3} = \left( \frac{\frac{\text{weight \%Ni}^{+3}}{58.71}}{\frac{\text{weight \%Ni}^{+3}}{58.71} + \frac{[100 - \text{weight \%Ni}^{+3}]}{74.71}} \right) \times 100$$

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(\*\*) 2 grams Baker's Soluble Starch Powder in 1 liter distilled and deionized water.

## Appendix 2

### "Pulse Transmission" and "Resonant Sphere"

#### Elastic Modulus Measurements

The accurate determination of dynamic elastic moduli on small samples (less than one inch in length) has been found to be of utmost importance for the research and development of new materials. Standard measurement techniques, such as the Forster resonance (213) and the sonic "pulse-echo" (220) methods, have not been found to be directly applicable to small specimen measurements. The Forster method consists of resonating a "free" bar with frequencies in the audible acoustic range and thus requires a long sample (equivalent to the long wavelength). The "pulse-echo" technique depends on a direct measurement of the transit time of a mechanical wave through the specimen and is therefore not accurate for short specimens (very short transit times). McSkimin has proposed two modifications of the basic sonic method, the "Phase Comparison" (221) and "Pulse Superposition" (222) technique, in order to provide more accurate transit time measurements. The phase comparison technique measures the difference in transit time between two pulses which have traveled different numbers of round trips along a specimen. The pulse superposition technique consists

of the superposition of two different waves of similar constant frequency but with a slight phase shift. A "beat" frequency is produced, and the transit time of this beat may be related to the velocity of sound in the sample. Further advancement was made with the development of the "pulse transmission" or "Time of Flight" technique by Birch (223) and the elimination of major instrumentation errors for the same technique by Mataboni and Schreiber (224).

The pulse transmission method (Figure 19) consists of displaying both a variable "timing frequency" and the initial test pulse, or alternately the final specimen signal, on the same oscilloscope. The variable timing frequency is adjusted (both in frequency and pulse shape) until the time delay between the initial test pulse and the specimen response signal is equal to an integral number of cycles (N) of timing frequency. The time between peaks on the timing frequency display is just  $\frac{1}{f}$  and the specimen transit time is

$$t = \frac{1}{f} \times N.$$

The velocity of sound in a sample of length, L, is

$$v = L/t = L\left(\frac{f}{N}\right).$$

In practice, the driver and pickup transducers attached to the specimen may be either x-cut quartz discs for the measurement of the longitudinal wave velocity ( $v_1$ ), or Y-cut quartz

discs for the measurement of the shear wave velocity ( $v_s$ ). The shear modulus (G), Young's modulus (E), bulk modulus (K) and Poisson's ratio ( $\sigma$ ) are given as:

$$G = \rho v_s^2$$

$$E = 2\rho v_s^2 (1 + \sigma)$$

$$K = \rho \left( v_l^2 - \frac{4}{3} v_s^2 \right)$$

$$\sigma = \frac{\left[ 1 - \frac{1}{2} \left( \frac{v_l}{v_s} \right)^2 \right]}{\left[ 1 - \left( \frac{v_l}{v_s} \right)^2 \right]}, \text{ where}$$

$\rho$  = specimen density

The previous sonic methods suffer, to some degree, from inherent inaccuracies in measuring short transit times, from large end effects caused by specimen geometry, and transducer coupling effects relative to the specimen size. All of these difficulties were eliminated through the development of the "resonant sphere technique" by Fraser and LeCraw (225). The method consists of placing a small sphere of the sample on a single shear wave transducer as in Fraser and LeCraw's original technique, or between two transducers, as in Soga and Anderson's (226) modified method, and of monitoring the resonant frequencies of the sphere.

The major experimental error in this technique is the production of specimens of good sphericity and the measurement of the specimen diameter. Pneumatic sphere grinding

equipment (227) as shown in Figure 20 is used to grind a spherical shape from that of a cube by random tangential abrasion of the cube against the inner wall of the alumina container. A highly polished surface is then obtained by lapping the sphere with successively finer silicon carbide powder and then Linde "B" alumina with counter-rotating lapping pipes (228) as shown in Figure 21.

A schematic representation of the resonant sphere method is shown in Figure 22. The variable frequency signal that excites the specimen is continuously switched on and off by the solid state switch and is monitored on the scope. When the generated frequency causes the sphere to resonate, the sphere continues to vibrate after the signal is switched off and a decay pattern is observed. An RC decay generator with variable capacitance and resistance is used to match the decay pattern, and the "Q" for the circuit (acoustic loss) may be calculated (227) from

$$Q = 2\pi f\tau = 2\pi f(R \cdot C).$$

The modes of vibration of the sphere are either spherical or shear (Figure 23) waves and only the spherical modes are dependent on Poisson's ratio. Fraser and LeCraw (225) have shown that an arbitrary experimental resonant frequency,  $f$ , for a sphere of diameter,  $d$ , may be related to the resonant frequency of a given specific mode,  $f_n$ , by a non-dimensional

normalized or "reduced frequency",  $f_r$ , which is not a function of specimen diameter, according to the relation:

$$f_r = \frac{f}{f_n} \times A_n$$

where  $A_n$  = mode constant for the nth mode of free-oscillation of a homogeneous elastic sphere.

The constants,  $A_n$ , have been determined and tabulated by Sato and Usami (229), and a plot (Figure 24) of reduced frequency versus Poisson's ratio,  $\sigma$ , for each vibrational mode has been given by Fraser and LeCraw (225).

In practice, one of the lower frequency, high intensity modes out of the experimental resonant frequency spectrum is arbitrarily chosen, identified as a specific pure shear mode (therefore not dependent on Poisson's ratio), and a series of reduced frequencies are calculated. A match between the experimental reduced frequencies and the plot of Fraser and LeCraw (225) provides a solution for Poisson's ratio (because the spherical modes are single valued functions of Poisson's ratio); at the same time, each of the vibrational modes is identified. The process may be simplified if the approximate value of Poisson's ratio has been previously determined (as by the "Pulse Transmission" method). If the initial identification of the first pure shear mode was incorrect, the entire process is repeated until a match is found.

The shear velocity may be calculated (226) for each of the pure shear modes from the relation:

$$v_{\text{shear}} = \frac{\pi d f_n}{A_n}$$

The shear velocity and the value of Poisson's ratio are then used to calculate the remaining elastic moduli.

### Appendix 3

#### The Composite Oscillator

The fundamental frequency of free longitudinal vibration of a bar has been found (233) to be related to Young's modulus according to the equation

$$E = \rho f^2 (4L^2 + 2\pi^2 \sigma^2 r^2) \approx 4\rho f^2 L^2 \quad \text{Eq (A3.1)}$$

where  $\rho$  = specimen density

$f$  = frequency of free vibration

$L$  = length

$\sigma$  = Poisson's ratio

$r$  = radius

If the radius is small compared to the length of the bar, and since  $\sigma < 0.5$ , the last term may normally be ignored. If a piezoelectric quartz crystal is attached to a rod of given dimensions and if a sinusoidally varying potential difference is applied across the electrode surfaces of the crystal, a stable state of forced vibration is established for the composite system. When the applied frequency is equal to the free vibrational frequency of the composite system, a "resonant" condition is established and the amplitude of the output is at a maximum. If the resonant frequency of the composite can be related to that of the isolated bar,

then the modulus of the bar could be calculated from the above equation. Zacharias (234) first used this method to measure Young's modulus at elevated temperature for thin nickel rods. Fine (235) explained that for materials with high internal friction the capacitance of the crystal distorts the output and the system must be balanced by the use of a second(or "gauge") crystal. If the crystals and specimens are frequency matched then, at resonance, each section is one-half wave length long, the frequency nodes appear at the center of each section, and the stress nodes occur at the cemented joints.

The relation between the resonant frequency of a three part composite oscillator and the natural frequency of each of the components was first given by Rose (236) and then by Cooke (237) as

$$m_1 \left[ \frac{\tan y_1}{y_1} \right] + m_2 \left[ \frac{\tan y_2}{y_2} \right] + m_3 \left[ \frac{\tan y_3}{y_3} \right] - \frac{m_1 m_2 y_3}{y_1 y_2 m_3} \{ \tan y_1 \tan y_2 \tan y_3 \} = 0$$

where  $m_i$  = mass of each section

$$y_i = \pi \left\{ \frac{f_x}{f_i} \right\}$$

$f_x$  = resonant frequency of the composite

$f_i$  = resonant frequency of each section.

If the quartz crystals are matched such that  $m_1 = m_2 = m_c$ ,

$y_1 = y_2 = y_c$ , and  $m_3 = m_s$ ,  $y_3 = y_s$ , then this equation may be rewritten in the form

$$(2m_c)f_c \tan \pi \frac{f_x}{f_c} + m_s f_s \tan \pi \frac{f_x}{f_s} \left[ 1 - \frac{\left( \frac{m^2 f^2}{c \ c} \right)}{\left( \frac{m^2 f^2}{s \ s} \right)} \tan^2 \pi \frac{f_x}{f_c} \right] = 0 \quad \text{Eq(A3.2)}$$

In theory, it is possible to measure the resonant frequency of the crystals alone, and then of the composite, and use equation (A3.2) to calculate the resonant frequency ( $f_s$ ) of the sample. In practice, the crystals and specimen may be roughly matched such that  $f_x \approx f_c \approx f_s$  and the  $\tan^2$  term may then be ignored. This results in a simplified expression,

$$M_c f_c \tan \pi \frac{f_x}{f_c} + m_s f_s \tan \pi \frac{f_x}{f_s} = 0 \quad \text{Eq(A3.3)}$$

where  $M_c = 2m_c =$  combined crystal mass.

The tangent terms may be manipulated (238) such that

$$\tan \pi \frac{f_x}{f_i} = \tan \left[ \pi + \pi \left\{ \frac{f_x}{f_i} - 1 \right\} \right] = \tan \pi \left[ \frac{f_x}{f_i} - 1 \right]$$

since

$$\tan(\alpha + \beta) = (\tan \alpha + \tan \beta) / (1 - \tan \alpha \tan \beta).$$

If  $f_x \approx f_i$ , then  $\frac{f_x}{f_i} \approx 1$ ,  $\left[ \frac{f_x}{f_i} - 1 \right]$  is small, and

$$\tan \pi \frac{f_x}{f_i} = \tan \pi \left[ \frac{f_x}{f_i} - 1 \right] \approx \pi \left[ \frac{f_x}{f_i} - 1 \right]. \quad \text{Thus if the crystals}$$

are closely matched, equation (A3.3) simplifies into the

linear relation,

$$f_s = f_x + \frac{M_c}{m_s} (f_x - f_c). \quad \text{Eq(A3.4).}$$

The assumptions inherent in the composite oscillator method may be summarized as,

- (1) internal friction for each of the components is small
- (2) there is no Poisson's contraction or expansion as the modulus changes (if  $\sigma$  changes then  $L$  would change)
- (3) there is no length change with temperature (thermal expansion is small)
- (4) cement joints are elastic and strain free, and
- (5) stress nodes are at or near the joints.

For this investigation, a CDC 6400 computer was used to solve for the frequency of the specimen. Equation (A3.4) provided an initial trial value for  $f_s$  and then a Newton-Raphson method was used to solve Equation (A3.2) or (A3.3) for  $f_s$ . Young's modulus was then computed from Equation (A3.1) and the modulus was plotted as a function of temperature on a Calcomp Plotter. The final program design and a tabulation of all of the pertinent data (with  $\tan^2$  term assumed small) are presented at the end of this appendix.

Marx (239) has shown that the acoustic loss for a composite oscillator such as that described above can be expressed as

$$\delta = K \left\{ \frac{V_D}{V_G} \right\}$$

where  $V_D$  = input voltage to the driver crystal

$V_G$  = output voltage from the gauge crystal

$K$  = constant depending on the equipment and the material.

A relative measure of  $\delta$  can be obtained by assuming  $K = 1$  and using the ratio of the input to output voltages.

```

REAL MS,MC,L
INTEGER V,VI,VII,VIII
DIMENSION EASY(100),TEMP(100),ELAS(100),TFM(100)
DIMENSION E1(100),E2(100),E3(100),E4(100),F5(100)
DIMENSION T1(100),T2(100),T3(100),T4(100),T5(100)
DIMENSION E(100),T(100)
DIMENSION BOX1(100),BOX2(100),BOX3(100),BOX4(100)
PI=3.14159265
PRINT 1
1 FORMAT(1H1,49H      NEWTON-RAPHSON METHOD TO SOLVE THE EQUATION )
PRINT 2
2 FORMAT(55H      MS*FS*TAN(PI*FX/FS)+4C*F(*TAN(PI*FX/FC)=0 , )
PRINT 3
3 FORMAT(55H      TO CALCULATE YOUNGS MODULUS FROM FS • AND TO )
PRINT 4
4 FORMAT(55H      PLOT THE MODULUS AS A FUNCTION OF TEMPERATURE )
READ 21,ITEM
NUMBER OF CURVES,MAXIMUM=H,PRINT IN COLUMN 3 OF DATA CARD
DO 60 MEN=1,ITFM
PRINT 60
600 FORMAT(1H1,//////)
READ 10
100 FORMAT(66H
1
)
PRINT 10
C SAMPLE IDENTITY,START IN COL.19 OF DATA CARD
READ 21,I
21 FORMAT(I3)
C NUMBER OF DATA POINTS IN EACH RUN,MAXIMUM=100,LAST DIGIT IS COLUMN
C 3
READ 22,MS,MC,RHU,L
22 FORMAT(4(F10.4))
C EXPERIMENTAL CONSTANTS,MASS OF SPECIMEN IN COLUMN 1-10, COMBINED
C MASS OF CRYSTALS IN COLUMN 11-20,SPECIMEN DENSITY IN COLUMN 21-30,
C SPECIMEN LENGTH IN COLUMN 31-40,ALL IN CGS SYSTEM OF UNITS

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```

PRINT 24,MS,MC,RHO,L
240FORMAT(1HX,MS=*,F10.4,2X,MC=*,F10.4,2X,*RHO=*,F10.4,2X,
1*L=*,F9.4)
DO 52 M=1,I
C EXPERIMENTAL DATA,FREQUENCY OF CRYSTALS IN COLUMN 1-10,FREQUENCY
C OF COMPOSITE OSCILLATOR IN COLUMN 1-20,TEMPERATURE IN COLUMN 21-
C 30
READ 23,FC,FX,T(M)
BOX3(M)=FX $ BOX4(M)=FC
K=1
C FOR VARIABLE TAN SQUARE TERM REPLACE THIS CARD WITH
C K=1 $ VK=1. $ 4IX=1
23 FORMAT(3(F10.4))
FS=FX+(MC/MS)*(FX-FC)
BOX1(M)=FS
C = 1.
C FOR VARIABLE TAN SQUARE TERM REPLACE THIS CARD WITH
C C=1.-((ABS(MC*FC*TAN(PI*FX/FC)/(MS*FS))))**2.
H=MC*FC*TAN( PI*FX/FC)
49 A=MS*FS*TAN( PI*FX/FS)
E(M)=((ABS(2.*L*FS))**2.)*RHO $ ZERO=A*C+R
C FOR VARIABLE TAN SQUARE TERM REPLACE THIS CARD WITH
C ZERO=ZERO
C ZERO=ABS(A*C)-ABS(B)
C IF(MIX.EQ.1) GO TO 99
C IF (ABS(ZERO).GT.ABS(ZERO1))VK=VK
C 99 MIX=0
C E(M)=((ABS(2.*L*FS))**2.)*RHO
BOX2(M)=FS
IF (ABS(ZERO)-1.E-2)52,52,51
51 IF(ABS(ZERO).GT.100000.)K=2.
IF(K.GT.1)GO TO 299

```

```

FS=FS*(ZERO/(MS*FS*((ABS(COS(PI*FX/FS)*FS))**2.)*PI*FX-(A/FS)))
1*1./C
C FOR VARIABLE TAN SQUARE TERM REPLACE THIS CARD WITH
C 1*1./C*VK
GO TO 49
299 FS=FS+ZERO*.001
C FOR VARIABLE TAN SQUARE TERM RPLACF THIS CARD WITH
C 299 FS=FS+ZERO*.01*VK
GO TO 49
52 CONTINUE
PRINT 53
530FORMAT(/,1BX,*T,DEGC FC,CPS* ) FSO,CPS F SF,CPS
1 PRINT 100
100 FORMAT(1H0)
DO 60 M=1,1
PRINT 54,T(M),E(M),BOX1(M),BOX2(M),BOX3(M),BOX4(M)
54 FORMAT(1BX,F6.1,6X,E13.5,4(6X,F7.0))
IF(MFN.GT.1) GO TO 500
EASY(M)=E(M)
TEMP(M)=T(M)
II=I
GO TO 60
500 IF(MFN.GT.2) GO TO 501
ELAS(M)=E(M)
TEM(M)=T(M)
III=J
GO TO 60
501 IF(MFN.GT.3)GO TO 502
E1(M)=E(M)
T1(M)=T(M)
IV=I
GO TO 60
502 IF(MFN.GT.4)GO TO 503
E2(M)=E(M)
T2(M)=T(M)

```

```

V=I
GO TO 60
503 IF (MEN.GT.5)GO TO 504
E3(M)=E(M)
T3(M)=T(M)
VI=I
GO TO 60
504 IF (MEN.GT.6)GO TO 505
E4(M)=E(M)
T4(M)=T(M)
VII=I
GO TO 60
505 IF (MEN.GT.7)GO TO 60
E5(M)=E(M)
T5(M)=T(M)
VIII=I
GO TO 60
60 CONTINUE
CALL NAMPLT
CALL QIKSET(7.0,0.0,50.0,9.0,8.0E11,2.E11)
0CALL QIKPLI(TEMP,EASY, II, 19H*TEMPERATURE,DEG C*,
127H*YOUNGS MODULUS,DYNFS/SQCMS,35H*YOUNGS MODULUS VERSUS TEMPERATU
2RE#)
CALL PLOT(-8.0,1.0,-3)
CALL QLINE(TEMP,EASY,-II,0)
CALL QLINE(TEMP,ELAS,-III,-2)
CALL QLINE(T1,E1,-IV,-3)
CALL QLINE(T2,E2,-V,-1)
CALL QLINE(T3,E3,-VI,-1)
CALL QLINE(T4,F4,-VII,-4)
CALL QLINE(T5,E5,-VIII,-5)
CALL QLINE(T,E,-I,-10)
CALL PLOT(10.0,0.0,-3)
CALL ENDPLT
CALL EXIT
END

```

PURE NIO,RUN 16,118.5 KC XTALS,FRST UP  
 MS= 5.1881 MC= 4.8352 RHO= 6.7830 L= 1.9000

T,DEGC	E,DYN/SQCM	FSO,CPS	FSF,CPS	FX,CPS	FC,CPS
26.0	9.09720E+11	96259	96374	107350	119251
83.5	9.05293E+11	96019	96139	107208	119214
119.0	9.24039E+11	97033	97129	107716	119179
158.0	9.37089E+11	97731	97813	108048	119118
188.0	9.67268E+11	99320	99375	108841	119057
210.0	1.00947E+12	101490	101520	109938	119003
212.0	1.01389E+12	101714	101742	110051	118997
222.0	1.04923E+12	103484	103500	110952	118965
234.0	1.13095E+12	107452	107455	112989	118930
245.0	1.39093E+12	119167	119167	119037	118897
247.0	1.59374E+12	131484	131501	125410	118893
248.0	1.87626E+12	138326	138405	128950	118890
248.5	2.40049E+12	155779	156551	137984	118890
249.0	2.42918E+12	156645	157484	138431	118888
249.5	2.43282E+12	156754	157602	138487	118887
250.0	2.43508E+12	156821	157675	138521	118885
252.0	2.43539E+12	156830	157685	138522	118878
256.0	2.42996E+12	156664	157509	138433	118869
288.0	2.31300E+12	153075	153671	136527	118771
312.0	2.20481E+12	149622	150034	134708	118705
315.0	2.18443E+12	148958	149339	134359	118695

PURE NIO,RUN 16,118.5 KC XTALS,FRST DWN  
 MS= 5.1881 MC= 4.8352 RH0= 6.7830 L= 1.9000

T,DEGC	E,DYN/SOCM	FSO,CPS	FSF,CPS	FX,CPS	FC,CPS
23.0	9.21863E+11	96914	97015	107690	119252
88.0	9.29675E+11	97334	97425	107886	119208
119.0	9.41240E+11	97950	98029	108191	119179
157.0	9.68123E+11	99364	99419	108895	119122
189.0	1.00993E+12	101513	101543	109975	119055
199.0	1.02888E+12	102468	102491	110459	119033
205.0	1.04398E+12	103223	103241	110842	119017
212.0	1.06377E+12	104202	104215	111339	118997
222.0	1.09916E+12	105928	105934	112217	118965
236.0	1.20017E+12	110695	110695	114665	118925
245.0	1.42300E+12	120533	120533	119744	118897
248.0	1.79362E+12	135279	135323	127373	118890
250.0	2.43006E+12	156671	157512	138443	118885
252.0	2.43326E+12	156766	157616	138489	118878
262.0	2.41538E+12	156226	157036	138197	118852
268.0	2.40028E+12	155769	156544	137949	118830
272.0	2.38232E+12	155220	155957	137661	118820

PURE NIO,RUN.16,118.5 KC XTALS,SCND UP  
 MS= 5.1881 MC= 4.8352 RHO= 6.7830 L= 1.9000

T,DEGC	E,DYN/SQCM	F50,CPS	FSF,CPS	FX,CPS	FC,CPS
37.0	9.22701E+11	96960	97059	107710	119245
90.0	9.23850E+11	97022	97119	107724	119207
112.0	9.26587E+11	97169	97263	107791	119188
183.0	9.80311E+11	99996	100043	109195	119065
207.0	1.01680E+12	101860	101888	110140	119024
237.0	1.18874E+12	110166	110166	114389	118920
240.0	1.25457E+12	113176	113176	115942	118910
241.0	1.29812E+12	115123	115123	116949	118908
243.0	1.31144E+12	115712	115712	117252	118904
244.0	1.36569E+12	118081	118081	118476	118900
245.0	1.42893E+12	120784	120785	119873	118895
246.0	1.52319E+12	124703	124705	121900	118892
247.5	1.79558E+12	135352	135397	127410	118888
249.5	2.16033E+12	148175	148513	134045	118884
250.0	2.43241E+12	156741	157588	138478	118882
250.0	2.44042E+12	156981	157847	138602	118882
252.0	2.44566E+12	157137	158017	138682	118880
261.0	2.43551E+12	156831	157689	138509	118850
294.0	2.36115E+12	154567	155263	137294	118760

PURE NIO,RUN 16,118.5 KC XTALS,SCND DWN  
 MS= 5.1881 MC= 4.8352 RHO= 6.7830 L= 1.9000

T,DEGC	E,DYN/SQCM	FSO,CPS	FSF,CPS	FX,CPS	FC,CPS
26.0	9.22531E+11	96950	97050	107710	119255
75.0	9.27281E+11	97206	97300	107823	119215
181.0	1.00318E+12	101169	101203	109804	119069
182.0	1.00418E+12	101220	101254	109830	119068
182.0	1.00707E+12	101367	101399	109906	119068
184.0	1.00751E+12	101389	101421	109916	119065
185.5	1.01034E+12	101533	101564	109989	119062
190.0	1.02314E+12	102180	102205	110318	119050
192.0	1.02326E+12	102186	102211	110321	119050
196.0	1.02850E+12	102449	102473	110455	119045
204.0	1.04422E+12	103234	103253	110852	119025
216.0	1.08531E+12	105254	105265	111879	118985
222.0	1.10693E+12	106303	106308	112411	118965
226.0	1.12462E+12	107151	107154	112845	118955
248.5	1.70123E+12	131772	131791	125558	118890
250.5	2.45383E+12	157381	158281	138809	118882
254.0	2.45072E+12	157288	158180	138759	118878
282.0	2.39599E+12	155665	156437	137879	118795
284.0	2.38890E+12	155418	156172	137749	118790

•12 PCT LI,RUN 22,118.5 KC XTALS,FRST UP  
 MS= 4.3655 MC= 4.8352 RHO= 6.2513 L= 1.8910

T,DEGC	E,DYN/SQCM	F50,CPS	FSF,CPS	FX,CPS	FC,CPS
25.0	9.14305E+11	101007	101120	110593	119248
82.0	9.28055E+11	101782	101878	110943	119214
135.0	9.45787E+11	102770	102847	111382	119157
156.0	9.55000E+11	103279	103346	111606	119124
170.0	9.66839E+11	103928	103985	111898	119094
192.0	9.93616E+11	105376	105415	112561	119048
203.5	1.01533E+12	106532	106560	113096	119022
213.0	1.04417E+12	108046	108063	113800	118995
220.0	1.07065E+12	109414	109425	114436	118970
227.5	1.12341E+12	112086	112089	115693	118950
234.0	1.19311E+12	115514	115514	117309	118930
239.0	1.27850E+12	119576	119576	119226	118910
241.5	1.33707E+12	122284	122284	120510	118908
243.5	1.41471E+12	125786	125785	122167	118900
247.0	1.59959E+12	133749	133751	125940	118890
248.0	1.68297E+12	137180	137193	127567	118888
248.5	1.76346E+12	140402	140435	129095	118886
249.0	1.80367E+12	141980	142027	129843	118885
250.5	1.81532E+12	142433	142485	130057	118883
257.0	1.81568E+12	142447	142499	130053	118863
272.0	1.80564E+12	142056	142105	129845	118820

.12 PCT LI,RUN 22,118.5 KC XTALS,FRST DWN  
 MS= 4.3655 MC= 4.8352 RHO= 6.2513 L= 1.8910

T,DEGC	E,DYN/SQCM	F50,CPS	F5F,CPS	F5,CPS	FC,CPS
64.0	8.98336E+11	100097	100233	110151	119228
96.5	8.99176E+11	100146	100280	110161	119203
126.0	9.02896E+11	100360	100488	110245	119170
146.0	9.08090E+11	100656	100776	110370	119140
163.0	9.20731E+11	101373	101475	110693	119108
206.0	9.87875E+11	105068	105110	112397	119014
245.0	1.48045E+12	128675	128674	123537	118898
246.5	1.54601E+12	131492	131492	124872	118895
247.0	1.59119E+12	133397	133400	125775	118893
247.5	1.64076E+12	135455	135461	126750	118891
248.0	1.68128E+12	137111	137124	127535	118889
248.0	1.73518E+12	139280	139305	128564	118889
249.0	1.78977E+12	141437	141479	129586	118886
249.5	1.81103E+12	142267	142317	129979	118885
251.0	1.81548E+12	142440	142492	130060	118883
254.0	1.81656E+12	142481	142534	130073	118870
259.0	1.81439E+12	142397	142449	130025	118855

1.96 PCT LI,RUN 25.118.5 KC XTALS,FRST UP  
 MS= 4.7995 MC= 4.8352 RHO= 6.7200 L= 1.8840

T,DEGC	E,DYN/SQCM	FS0,CPS	FSF,CPS	FX,CPS	FC,CPS
25.5	9.10007E+11	97514	97662	108424	119251
86.0	9.44294E+11	99386	99485	109336	119213
154.0	9.97918E+11	102219	102271	110704	119126
188.0	1.08288E+12	106521	106536	112812	119057
197.0	1.12485E+12	108573	108580	113822	119032
206.0	1.18575E+12	111479	111481	115261	119015
217.0	1.30793E+12	117084	117084	118038	118985
220.5	1.38601E+12	120528	120528	119746	118970
222.0	1.43900E+12	122810	122810	120882	118968
225.0	1.52544E+12	126444	126445	122688	118960
226.0	1.57990E+12	128679	128683	123800	118957
227.0	1.63375E+12	130849	130857	124878	118951
228.0	1.72966E+12	134620	134643	126754	118946
230.0	1.88580E+12	140510	140589	129685	118940
231.5	2.03728E+12	145940	146127	132388	118936
233.0	2.07515E+12	147255	147479	133040	118930
237.5	2.07481E+12	147243	147467	133029	118920
243.0	2.02670E+12	145569	145747	132185	118900

1.96 PCT LI,RUN 25,118.5 KC XTALS,FRST DWN  
 MS= 4.7995 MC= 4.8352 RHO= 6.7200 L= 1.8840

T,DEGC	E,DYN/SOCM	F50,CPS	F5F,CPS	F5,CPS	FC,CPS
28.0	9.54093E+11	99910	100000	109614	119246
96.0	1.00586E+12	102630	102677	110948	119205
152.0	1.05473E+12	105118	105142	112150	119130
178.0	1.11661E+12	108174	108182	113646	119078
220.0	1.34533E+12	118746	118746	118859	118971
221.0	1.36300E+12	119523	119523	119245	118969
222.0	1.38963E+12	120685	120685	119822	118965
223.5	1.42235E+12	122098	122098	120524	118962
225.0	1.47293E+12	124250	124250	121595	118960
227.0	1.60319E+12	129623	129628	124267	118951
229.0	1.71287E+12	133959	133988	126428	118943
230.0	2.00227E+12	144709	144866	131777	118940

1.96 PCT LI,RUN 25,118.5 KC.XTALS.SCND UP  
 MS= 4.7995 MC= 4.8352 RHO= 6.7200 L= 1.8840

T,DEGC	E,DYN/SQCM	FSD,CPS	FSF,CPS	FX,CPS	FC,CPS
110.0	9.90750E+11	101846	101903	110549	119188
131.0	1.05836E+12	105300	105322	112257	119163
145.0	1.03972E+12	104361	104391	111778	119140
150.0	1.05034E+12	104897	104923	112041	119132
153.5	1.07415E+12	106088	106105	112631	119126
178.0	1.08839E+12	106792	106806	112960	119082
190.0	1.13650E+12	109135	109141	114111	119050
204.0	1.20159E+12	112222	112223	115631	119015
213.0	1.26996E+12	115372	115372	117185	118985
220.0	1.37231E+12	119931	119931	119449	118971
222.0	1.40884E+12	121516	121516	120236	118965
227.0	1.61107E+12	129940	129945	124425	118951
229.0	1.70942E+12	133834	133853	126361	118943
229.5	1.77747E+12	136456	136491	127666	118941
231.0	1.89682E+12	140914	141000	129885	118937
232.0	2.02331E+12	145626	145805	132230	118933

1.96 PCT LI,RUN 25.118.5 KC XTALS,SCND DWN  
 MS= 4.7995 MC= 4.8352 RHO= 6.7200 L= 1.8840

T,DEGC	E,DYN/SQCM	FSO,CPS	FSF,CPS	FX,CPS	FC,CPS
25.0	9.59119E+11	10017A	100263	109750	119251
104.0	1.00279E+12	102471	102520	110864	119195
203.0	1.18417E+12	111405	111407	115228	119023
215.0	1.26749E+12	115259	115259	117130	118987
229.0	1.75992E+12	135785	135816	127333	118943
230.0	1.88383E+12	140438	140516	129649	118940
231.0	2.01197E+12	145052	145216	131946	118937
232.0	2.02805E+12	145617	145795	132224	118930
232.5	2.06145E+12	146781	146991	132804	118930
236.0	2.04814E+12	146319	146516	132571	118925
239.0	2.04469E+12	14619A	146392	132504	118911

4.97 PCT LI, RUN 26, 118.5 KC XTALS, FRST UP  
 MS= 4.9309 MC= 4.8352 RH0= 6.5850 L= 1.8980

T, DEGC	E, DYN/SQCM	F50, CPS	FSF, CPS	FX, CPS	FC, CPS
39.0	9.79456E+11	101547	101599	110308	119242
64.0	9.96243E+11	102425	102466	110744	119228
95.0	1.02413E+12	103862	103890	111457	119202
108.0	1.04212E+12	104777	104798	111913	119190
114.0	1.05155E+12	105254	105272	112151	119185
124.0	1.063361E+12	105858	105873	112449	119170
139.0	1.09193E+12	107264	107274	113149	119150
151.0	1.12347E+12	108807	108812	113919	119132
161.0	1.16570E+12	110836	110838	114934	119113
183.5	1.35173E+12	119355	119355	119209	119060
189.0	1.44847E+12	123552	123552	121324	119052
192.0	1.52725E+12	126865	126868	122995	119048
193.5	1.59702E+12	129726	129733	124438	119045
196.0	1.67073E+12	132676	132693	125925	119040
197.0	1.74956E+12	135752	135788	127477	119038
198.0	1.81394E+12	138204	138263	128712	119032
199.0	1.86973E+12	140287	140373	129763	119031
200.0	1.92604E+12	142349	142472	130804	119030
201.0	2.00417E+12	145147	145333	132215	119027
201.5	2.09372E+12	148262	148544	133787	119025
202.0	2.16946E+12	150823	151207	135079	119023
202.5	2.22830E+12	152766	153244	136059	119021
203.0	2.27287E+12	154211	154769	136788	119020
203.5	2.28837E+12	154708	155295	137038	119018
204.0	2.29951E+12	155064	155673	137216	119015
207.0	2.30505E+12	155240	155861	137304	119013
213.0	2.30395E+12	155203	155823	137274	118990
218.0	2.30160E+12	155128	155744	137230	118978
223.0	2.29523E+12	154924	155528	137119	118962

4.97 PCT LI,RUN 26.118.5 KC XTALS,FRST DWN  
 MS= 4.9309 MC= 4.8352 RHO= 6.5850 L= 1.8980

T,DEGC	E,DYN/SQCM	FS0,CPS	FSF,CPS	FX,CPS	FC,CPS
34.0	9.36869E+11	99279	99365	109164	119245
82.0	9.71583E+11	101133	101190	110084	119212
124.0	1.02862E+12	104092	104117	111557	119170
175.0	1.24544E+12	114566	114566	116801	119080
190.5	1.49372E+12	125466	125467	122290	119051
193.0	1.55825E+12	128145	128149	123640	119046
195.0	1.66592E+12	132486	132502	125830	119042
197.0	1.74273E+12	135489	135522	127344	119038
198.0	1.78595E+12	137145	137193	128177	119032
198.0	1.82405E+12	138584	138648	128904	119032
199.0	1.89339E+12	141158	141259	130203	119031
200.0	1.96395E+12	143716	143867	131494	119030
201.5	2.04340E+12	146524	146748	132909	119025
202.0	2.12049E+12	149176	149491	134247	119023
207.0	2.32543E+12	155886	156548	137630	119013
214.0	2.31701E+12	155618	156264	137486	118995
216.0	2.31274E+12	155482	156120	137415	118990

6.84 PCT LI,RUN 30.118.5 KC XTALS.FRST UP  
 MS= 4.9643 MC= 4.8352 RHO= 6.5718 L= 1.9060

T,DEGC	E,DYN/SQCM	F50,CPS	FSF,CPS	FX,CPS	FC,CPS
28.0	9.63270E+11	100369	100434	109684	119248
85.0	1.02292E+12	103467	103497	111236	119212
102.5	1.05010E+12	104843	104862	111926	119198
121.5	1.09546E+12	107094	107103	113056	119177
131.0	1.12607E+12	108584	108589	113805	119165
153.0	1.23177E+12	113571	113571	116313	119128
156.5	1.26486E+12	115087	115087	117077	119120
162.0	1.31534E+12	117361	117361	118224	119110
165.5	1.35456E+12	119098	119098	119099	119100
170.0	1.40717E+12	121389	121389	120256	119093
173.0	1.45534E+12	123449	123449	121296	119086
176.0	1.49993E+12	125325	125326	122245	119083
179.0	1.54406E+12	127154	127156	123166	119072
181.0	1.59226E+12	129120	129125	124161	119070
184.0	1.64127E+12	131087	131098	125155	119065
186.0	1.72054E+12	134201	134226	126730	119060
189.0	1.78433E+12	136647	136692	127965	119051
191.0	1.85763E+12	139395	139471	129356	119049
193.0	1.92748E+12	141951	142069	130649	119045
195.0	1.95261E+12	142856	142992	131103	119040
206.0	1.91591E+12	141531	141642	130424	119020

6.84 PCT LI,RUN 30,118.5 KC XTALS,FRST DWN  
 MS= 4.9643 MC= 4.8352 RHO= 6.5718 L= 1.9060

T,DEGC	E,DYN/SQCM	FSO,CPS	FSF,CPS	FX,CPS	FC,CPS
63.0	9.77234E+11	101105	101159	110046	119226
98.0	1.03114E+12	103886	103912	111442	119200
121.5	1.09172E+12	106911	106920	112963	119177
134.0	1.13694E+12	109108	109112	114063	119150
169.0	1.40658E+12	121363	121363	120243	119093
182.5	1.66762E+12	132131	132146	125685	119067
184.0	1.71940E+12	134156	134182	126710	119065
185.0	1.73873E+12	134903	134934	127087	119062
186.0	1.78311E+12	136601	136645	127946	119060
187.5	1.82129E+12	138041	138100	128674	119057
188.5	1.84373E+12	138879	138948	129096	119052
189.0	1.88677E+12	140469	140561	129901	119051
190.5	1.91650E+12	141554	141664	130450	119050
191.0	1.97987E+12	143830	143987	131602	119048
192.5	1.99563E+12	144388	144559	131884	119046
197.0	1.99837E+12	144485	144658	131930	119040
203.0	1.96028E+12	143130	143273	131235	119022

8.23 PCT LI,RUN 19,118.5 KC XTALS,FRST UP  
 MS= 4.6808 MC= 4.8352 RHO= 6.2690 L= 1.8980

T,DEGC	E,DYN/SQCM	FSO,CPS	FSF,CPS	FX,CPS	FC,CPS
26.5	1.32299E+12	121019	121019	120120	119250
85.0	1.44749E+12	126585	126585	122838	119211
100.0	1.48611E+12	128261	128263	123656	119198
114.0	1.53309E+12	130270	130274	124636	119182
125.0	1.57378E+12	131984	131992	125473	119170
130.0	1.59740E+12	132968	132979	125953	119162
137.0	1.63221E+12	134403	134420	126654	119152
143.0	1.66752E+12	135842	135866	127357	119143
151.0	1.72263E+12	138053	138093	128438	119130
155.5	1.76252E+12	139628	139682	129209	119123
158.0	1.78264E+12	140414	140477	129593	119118
160.0	1.80466E+12	141267	141342	130010	119112
162.5	1.82160E+12	141920	142004	130329	119108
165.0	1.85610E+12	143239	143343	130974	119102
167.0	1.87238E+12	143854	143970	131276	119100
169.0	1.89181E+12	144585	144715	131632	119093
170.5	1.90996E+12	145263	145407	131964	119090
173.0	1.94386E+12	146519	146692	132579	119085
176.0	1.97566E+12	147682	147887	133149	119080
182.0	1.99438E+12	148361	148586	133478	119070
189.0	2.00144E+12	148616	148850	133589	119042
198.0	2.00785E+12	148846	149087	133697	119032
230.0	1.99299E+12	148306	148535	133385	118940

8.23 PCT LI,RUN 19,118.5 KC XTALS,FRST DWN  
 MS= 4.6808 MC= 4.8352 RHO= 6.2690 L= 1.8980

T,DEGC	E,DYN/SQCM	FS0,CPS	FSF,CPS	FX,CPS	FC,CPS
43.0	1.34338E+12	121948	121948	120572	119240
76.0	1.40134E+12	124550	124551	121842	119220
94.0	1.44622E+12	126529	126529	122806	119202
107.0	1.48635E+12	128271	128273	123658	119192
123.0	1.55025E+12	130996	131001	124988	119172
136.0	1.61483E+12	133689	133702	126304	119155
158.0	1.77208E+12	140002	140061	129390	119117
161.0	1.80318E+12	141211	141285	129981	119110
164.0	1.83284E+12	142351	142442	130538	119102
168.0	1.87196E+12	143838	143954	131264	119092
171.0	1.90865E+12	145214	145358	131938	119086
173.5	1.94171E+12	146439	146611	132540	119085
177.0	2.00535E+12	148757	148994	133679	119082
178.0	2.01021E+12	148932	149175	133764	119080
180.5	2.01566E+12	149128	149377	133855	119070
185.5	2.01805E+12	149213	149465	133892	119060
194.0	2.01853E+12	149230	149483	133891	119042
200.0	2.01781E+12	149204	149457	133872	119030
203.5	2.01567E+12	149126	149377	133829	119020
208.0	2.01416E+12	149072	149321	133797	119010
212.0	2.01163E+12	148980	149228	133746	118998
218.0	2.00530E+12	148755	148996	133626	118980
225.0	2.00000E+12	148560	148795	133520	118960

LI-MG-NI ALLOY, RUN: 34, 118.5 KC XTALS, FRST UP  
 MS= 3.9474 MC= 4.8352 RHO= 5.6400 L= 1.9120

T, DEGC	E, DYN/SQCM	F50, CPS	FSF, CPS	FX, CPS	FC, CPS
28.0	8.14699E+11	99159	99390	110219	119248
60.0	8.80257E+11	103208	103311	112029	119230
105.5	9.27204E+11	105978	106030	113254	119194
127.5	1.00010E+12	110105	110119	115094	119167
140.0	1.05613E+12	113158	113162	116457	119150
154.0	1.20520E+12	120885	120885	119916	119125
157.0	1.23963E+12	122600	122599	120684	119120
161.0	1.29343E+12	125233	125231	121865	119115
165.0	1.33107E+12	127045	127041	122672	119102
169.5	1.37772E+12	129255	129248	123662	119096
173.0	1.40532E+12	130545	130536	124236	119085
182.0	1.44836E+12	132533	132520	125121	119070
197.0	1.47275E+12	133644	133631	125602	119035
205.5	1.47652E+12	133817	133802	125668	119015
213.5	1.47735E+12	133855	133840	125674	118995
222.0	1.47727E+12	133851	133836	125658	118969

LI-MG-NI ALLOY, RUN 34, 118.5 KC XTALS, FRST DWN  
 MS= 3.9474 MC= 4.8352 RHO= 5.6400 L= 1.9120

T, DEGC	E, DYN/SQCM	F50, CPS	FSF, CPS	FX, CPS	FC, CPS
40.0	7.98814E+11	98141	98416	109759	119244
57.0	8.13006E+11	99052	99286	110162	119232
72.0	8.29914E+11	100121	100313	110637	119222
95.0	8.69763E+11	102576	102693	111730	119203
120.0	9.42299E+11	106849	106890	113636	119177
127.0	9.77400E+11	108840	108863	114525	119166
153.0	1.16656E+12	118931	118931	119039	119127
157.0	1.22827E+12	122037	122037	120431	119120
164.0	1.30375E+12	125733	125730	122084	119105
176.0	1.42108E+12	131277	131266	124563	119082
182.0	1.44462E+12	132362	132349	125044	119070
184.5	1.45397E+12	132790	132776	125231	119060
192.0	1.46628E+12	133352	133337	125477	119048
200.0	1.47347E+12	133679	133664	125614	119030
212.0	1.47723E+12	133850	133834	125677	119005

PURE NIO, RIJN 16,92.5 KC XTALS, FRST UP  
 MS= 5.1881 MC= 6.3474 RHO= 6.7830 LF 1.9000

T, DEGC	E, DYN/SQCM	F <sub>0</sub> , CPS	F <sub>SF</sub> , CPS	F <sub>X</sub> , CPS	F <sub>C</sub> , CPS
26.5	8.61266E+11	93772	93772	93114	92576
189.0	9.27548E+11	97315	97314	94647	92466
192.0	9.31753E+11	97536	97534	94744	92462
226.0	1.03967E+12	103038	103027	97186	92403
234.0	1.10927E+12	106435	106420	98703	92383
241.0	1.21615E+12	111438	111429	100944	92367
244.0	1.28194E+12	114392	114403	102268	92358
246.0	1.51963E+12	124277	124518	106712	92355
248.0	2.11713E+12	144488	147021	115799	92350
250.0	2.14178E+12	145185	147874	116110	92345
261.0	2.11375E+12	144382	146904	115731	92313
266.0	2.11362E+12	144376	146899	115724	92305
270.0	2.13924E+12	145099	147787	116041	92290
272.0	2.15651E+12	145581	148382	116252	92280
292.0	2.03314E+12	142003	144075	114607	92215
296.0	2.02624E+12	141792	143830	114503	92198

PURE NIO,RUN 16,92.5 KC XTALS,SCND UP  
 MS= 5.1881 MC= 6.3474 RHO= 6.7830 L= 1.9000

T,DEGC	E,DYN/SQCM	F50,CPS	F5F,CPS	FX,CPS	FC,CPS
26.5	8.83704E+11	94986	94986	93655	92567
42.0	8.82530E+11	94923	94923	93631	92575
59.0	8.82102E+11	94900	94900	93619	92572
72.0	8.82400E+11	94916	94916	93624	92568
86.0	8.83611E+11	94981	94981	93650	92562
105.0	8.86861E+11	95156	95155	93723	92552
140.0	9.08089E+11	96288	96287	94217	92524
158.0	9.14485E+11	96627	96626	94360	92507
194.0	9.54645E+11	98728	98725	95278	92458
219.0	1.02009E+12	102062	102053	96747	92403
232.0	1.10345E+12	106156	106141	98575	92379
243.0	1.32038E+12	116076	116106	103027	92361
247.0	1.91596E+12	138410	139862	113067	92353
249.0	2.15669E+12	145604	148388	116300	92348
250.0	2.15780E+12	145635	148426	116312	92345
252.0	2.15624E+12	145589	148373	116289	92340
256.0	2.15163E+12	145458	148214	116225	92331
280.0	2.09673E+12	143878	146311	115472	92254
292.0	2.08564E+12	143548	145923	115302	92215
308.0	2.06658E+12	142978	145255	115014	92157

PURE NIO,RUN 16,92.5 KC XTALS,SCND DWN  
 MS= 5.1881 MC= 6.3474 RHO= 6.7830 L= 1.9000

T,DEGC	E,DYN/SQCM	FSO,CPS	FSF,CPS	FX,CPS	FC,CPS
26.5	8.91831E+11	95422	95422	93856	92576
46.0	8.93078E+11	95489	95488	93886	92576
51.0	8.94174E+11	95547	95547	93914	92579
66.0	8.95586E+11	95623	95622	93943	92570
90.0	9.03139E+11	96025	96025	94118	92559
108.0	9.09315E+11	96353	96352	94260	92549
136.0	9.25174E+11	97191	97189	94625	92528
156.0	9.45390E+11	98248	98245	95090	92509
172.0	9.63558E+11	99188	99185	95501	92487
187.0	9.86618E+11	100370	100364	96022	92468
210.0	1.04075E+12	103091	103081	97225	92430
234.0	1.17748E+12	109657	109643	100152	92383
240.0	1.25331E+12	113118	113119	101701	92369
242.0	1.31653E+12	115909	115937	102953	92363
245.0	1.50317E+12	123666	123882	106440	92360
249.0	2.17478E+12	146107	149009	116526	92348
250.0	2.17663E+12	146157	149073	116547	92345
252.0	2.17553E+12	146125	149035	116530	92340
254.0	2.16761E+12	145905	148763	116428	92335
258.0	2.16241E+12	145759	148585	116359	92329
276.0	2.13365E+12	144937	147593	115958	92272
268.0	2.14649E+12	145304	148037	116136	92295
284.0	2.11860E+12	144504	147072	115750	92248
291.0	2.06799E+12	143034	145305	115072	92217
302.0	2.06758E+12	143011	145290	115037	92172

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Table 1  
IMPURITY CONCENTRATION OF STARTING MATERIALS  
 (parts per million)

Material Identification	NiO Johnson-Matthey Specpure Grade I	NiO Atomergic Sub-Micron	NiO Baker Reagent	Fisher MgO		Fisher Li <sub>2</sub> CO <sub>3</sub>
	Lot. No. S6616	Lot No. C1435	Lot. No. 2796	"Electronic Grade"		Lot. No. 764296
Ag	<1					
Al	<1	20		150	75	
B				10	40	3
Ca	<1			50	1000	150
Cl			50	27	180	285
Co		200	2000			10
Cr		10			10	5
Cu	<1	150	200	3	1	
F					140	110
Fe	10	200	100	100	200	85
K						10
Mg	<1	30				100
Mn					70	2
N			50			100
Na					180	100
Ni	-	-	-		5	10
P					7	130
Pb			50			10
S			100	50	50	510
Si	3	300		300	1000	2400
Ti					50	10
Zn						5
Other, as Insolubles (in HCl)			2000			
Approx. Particle Size, Micron	2-5	0.015	0.1	.05	.05	-
Source of Analysis, Note No.	1	1	1	2	2	3

- Notes: 1. Supplier Analysis  
 2. Jet Propulsion Lab. Tech. Rept. No. 32-736, M.H. Leipold, T. H. Nielsen  
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Table 2

Survey of Stoichiometry Range ReportedFor Pure Nickel Oxide

<u>Stoichiometry Range</u>	<u>Nature of Sample</u>	<u>Year (and Reference)</u>	
$\text{NiO}_{1.05}$ (Max.)	Powder	1931	(46)
$\text{NiO}_{1.025}$ (Max.)	Powder Calcined from $\text{NiCO}_3$	1934	(47)
$\text{NiO}_{1.0005}$ - $\text{NiO}_{1.005}$	Oxidized Nickel Foil	1934	(48)
$\text{NiO}$ - $\text{NiO}_{1.006}$	Porous Sintered Specimen	1936	(49)
$\text{NiO}$ - $\text{NiO}_{1.07}$	Powder, 300 Atm. Pressure	1940	(35)
$\text{NiO}_{1.02}$ - $\text{NiO}_{1.2}$	Powder, Calcined $\text{Ni}(\text{NO}_3)_2$	1954	(36)
$\text{NiO}_{1.0007}$ - $\text{NiO}_{1.0196}$	Powder, Calcined $\text{Ni}(\text{NO}_3)_2$	1962	(50)
$\text{NiO}_{1.00098}$	"Commercial" Nickel Oxide	1964	(51)
$\text{NiO}_{1.00013}$ - $\text{NiO}_{1.0224}$	Powder, Calcined $\text{NiCO}_3$	1965	(52)
$\text{NiO}$ - $\text{NiO}_{1.00016}$	Thermal Dehydra- tion $\text{Ni}(\text{OH})_2$	1966	(53)
$\text{NiO}_{1.000} \pm 0.002$	"Specpure" Nickel Oxide	1968	(54)

Table 3

Calculated Values of [VNi] at 25°C and 1200°C

and  $P_{O_2} = 0.209$  atm, (vacancies per ion pair)

<u>Source</u>	<u>[VNi] at 25°C</u>	<u>[VNi] at 1200°C</u>
Mitoff (67)	$3.6 \times 10^{-11}$	$1.83 \times 10^{-4}$
Price (69, 70)	$3.6 \times 10^{-11}$	$1.83 \times 10^{-4}$
Eror (68)	-	$2.47 \times 10^{-4}$
Socket, Schmalzried (71)	-	$3.1 \times 10^{-4}$
Ormont (72)	$2 \times 10^{-11}$	-

Table 4

Ni<sup>+3</sup> and Li<sup>+1</sup> Chemical Analyses

Description	pH	Powder Analysis, at% Ni <sup>+3</sup>	Powder Analysis, at% Li <sup>+1</sup>	Sample Analysis, at% Ni <sup>+3</sup>	Sample Analysis, at% Li <sup>+1</sup>
"Blank"	-	0	-	-	-
99.999% NiO, as rec'd.	-	0	-	-	-
99.999% NiO, 1000°C airfire	-	0	-	-	-
5%Li(Nom), unwashed	Basic	5.2413 ±0.297	5.31	5.0731 ±0.0491	5.29
0.1%Li(Nom), washed	Neutral	0.1180 ±0.0003	0.12	5.3364	5.63
0.5%Li(Nom), washed	Neutral	0.4920 ±0.0003		0.117	
1%Li(Nom), washed	Neutral	0.9449 ±0.0041			
2%Li(Nom), washed	Neutral	1.9586 ±0.0452			
5%Li(Nom), washed	Neutral	4.9684 ±0.0010	4.98		
20%Li(Nom), washed	Neutral	6.8389 ±0.0205			
20%Li(Nom), washed	Neutral	6.9585 ±0.1211			
10%Li(Nom), washed	Neutral	8.2320 ±0.1337	8.277	8.2230 ±0.1345	
30%Li(Nom), washed	Neutral	9.9745 ±0.0292			
25%Li(Nom), washed	Neutral	12.278 ±0.300			

Table 5

Periodic Table of the Elements Demonstrating  
the Extent of Solubility and Compound Formation  
in NiO-M<sub>x</sub>O<sub>y</sub> Phase Systems.

PERIOD	GROUP IA	IIA	IIIB	IVB	VB	VIB	VII B	VIII B	IB	IIB	IIIA	IVA	VA
1	H												
2	Li   -17 28-30% LiNiO <sub>2</sub> Li <sub>2</sub> NiO <sub>3</sub>	Be   -57 < 0.01%									Al   -31 ~1% NiAl <sub>2</sub> O <sub>4</sub>	Si   4 -43	P   5 -53 0 Ni <sub>3</sub> (PO <sub>4</sub> ) <sub>2</sub>
3	Na   +32 ~1% NaNiO <sub>2</sub>	Mg   2 -10 100% SOLID SOLUTION											
4	K   +85 <1% KNiO <sub>2</sub> K <sub>2</sub> NiO <sub>3</sub> K <sub>2</sub> Ni <sub>2</sub> O <sub>5</sub>	Ca   +38 3-5% EUTECTIC SYSTEM	Sc   +11	Ti   4 -6 <1% NiTiO <sub>3</sub>	V   5 -18 0 Ni(VO <sub>3</sub> ) <sub>2</sub> Ni <sub>2</sub> V <sub>2</sub> O <sub>7</sub> Ni <sub>3</sub> (VO <sub>4</sub> ) <sub>2</sub>	Cr   3 -4 0.1-1% NiCr <sub>2</sub> O <sub>4</sub>	Mn   2+11 3-9 100% NiMn <sub>2</sub> O <sub>4</sub> NiMnO <sub>3</sub>	Co   2+3 3-13 <1% NiFe <sub>2</sub> O <sub>4</sub> NiCo <sub>2</sub> O <sub>4</sub>	Ni   2,0,7,2 3,0,6,2	Zn   2 +3 28-35% 900°C 40% 1100°C	Ga   3 -14 0-1% NiGa <sub>2</sub> O <sub>4</sub>	Ge   4 -27	As   5 -35
5	Rb   +105	Sr   2 +57	Y   3 +29	Zr   4 +11 ~1%	Nb   5 -3 NiNb <sub>2</sub> O <sub>6</sub> Ni <sub>4</sub> Nb <sub>2</sub> O <sub>9</sub>	Mo   6 -14 NiMoO <sub>4</sub>	Tc	Ru   4 -11	Pd   2 +20	Cd   2 +35 0% NiIn <sub>2</sub> O <sub>4</sub>	In   3 +13	Sn   4 -2	Sb   5 -14 NiSb <sub>2</sub> O <sub>6</sub>
6	Cs   +115 Cs <sub>3</sub> NiO <sub>5</sub>	Ba   2 +88 <3% NiBaO <sub>2</sub>	La   3 +60 LaNiO <sub>3</sub> La <sub>2</sub> NiO <sub>4</sub>	Hf   4 +11 ~1% NiHfO <sub>4</sub>	Ta   5 +1 ~1% NiTa <sub>2</sub> O <sub>6</sub>	W   6 -6 0.75-1.5% NiWO <sub>4</sub>	Re	Os   4 -7	Pt	Hg   2 +53	Tl   3 +32	Pb   4 +12	Bi   3 +67 0
7	Fr   +145	Ra   2 +95 Ac   3 +64											

KEY

Li   -17
28-30% LiNiO <sub>2</sub> Li <sub>2</sub> Ni <sub>3</sub> O <sub>4</sub>

SYMBOL → COMMON VALENCE  
 → RADIUS RATIO COMPARED TO Ni<sup>+2</sup>  
 → MAXIMUM SOLUBILITY IN NiO

OTHER COMPOUNDS →

R<sub>Ni</sub>

Ce   4 +40	Pr   3 +52	Nd   3 +50	Pm   3 +47	Sm   3 +45	Eu   3 +43	Gd   3 +42
~1%		0	0	0	0	0

Table 6

Final Grain Size Range for Pressure SinteredLithium-Nickel Oxide Alloys

<u>Atomic Percent Lithium</u>	<u>Run No.</u>	<u>Grain Size Range, microns</u>
Pure NiO	16	1-2
Pure NiO	16, airfired	15-20
.12	22	3-4
.49	27	10-15
.95	29	15-20
.95	31	15-20
1.96	25	40
4.97	26	35-50
6.84	30	30-60
8.23	19	8-10

Table 7.

Experimental Values of Néel Temperature  
for Nickel Oxide

<u>Néel Temperature</u>	<u>Measurement Method</u>	<u>Author</u>	<u>Reference No.</u>
525	Dilatometric	Foex	(203)
525	Magnetic Susceptibility	Perakis	(50)
604	" "	Perakis and coworkers	(107)
623	" "	Perakis and coworkers	(108)
607	" "	Foex and coworkers	(204)
647	" "	LaBlanchetais	(205)
647	" "	Trombe	(206)
523	" "	Richardson and coworkers	(207)
523(640)	" "	Singer	(208)
523	" "	Blasse	(209)
523	Magnetic Torque	Kondoh and coworkers	(210)
533	Magnetic Scattering	Roth	(211)
520	Mossbauer Effect	Bhide and coworkers	(212)
518	Specific Heat	Shimomura and coworkers	(213)
523	" "	Tomlinson and coworkers	(214)
525	" "	King and coworkers	(215)
513	" "	Maksimov	(216)
507	Modulus	Street and Lewis	(202)
510	Modulus	Belov and Levitin	(217)
524	Magnetostriction	Belov and Levitin	(218)

Table 8  
Resonant Sphere Method Data Analysis - Pure NiO Run #12

Intensity	f, Observed Frequency cps	f <sub>r</sub> , Reduced Frequency (*)	Mode Identification (**)	A <sub>n</sub> , (#) Shear Wave Mode Constant	v <sub>s</sub> , Shear Velocity cm/sec	R, ohms	C, microfarads	Q <sup>-1</sup> , Inverse Acoustic Loss (##)
Weak	19,830	Background and Equipment Resonance	-----	-----	-----	-----	-----	-----
Weak	43,240		-----	-----	-----	-----	-----	-----
Weak	136,000		-----	-----	-----	-----	-----	-----
Weak	141,000		-----	-----	-----	-----	-----	-----
Very weak	204,000	2.501	-----	-----	-----	-----	-----	-----
Weak	256,000		-----	-----	-----	-----	-----	-----
Very strong	274,500		1T <sub>2</sub>	2.501	2.255x10 <sup>5</sup>	22,000	.01	2.74x10 <sup>-3</sup>
Very weak	279,000	2.540	Unidentified } Split Peaks	-----	-----	-----	-----	-----
Weak	290,000	2.640		-----	-----	-----	-----	-----
Medium	307,000	2.796		1S <sub>2</sub>	-----	-----	-----	-----
Very strong	407,870	3.715	2S <sub>1</sub>	-----	-----	18,000	.01	2.17x10 <sup>-3</sup>
Medium	419,460	3.820	1T <sub>3</sub>	3.865	2.225x10 <sup>5</sup>	-----	-----	-----
Medium	543,830	4.953	1T <sub>4</sub>	5.095	2.200x10 <sup>5</sup>	-----	-----	-----
Medium	679,840	6.193	1S <sub>5</sub>	-----	-----	-----	-----	-----
Medium	684,840	6.238	1T <sub>5</sub>	6.266	2.250x10 <sup>5</sup>	-----	-----	-----
Weak	776,500	7.073	2T <sub>2</sub>	7.136	2.240x10 <sup>5</sup>	-----	-----	-----
Weak	805,000	7.333	3S <sub>1</sub>	-----	-----	-----	-----	-----
Very strong	856,200	7.798	1S <sub>0</sub>	-----	-----	31,000	.01	5.96x10 <sup>-4</sup>
					Average Shear Velocity =	2.231x10 <sup>5</sup>		

(\*) based on the tentative assumption that the peak at f = 274,000 = f<sub>n</sub> is a T<sub>2</sub> shear mode with A<sub>n</sub> = 2.501 and  
 $f_r = f \left( \frac{A_n}{f_n} \right) = f \left[ \frac{2.501}{274,000} \right]$

(\*\*) based on match between experimental reduced frequencies and the curve of f<sub>r</sub> versus Poisson's ratio given by Fraser and LeCraw(225) at σ=0.416

(#) from Sato and Usami (229)

(##) from Q = 2πf<sub>n</sub>(RC)

(###) from v<sub>s</sub> = πd<sup>1/2</sup>f<sub>n</sub> where d = 0.6549 cm.

Table 9  
Compilation of Experimental Data and Elastic Moduli for Pure and Doped Nickel Oxide Using  
 Different Measurement Techniques

Sample Identity and Measurement Method							
	Pure NiO Run 12	Pure NiO Run 12	Pure NiO Run 12	Pure NiO Run 12	8.23% Li Alloy Run 19	8.23% Li Alloy Run 19	8.23% Li Alloy Run 19
	Pulse Trans- mission Longitudinal Wave Measurement	Pulse Trans- mission Shear Wave Measurement	Resonant Sphere Method (#)	Composite Oscillation Method	Pulse Trans- mission Longitudinal Wave Measurement	Pulse Trans- mission Shear Wave Measurement	Composite Oscillator Method
<u>Specimen</u>							
<u>Length, cm</u>	0.6934	0.6934	-	1.90	0.6797	0.6797	1.898
<u>Specimen</u>							
<u>Diameter, cm</u>	-	-	0.6549	-	-	-	-
<u>Matched timing</u>							
<u>frequency, cps</u>	2,641,000	1,129,789	-	-	2,719,236	2,595,700	-
<u>Integer frequency</u>							
<u>number</u>	3	4	-	-	3	6	-
<u>Resonant fre-</u>							
<u>quency, cps</u>	-	-	-	98,600(*)	-	-	121,019(**)
<u>Velocity,</u>							
<u>cm/ sec</u>	$6.137 \times 10^5 (v_L)$	$1.959 \times 10^5 (v_S)$	$2.231 \times 10^5$	-	$6.161 \times 10^5 (v_L)$	$2.94 \times 10^5 (v_S)$	-
<u>Shear modulus,</u>							
<u>d/cm<sup>2</sup></u>		$2.61 \times 10^{11}$	$3.38 \times 10^{11}$	-	$5.41 \times 10^{11}$		-
<u>Young's modulus,</u>							
<u>d/cm<sup>2</sup></u>		$7.50 \times 10^{11}$	$9.58 \times 10^{11}$	$9.56 \times 10^{11}$	$14.66 \times 10^{11}$		$13.23 \times 10^{11}$
<u>Bulk modulus,</u>							
<u>d/cm<sup>2</sup></u>		$22.0 \times 10^{11}$	$19.0 \times 10^{11}$	-	$16.62 \times 10^{11}$		-
<u>Poisson's ratio</u>	0.443		0.416	-	0.35		-
<u>Density, g/cm<sup>3</sup></u>	6.801		6.801	6.801	6.269		6.269

(\*) Measurement was made using quartz crystals with an average frequency of 92,550 cps, a total crystal mass of 6.34 grams, and a specimen mass of 5.26 grams. "Silastic" cement was used.

(\*\*) Measurement was made using quartz crystals with an average frequency of 119,250 cps, a total crystal mass of 4.84 grams, and a specimen mass of 4.68 grams. "GA-60" cement was used.

(#) See Table 8 for Resonant Sphere Data Analysis.

Table 10

Experimental and Derived Values of Mean Sound Velocity and  
Bulk Modulus for Pure Nickel Oxide at Room Temperature

<u>Source</u>	<u>K, dyne/cm<sup>2</sup></u>	<u>v<sub>m</sub>, cm/sec</u>
Sphere Resonance	19.0 X 10 <sup>11</sup>	2.55 X 10 <sup>5</sup>
Pulse Transmission	22.0 X 10 <sup>11</sup>	2.2 X 10 <sup>5</sup>
Compressibility Data	18.5 X 10 <sup>11</sup>	2.49 X 10 <sup>5</sup>
Szigeti Relation	20.2 X 10 <sup>11</sup>	2.59 X 10 <sup>5</sup>
Debye Analysis	25.0 X 10 <sup>11</sup>	2.9 X 10 <sup>5</sup>

Table II  
 Comparison of Modulus Values Obtained for Pure Nickel  
 Oxide Using Equation (A3.3) and Equation (A3.2)

T, °C	fs(o), cps		Equation (A3.3)		Equation (A3.2)	
	f <sub>x</sub> , cps	fs(o), cps	C <sub>1</sub> (*)	fs(f)cps E, dyne/cm <sup>2</sup>	C <sub>2</sub> (#)	fs(f), cps E, dyne/cm <sup>2</sup>
26	107,710	96,950	1.0	97,050 9.2 X 10 <sup>11</sup>	0.871	95,631 8.96 X 10 <sup>11</sup>
250.5	138,809	157,381	1.0	158,281 25.5 X 10 <sup>11</sup>	0.833	161,781 25.6 X 10 <sup>11</sup>

Note: (\*) C<sub>1</sub> = 1.0

$$C_2 = 1 - \frac{M_C^2 f_C^2}{m_S^2 f_S^2} \tan^2 \pi \frac{f_x}{f_C}$$

Figure 1

Vacuum Pressure Sintering Furnace. The Water-Cooled Base and the Induction Heating Coil can be seen in the Foreground. A Similar System is Shown Inside the Chamber. The  $1\frac{1}{4}$  Inch Diameter "T.Z.M." Plungers are Attached to the Upper and Lower Rams.

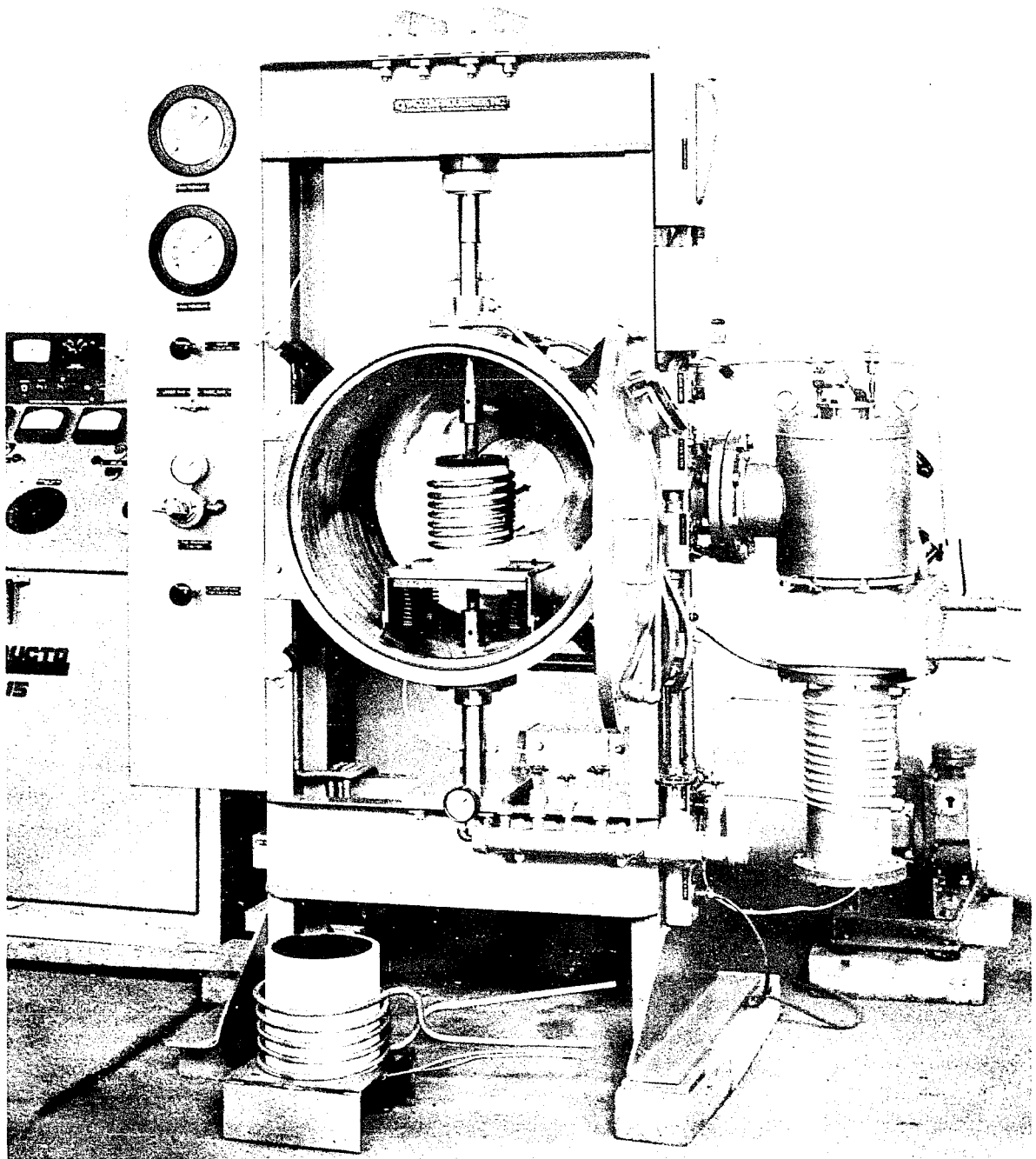


Figure 2

Schematic Drawing of Pressure-Sintering Die System. Graphite Susceptors Extend Over the Entire Length of the Silica Liner for Uniform Heating.

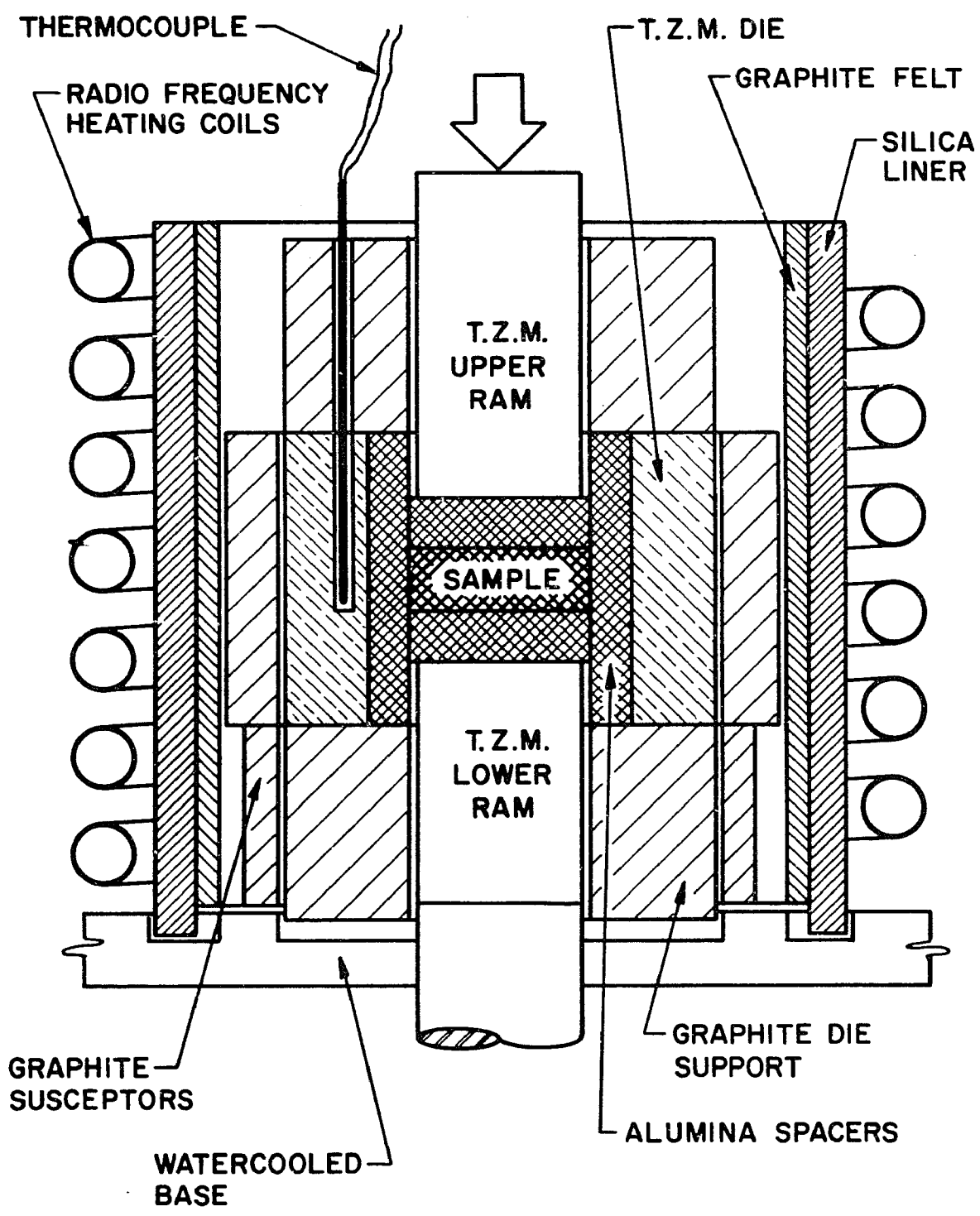


Figure 3

Chemical Apparatus for the Dissolution of  
Powdered Samples in Hydrochloric Acid for  
the Iodometric Titration Analysis of  $\text{Ni}^{+3}$

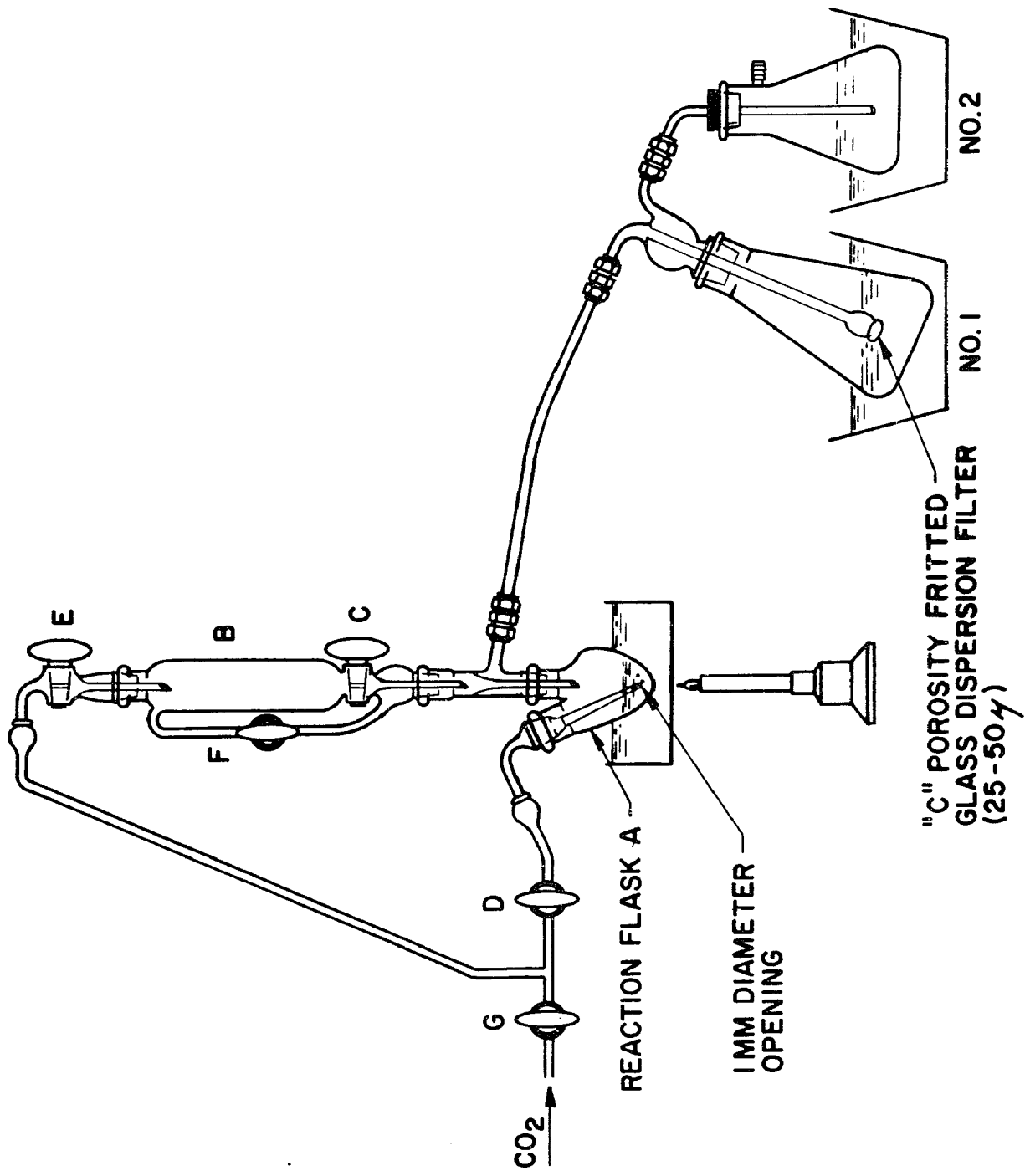


Figure 4

Schematic Representation of the Composite  
Oscillator Method for the Determination of  
Young's Modulus.

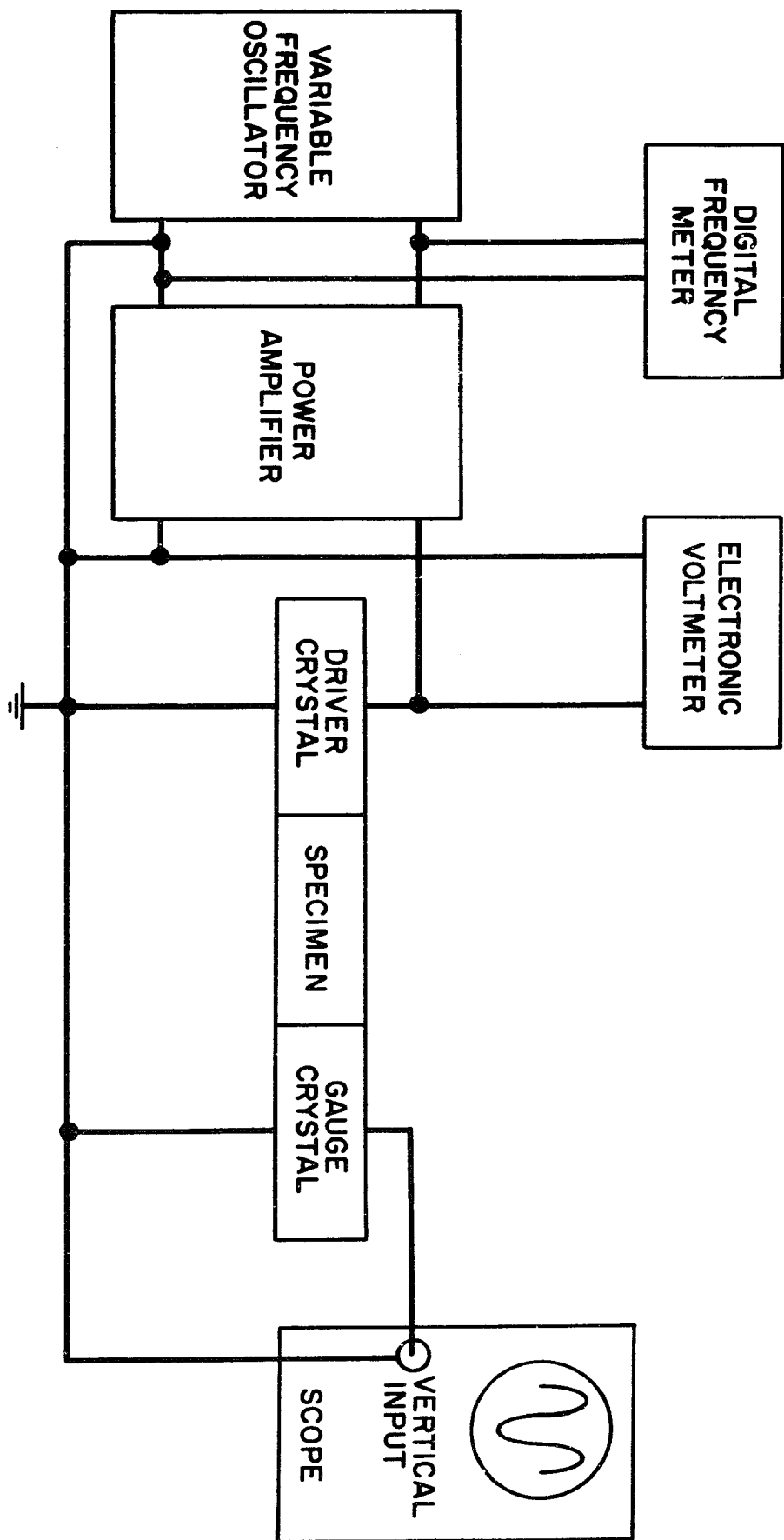
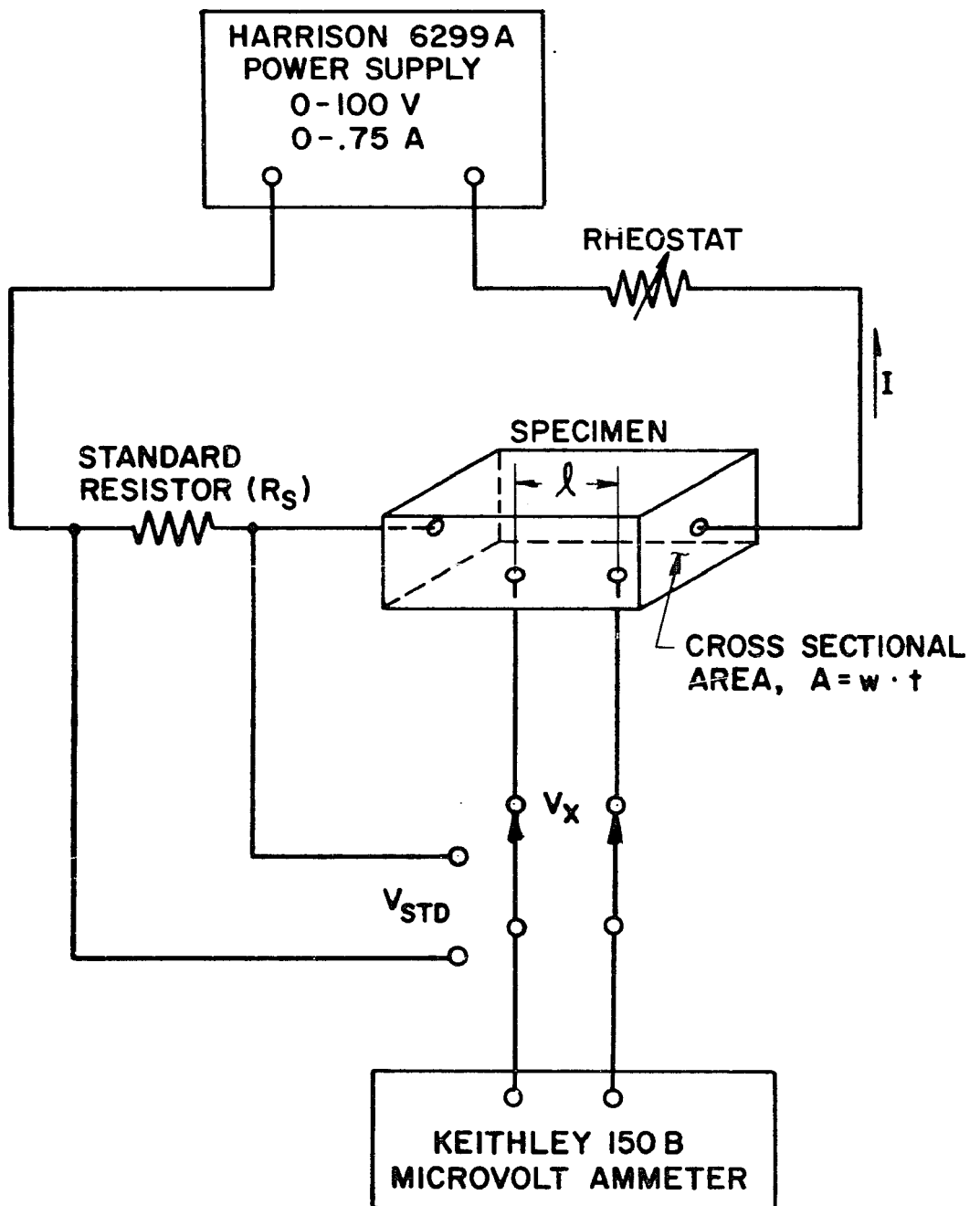


Figure 5

Schematic Representation of the Equipment  
Used for the Four Point Resistivity  
Measurements.



$$\rho = \frac{wt}{l} \cdot \frac{V_X}{V_{STD}} \cdot R_{STD}$$

Figure 6

Phase Diagram for the Ni-O System (After  
Bogatskii (29) ).

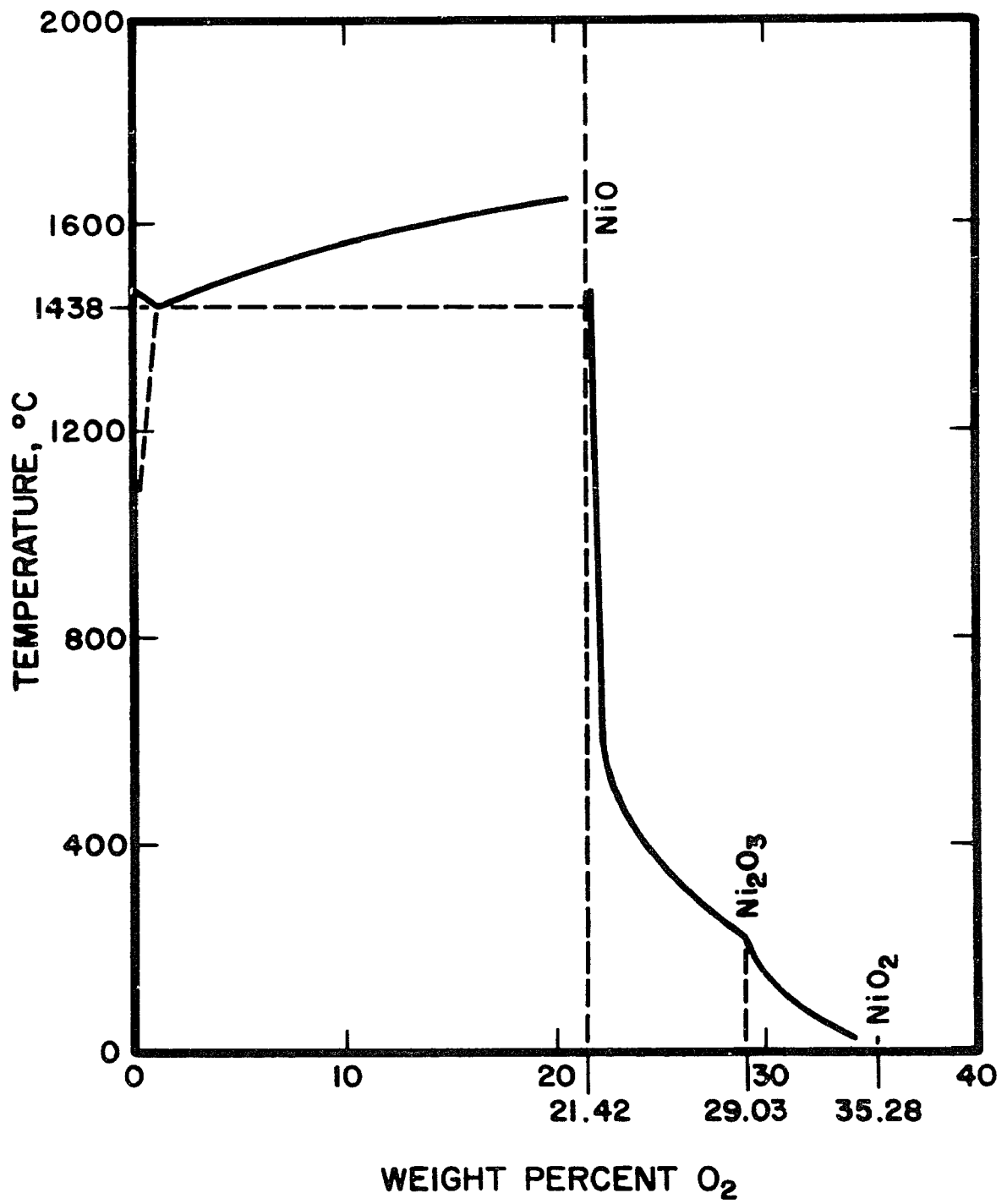


Figure 7

Standard Free Energy of Formation (Kilocalories per Half Mole Oxygen) as a Function of Temperature. The Upper Shaded Area is the Stable Phase Field for Pure NiO and the Cross-Hatched Area is the Stable Phase Field for Pure FeO.

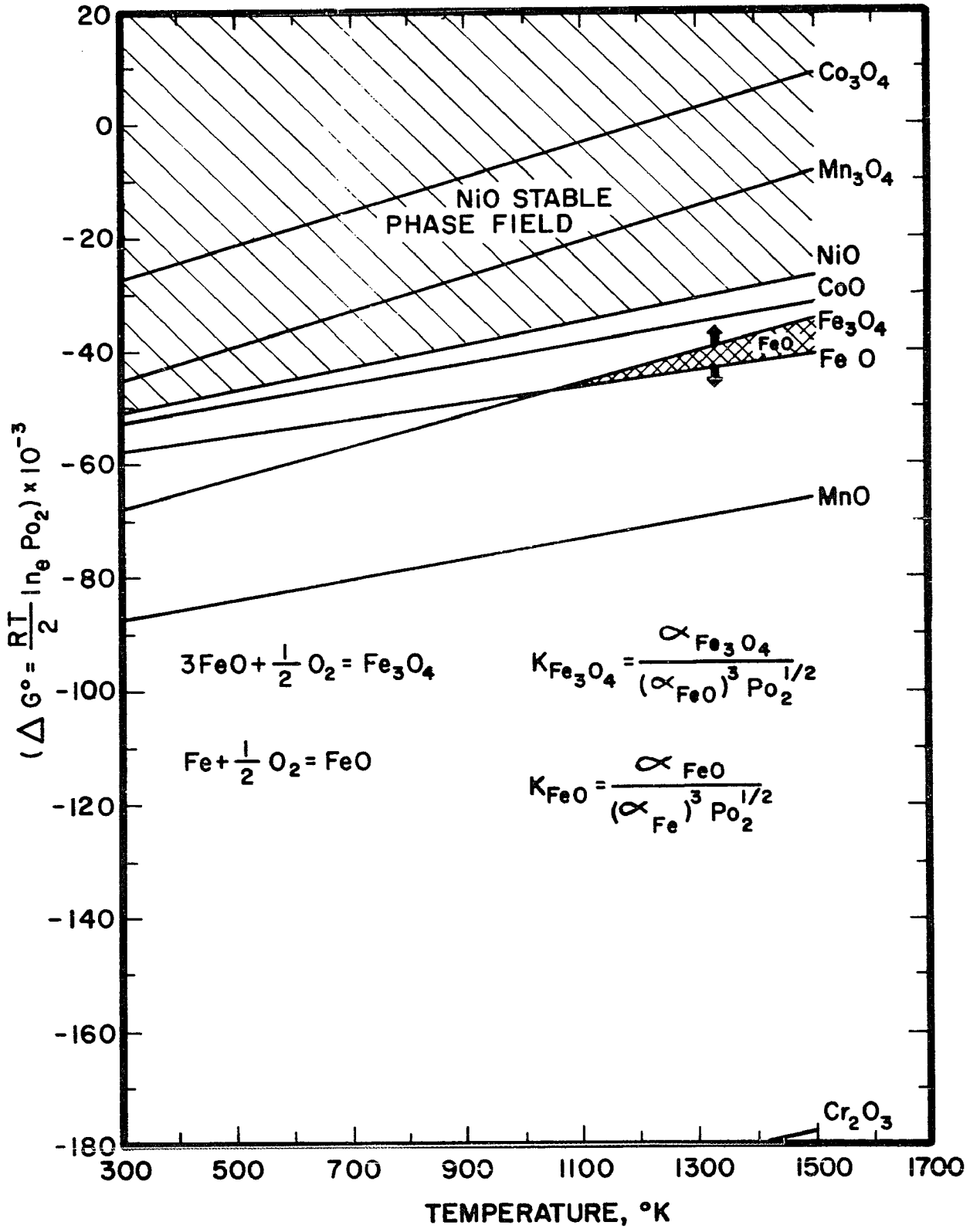


Figure 8

Lattice Parameter (in Terms of Unit Cell  
Volume) as a Function of Mole Percent Lithium  
in Nickel Oxide.

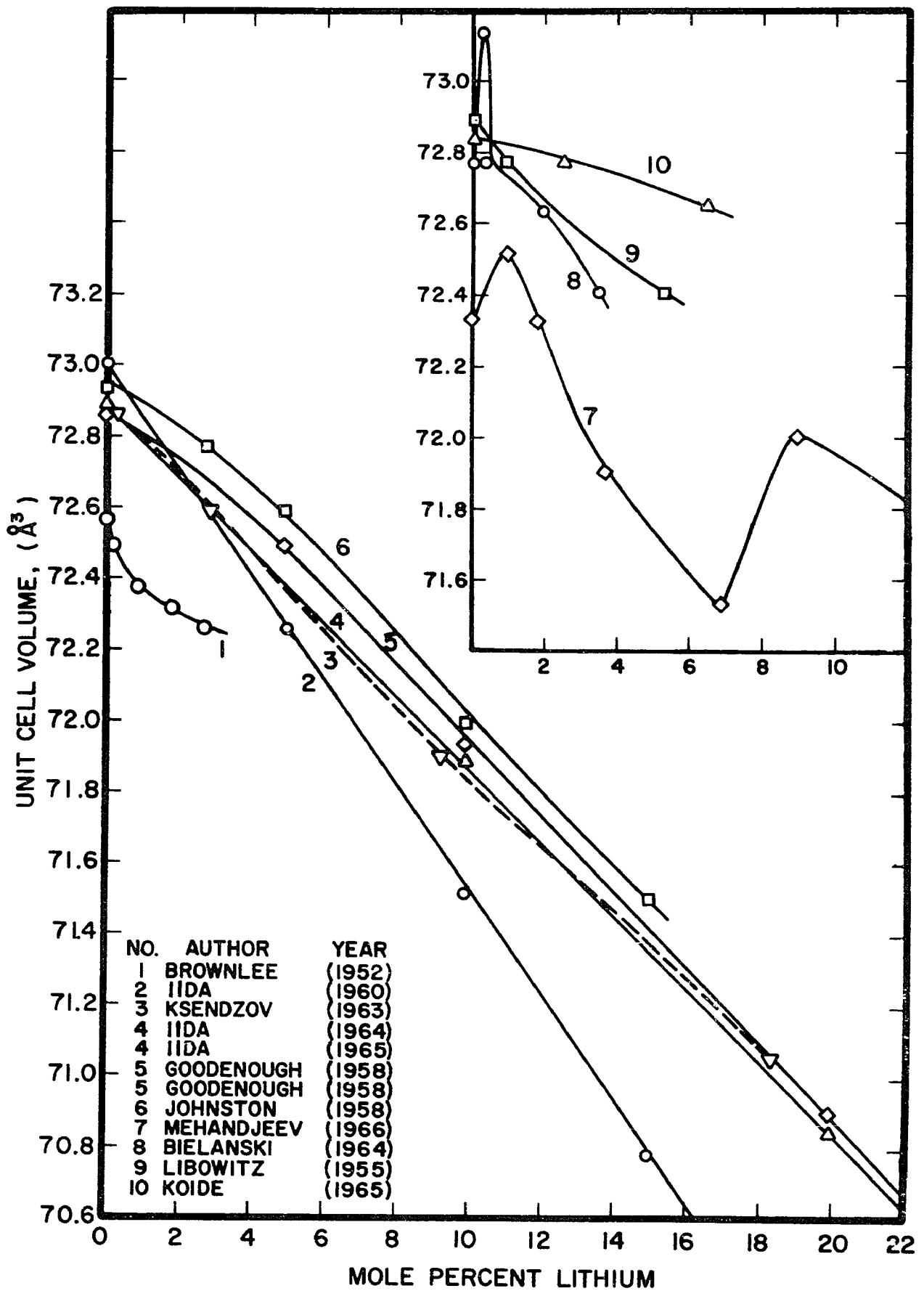


Figure 9

A P-T Diagram Showing Published Data on the Ni/NiO Phase Boundary. The Vertical Line Between the Two Open Circles Represents the Ambient Pressure Range During Sintering in the Present Investigation.

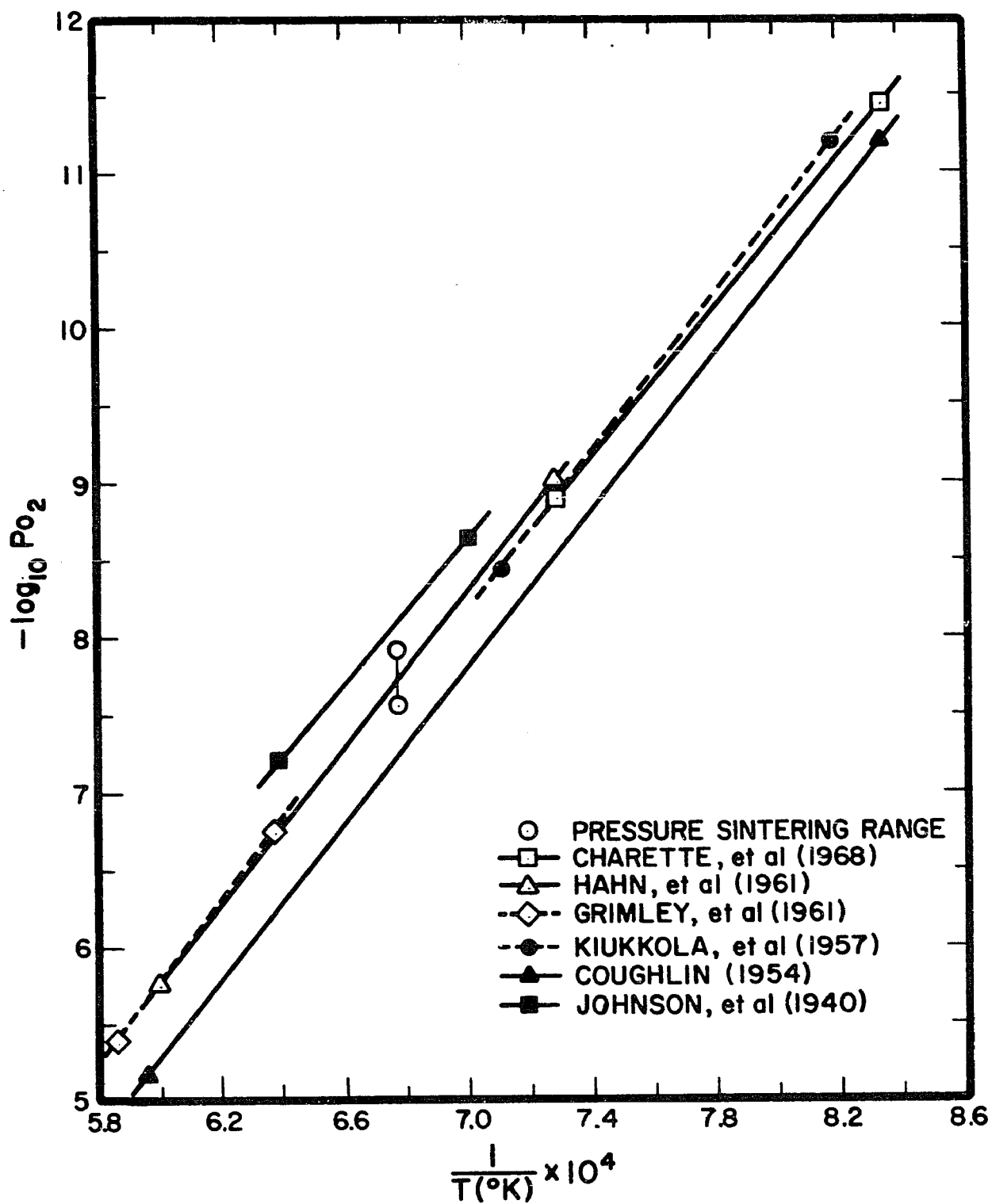


Figure 10

Relative Density as a Function of Atomic  
Percent Lithium for Specimens Pressure-Sintered  
at 1100°C for 90 Minutes. The Pure Nickel Oxide  
Sample was Fired at 1350°C for 24 Hours After  
Vacuum Pressure-Sintering.

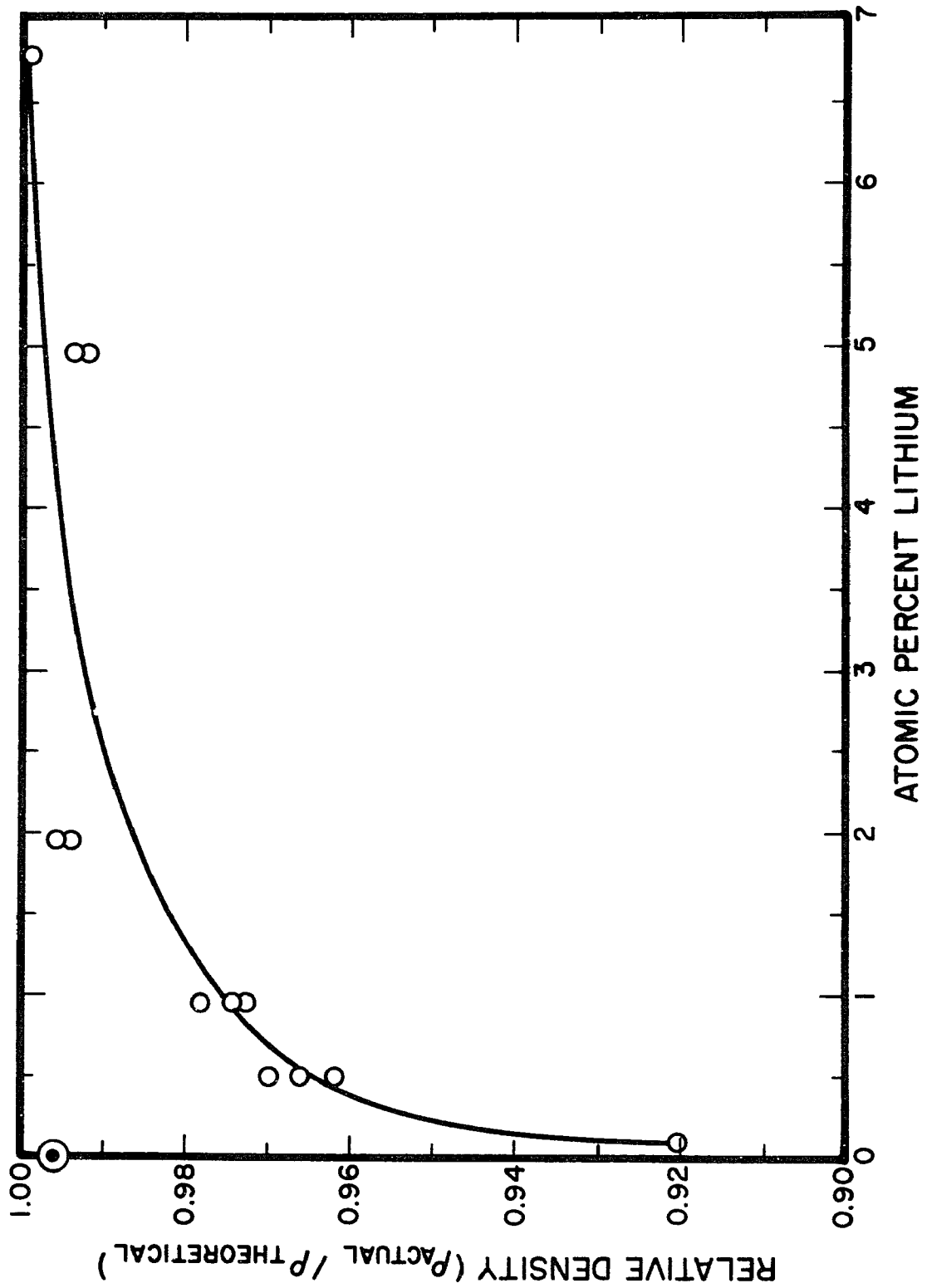


Figure 11

Electron Photomicrographs of Representative  
Pure- and Alloy-Starting Powders.



A. STARTING POWDER. PURE NICKEL OXIDE.  
2300X. ONE INCH EQUALS  $11\mu$ .



B. STARTING ALLOY POWDER. 0.12 ATOMIC PERCENT  
LITHIUM ALLOY. 2357X. ONE INCH EQUALS  $10\mu$ .



C. STARTING ALLOY POWDER. 1.96 ATOMIC PERCENT LITHIUM ALLOY. 2357X. ONE INCH EQUALS 10 $\mu$ .



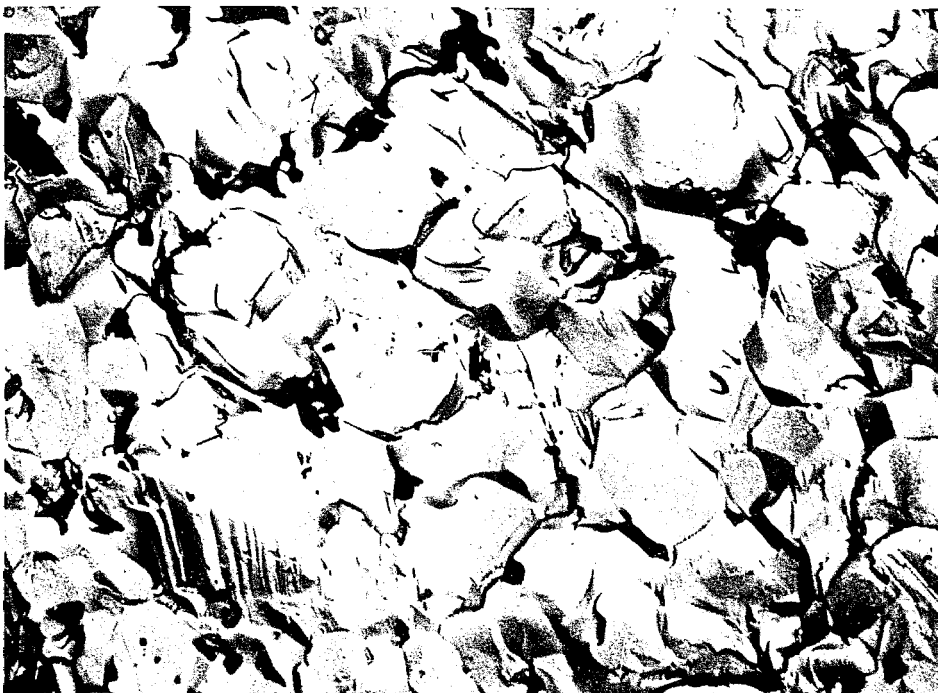
D. STARTING ALLOY POWDER. 8.23 ATOMIC PERCENT LITHIUM ALLOY. 2357X. ONE INCH EQUALS 10 $\mu$ .

Figure 12

Carbon-Chrome Electron Microscope Replicas  
of Representative Pure and Alloy Pressure-  
Sintered Samples.



A. CARBON-CHROME REPLICA OF PURE NICKEL OXIDE  
AFTER 1350°C AIR FIRE. 5100X. ONE INCH EQUALS 5.5 $\mu$ .



B. CARBON-CHROME REPLICA OF 0.12 ATOMIC PERCENT  
LITHIUM ALLOY. 3674X. ONE INCH EQUALS 7.1 $\mu$ .



C. CARBON-CHROME REPLICA OF 1.96 ATOMIC PERCENT LITHIUM ALLOY. 2839 X. ONE INCH EQUALS 10 $\mu$ .



D. CARBON-CHROME REPLICA OF 8.23 ATOMIC PERCENT LITHIUM ALLOY. 2839 X. ONE INCH EQUALS 10 $\mu$ .

Figure 13

Photomicrographs Showing Microprobe Trace (A) Before Etching and Same Area (B) After Etching of Pure Nickel Oxide Specimen. These Photographs are the Mirror Image of the Microprobe Scans Shown in Figures 14, 15 and 16. The Pore at the Right-Center Position in Each Photograph (Left-Center Position in Each Probe Scan) may be Used as a Reference.



A



B

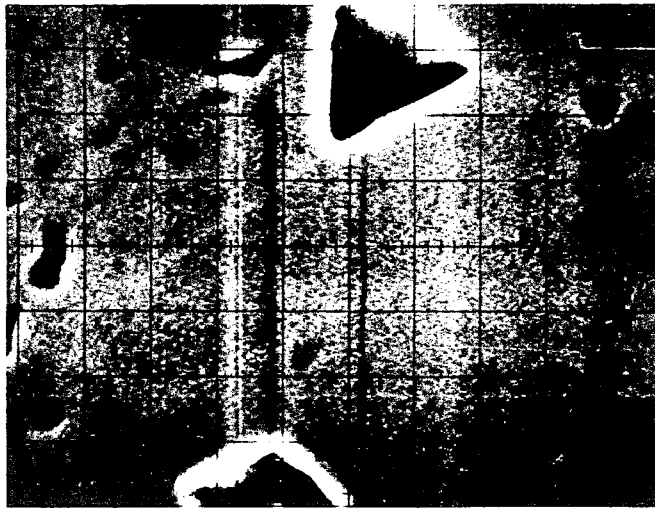
PHOTOMICROGRAPHS OF PURE NICKEL OXIDE SPECIMEN. 1000X.

A. SHOWING TRACE FROM MICROPROBE SCAN BEFORE ETCHING.

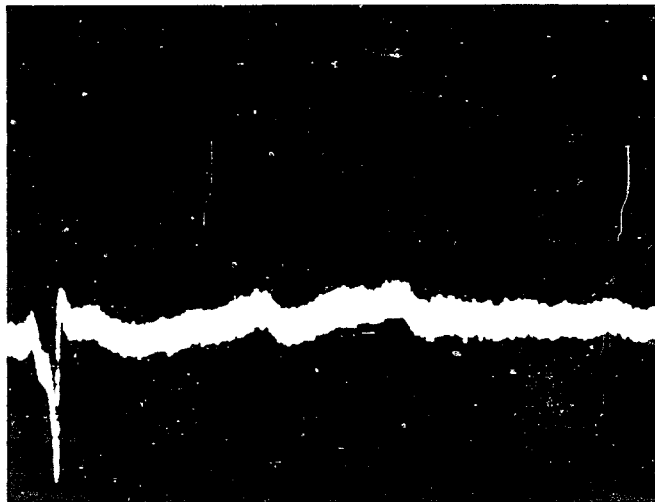
B. SAME AREA ETCHED FOR 10 MINUTES IN BOILING CONCENTRATED HCl. NOTE POSITION OF GRAIN BOUNDARIES.

Figure 14

Electron Microprobe Specimen Current Image (A)  
and Line Scan (B) for Pure Nickel Oxide.



A



B

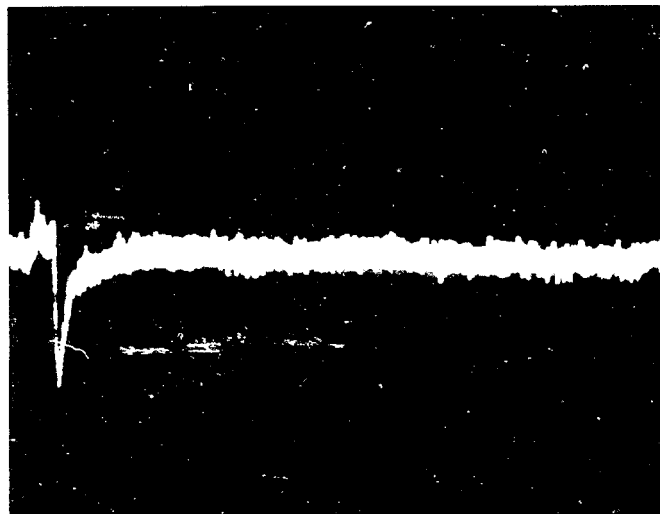
SPECIMEN CURRENT IMAGE (A) AND LINE SCAN (B) AT 1000X. PURE NICKEL OXIDE. PEAK HEIGHT IS  $0.0004\mu\text{AMPS}$ . ABOVE BASE LINE. BASE LINE CURRENT IS  $0.01\mu\text{AMPS}$ .

Figure 15

Electron Microprobe Secondary Electron Image (A)  
and Line Scan (B) for Pure Nickel Oxide.



A

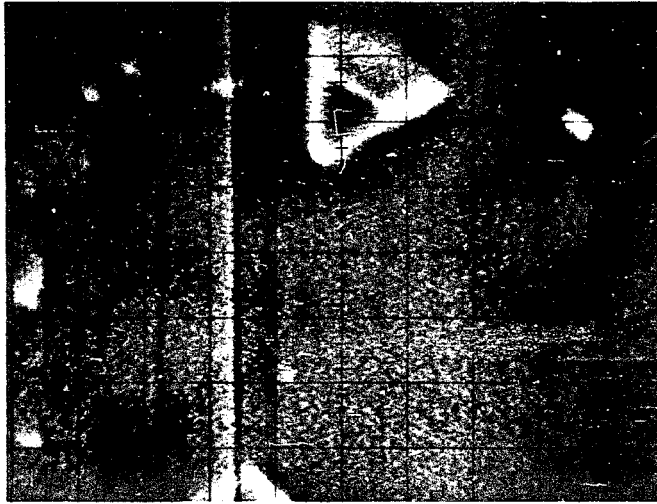


B

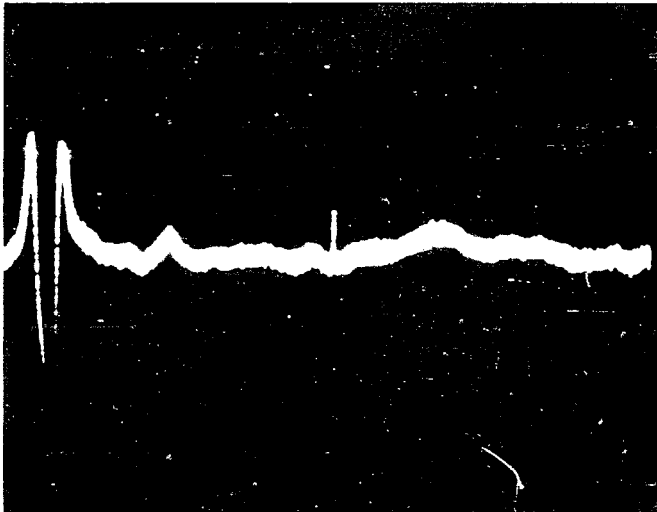
SECONDARY ELECTRON IMAGE (A) AND LINE SCAN (B) AT  
1000X. PURE NICKEL OXIDE.

Figure 16

Electron Microprobe Back Scattered Electron Image (A) and Line Scan (B) for Pure Nickel Oxide. The Line Scan (B) is Flipped 180° on the Horizontal Axis so That the Trace at the Pore Conforms With Figures 14 and 15.



A

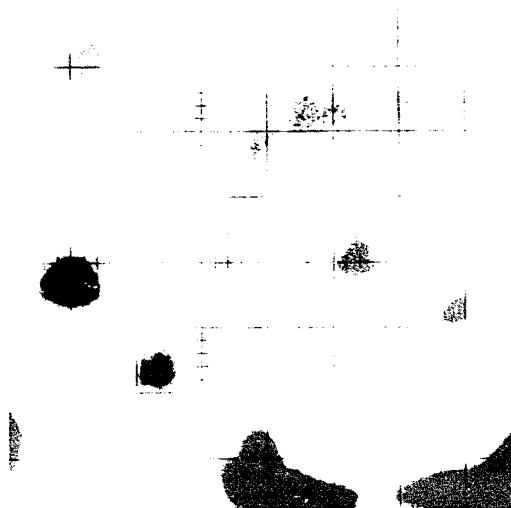


B

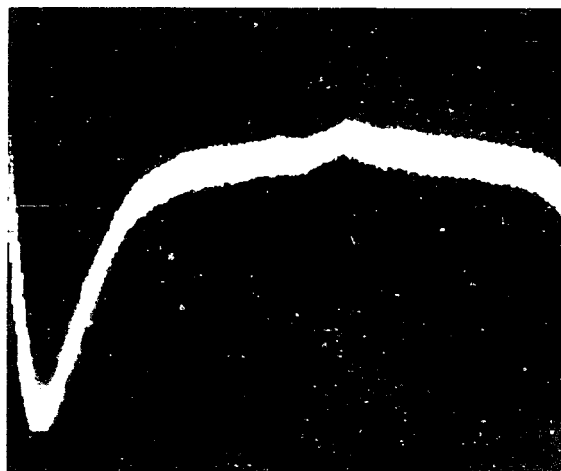
BACK SCATTERED ELECTRON IMAGE (A) AND LINE  
SCAN (B) AT 1000X. PURE NICKEL OXIDE.

Figure 17

Electron Microprobe Specimen Current Image (A)  
and Line Scan (B) for 8.23 Atomic Percent Lithium  
Alloy.



A

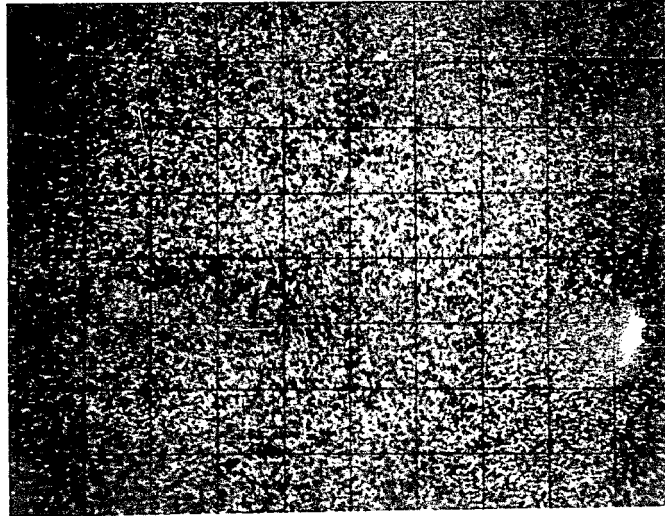


B

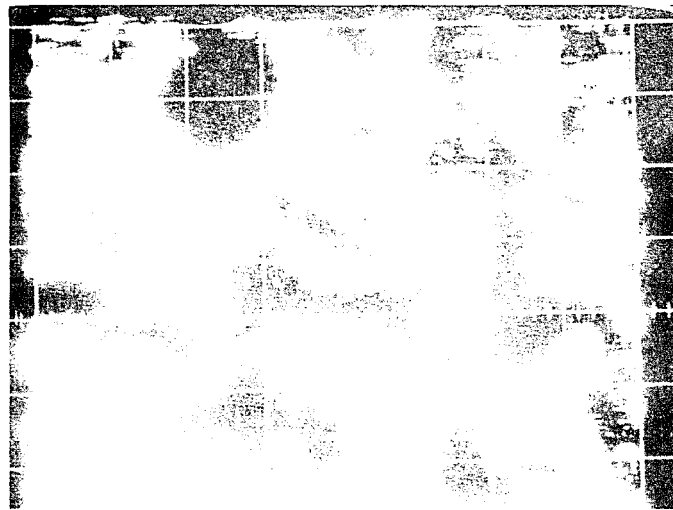
SPECIMEN CURRENT IMAGE (A) AT 1000X AND LINE SCAN (B) AT 2000X. 8.23 ATOMIC PERCENT LITHIUM ALLOY. PORE PEAK HEIGHT IS  $0.0017 \mu$  AMPS. BELOW BASE LINE. BASE LINE CURRENT IS  $0.0112 \mu$  AMPS.

Figure 18

Ni-K $\alpha$  Scan for 8.23 Atomic Percent Lithium-Nickel Oxide Alloy (A) and Mg-K $\alpha$  Scan for 5 Atomic Percent Lithium-Magnesium Oxide Alloy (B).



A



B

A. Ni-K $\alpha$  SCAN FOR 8.23 ATOMIC PERCENT LITHIUM-NICKEL OXIDE ALLOY. 1000X. (PRESENT STUDY).

B. Mg-K $\alpha$  SCAN FOR 5 ATOMIC PERCENT LITHIUM-MAGNESIUM OXIDE ALLOY. (AFTER BICKELHAUPT).

Figure 19

Schematic Representation of the Pulse Transmission  
Method for Modulus Measurements

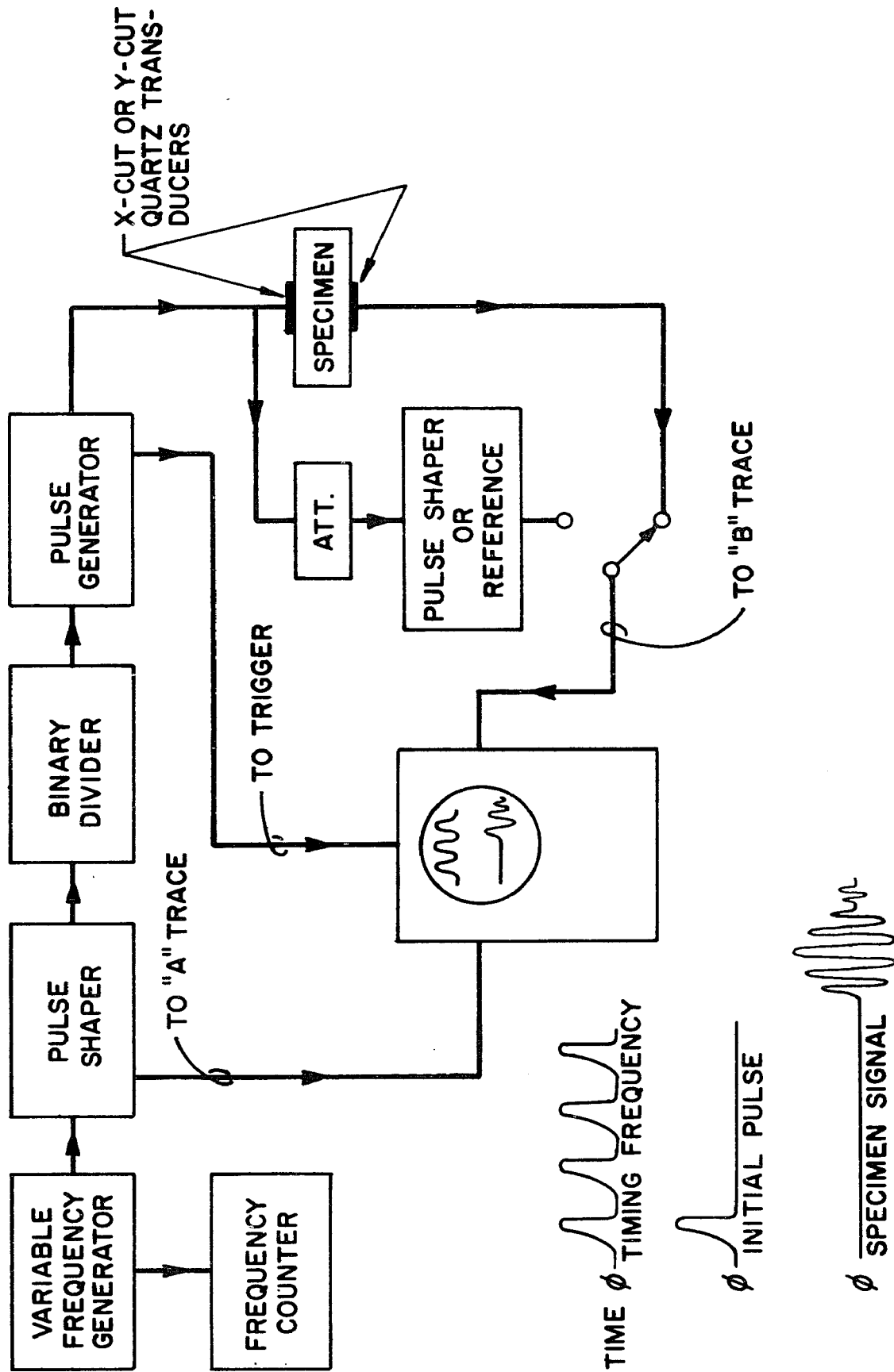


Figure 20

Schematic Representation of the Pneumatic  
Sphere Grinder.

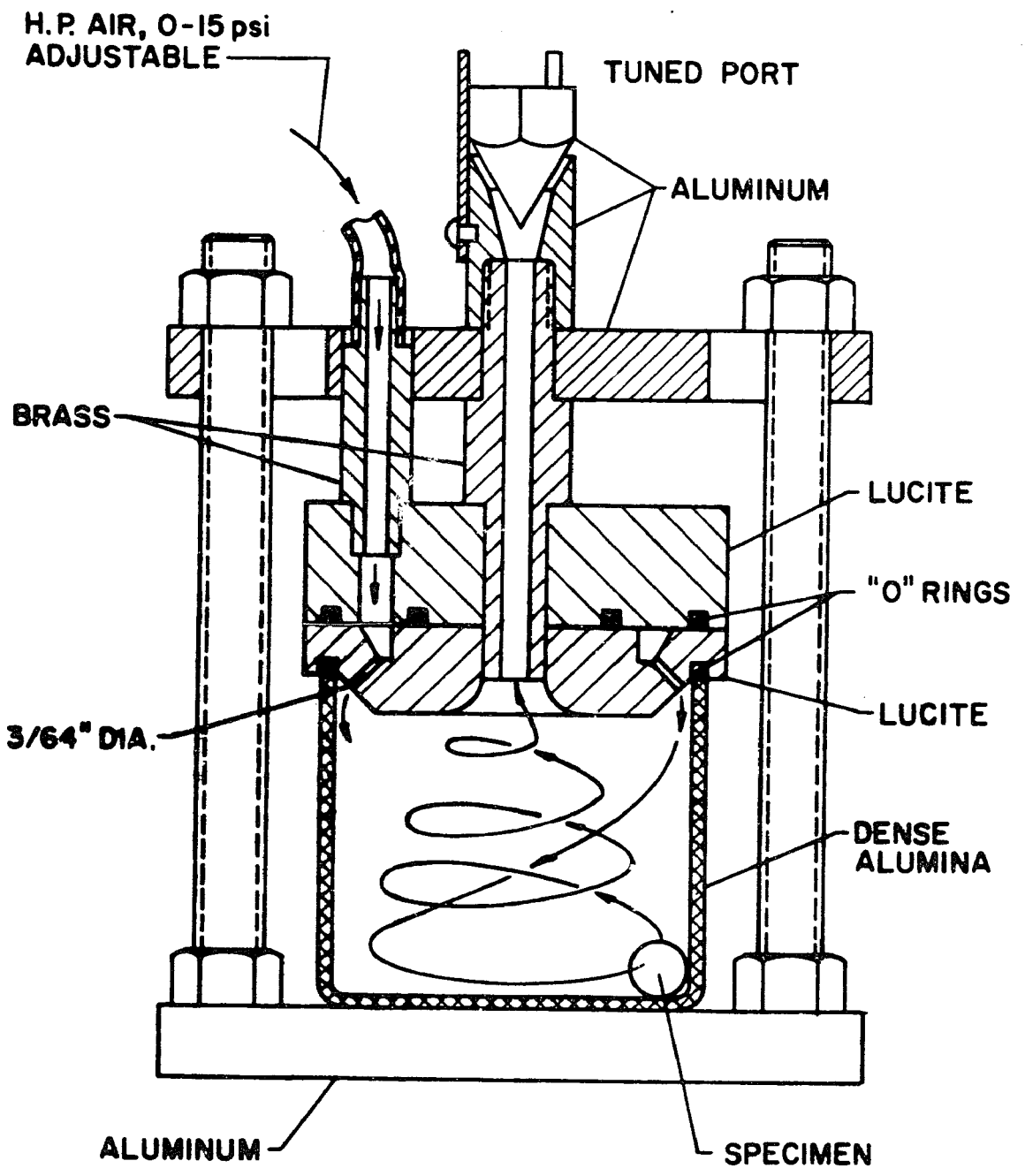


Figure 21

Schematic Representation of the Contra-Rotating  
Sphere Lapping and Polishing System.

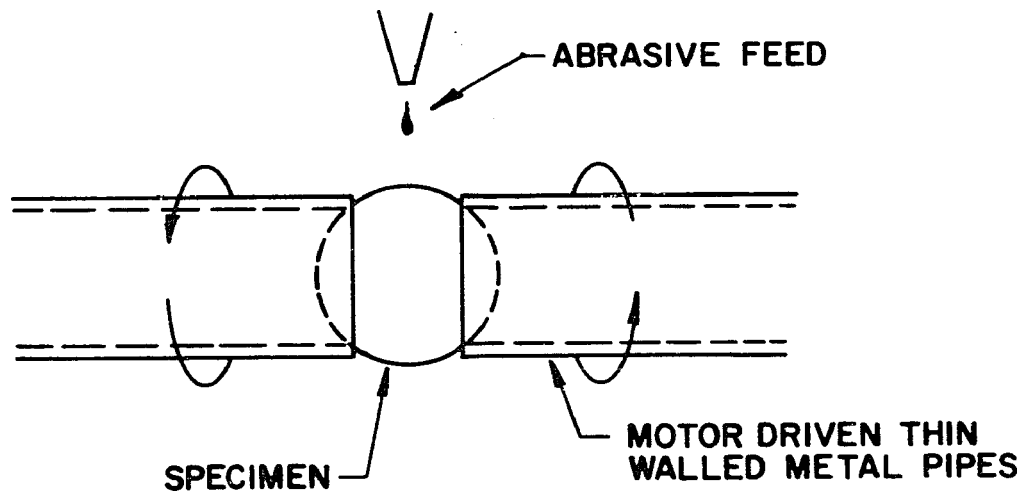


Figure 22

Schematic Representation of the Sphere  
Resonance Method for Modulus Measurements.

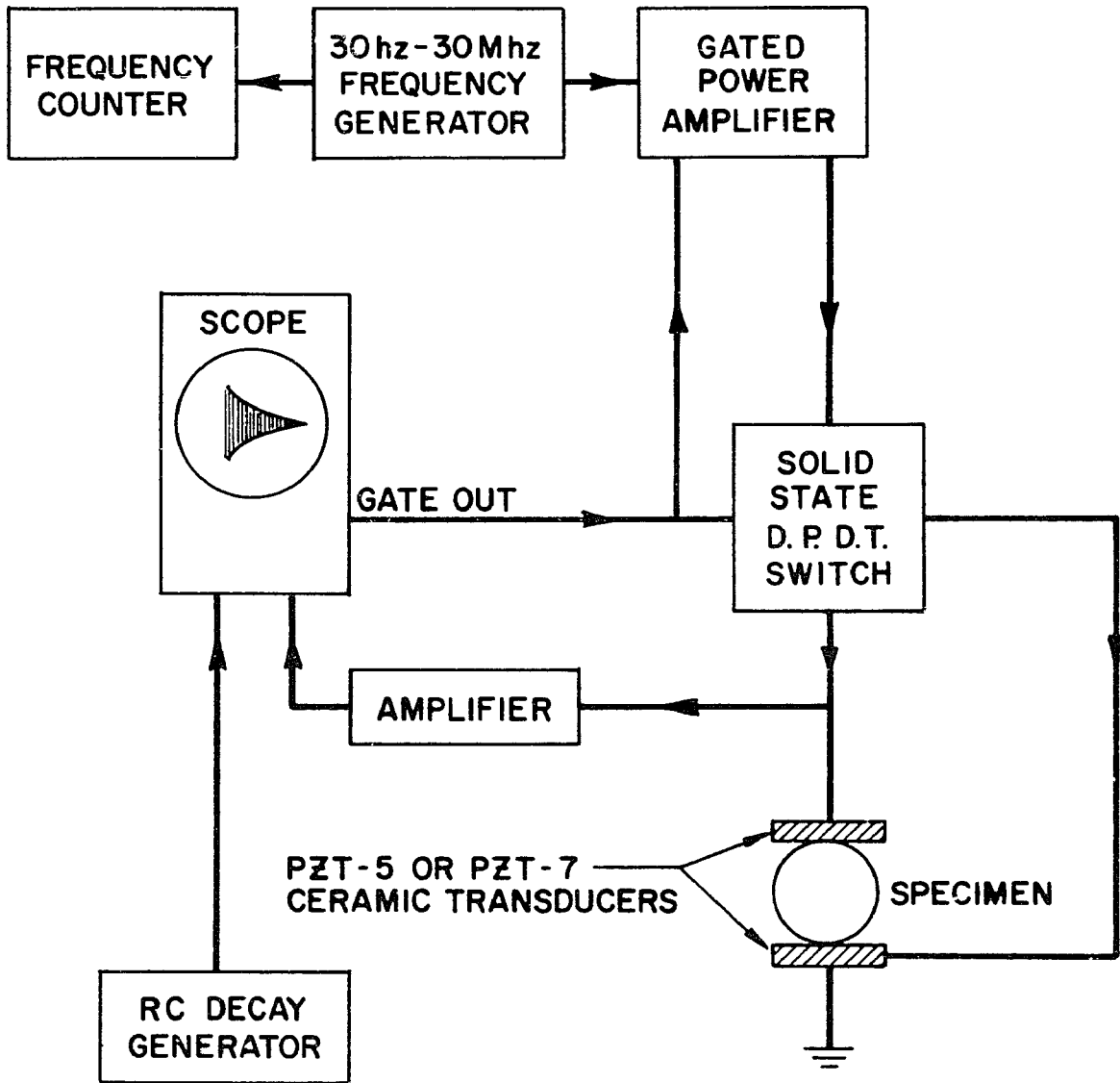


Figure 23

Schematic Representation of the First Three  
Shear Vibration Modes of a Sphere.

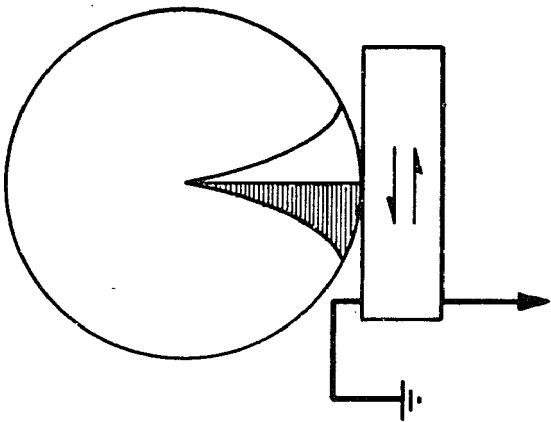
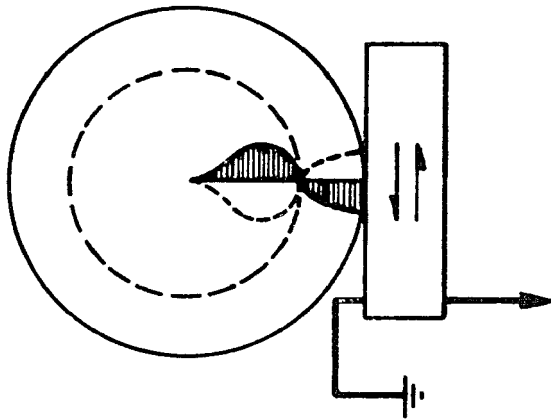
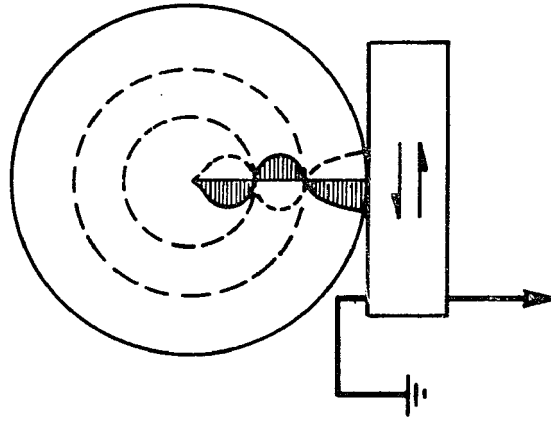


Figure 24

Normalized Resonant Sphere Frequency,  $f_r$ ,  
Versus Poisson's Ratio. Note That Only  
the Spherical Modes,  $i^j$ , are a Function  
of Poisson's Ratio. The Data for Pure  
Nickel Oxide are Shown and a Best Fit is  
Found at  $\sigma = 0.416$ .

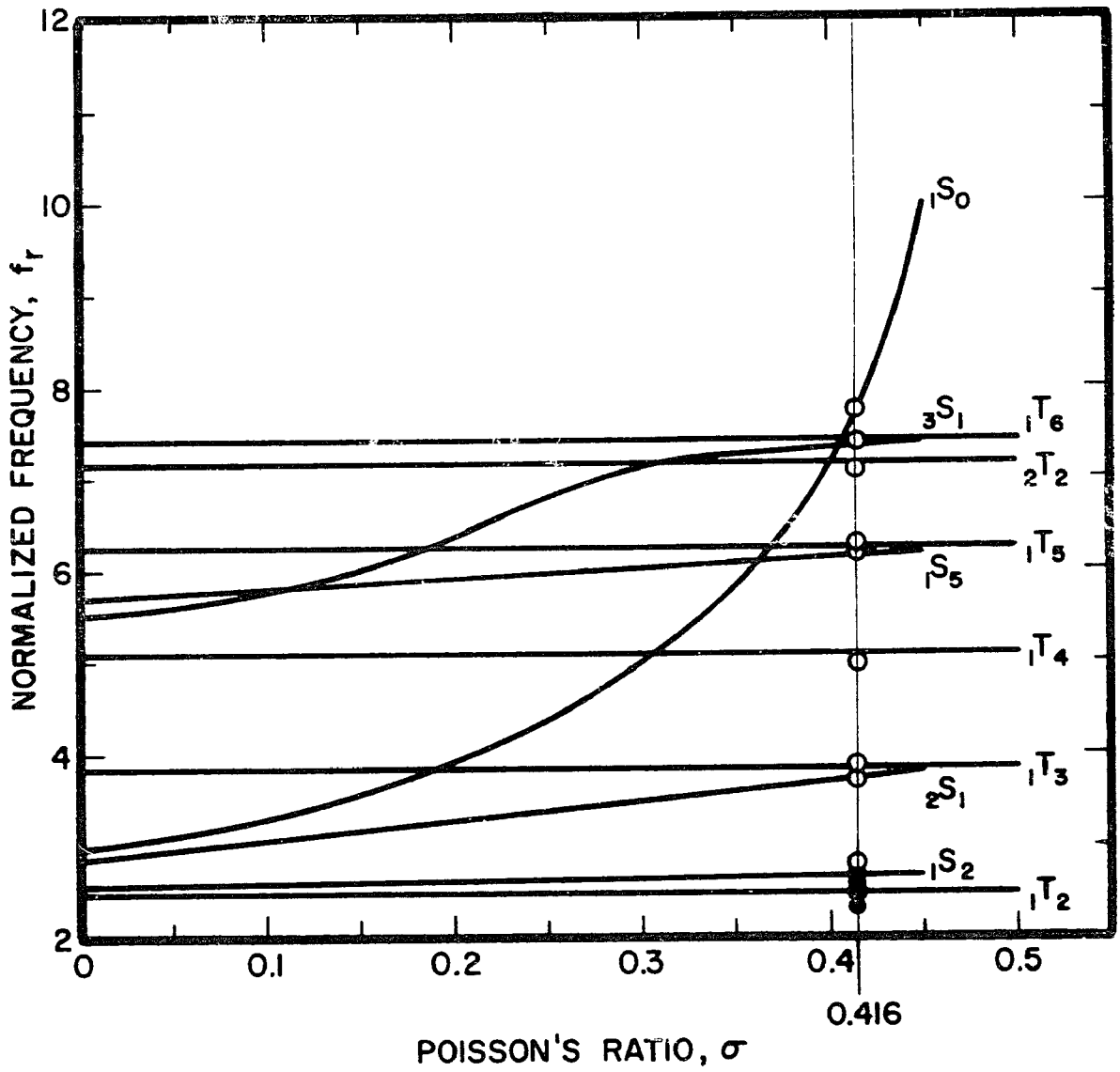


Figure 25

Young's Modulus as a Function of Temperature for the Same Pure Nickel Oxide Specimen Using Two Different Sets of Matched Crystals. Open Circles are 92.5 KC Measurements, Closed Circles are 118.5 KC Measurements.

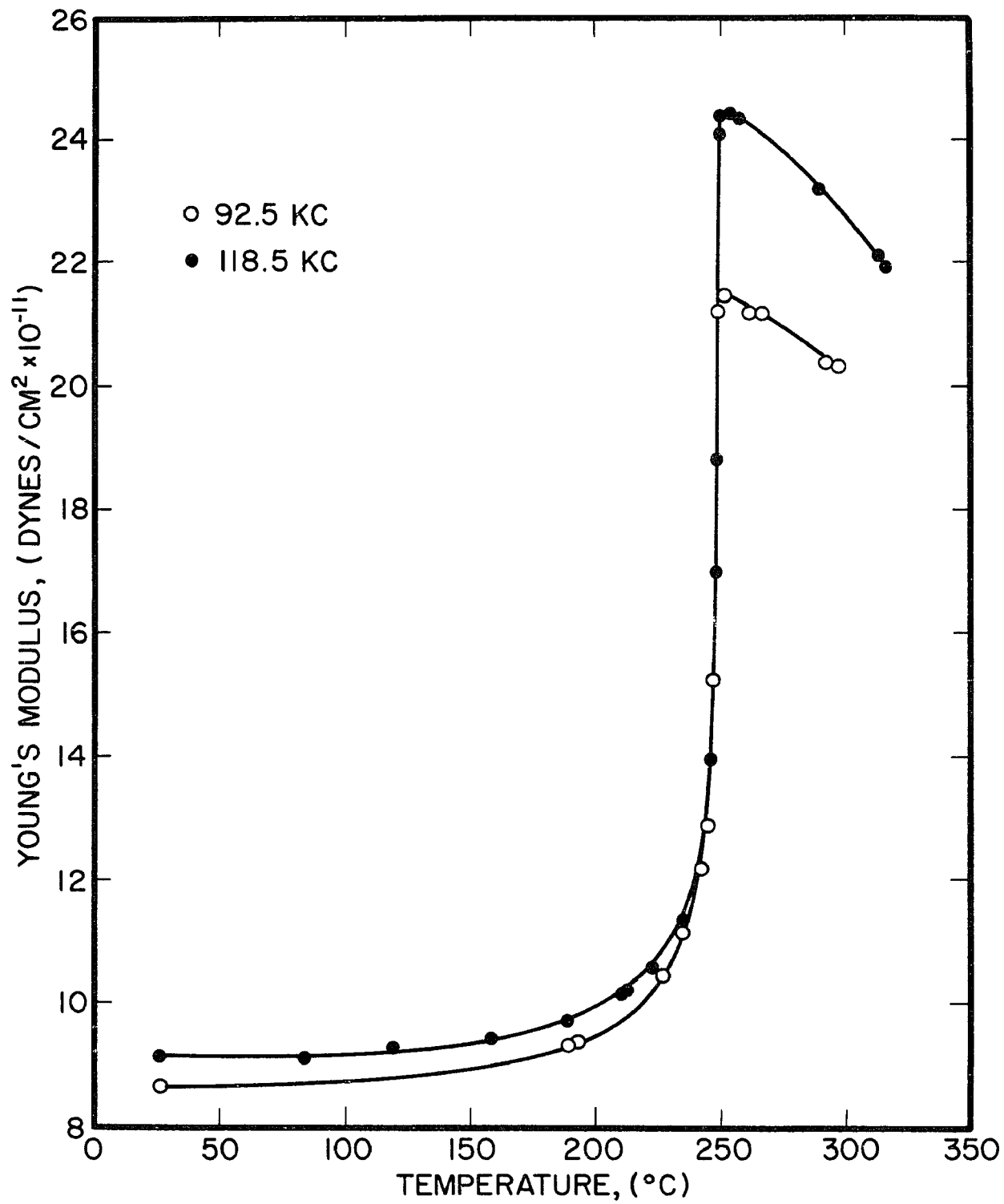


Figure 26

Young's Modulus as a Function of Temperature for Pure Nickel Oxide Measured with 118.5 KC Crystals. Open Circles<sub>2</sub> are Values Obtained From Equation A3.2 ( $\tan^2$  Term Variable) and Closed Circles<sub>2</sub> are Values Obtained From Equation A3.3 ( $\tan^2 \approx 0$ ).

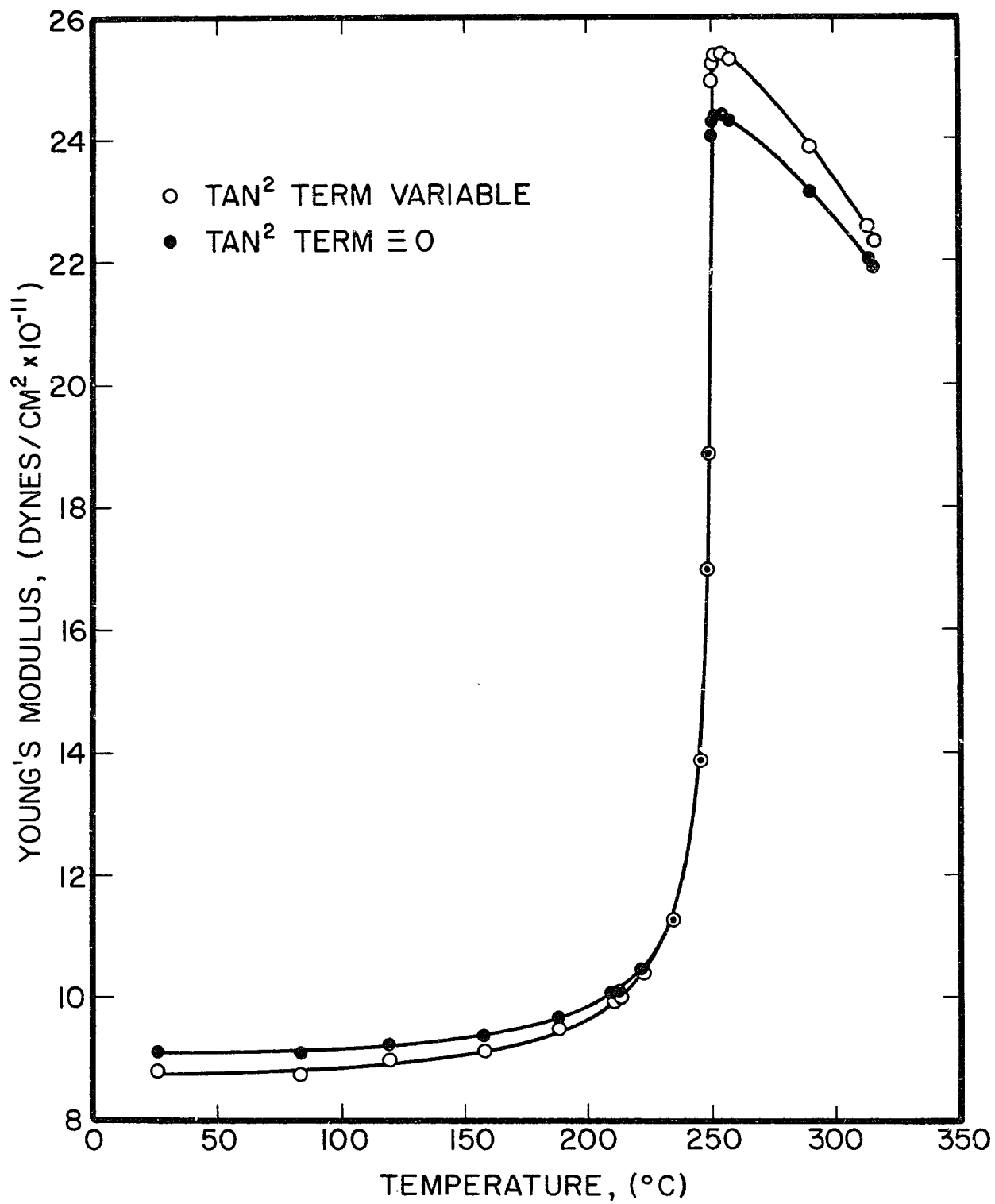


Figure 27

Young's Modulus as a Function of Temperature for Each of the Lithium-Nickel Oxide Alloys Investigated. Each Curve is Identified by the Lithium Content (Atomic Percent) of the Sample, Measurements Taken With 118.5 KC Crystals (Increasing Temperature).

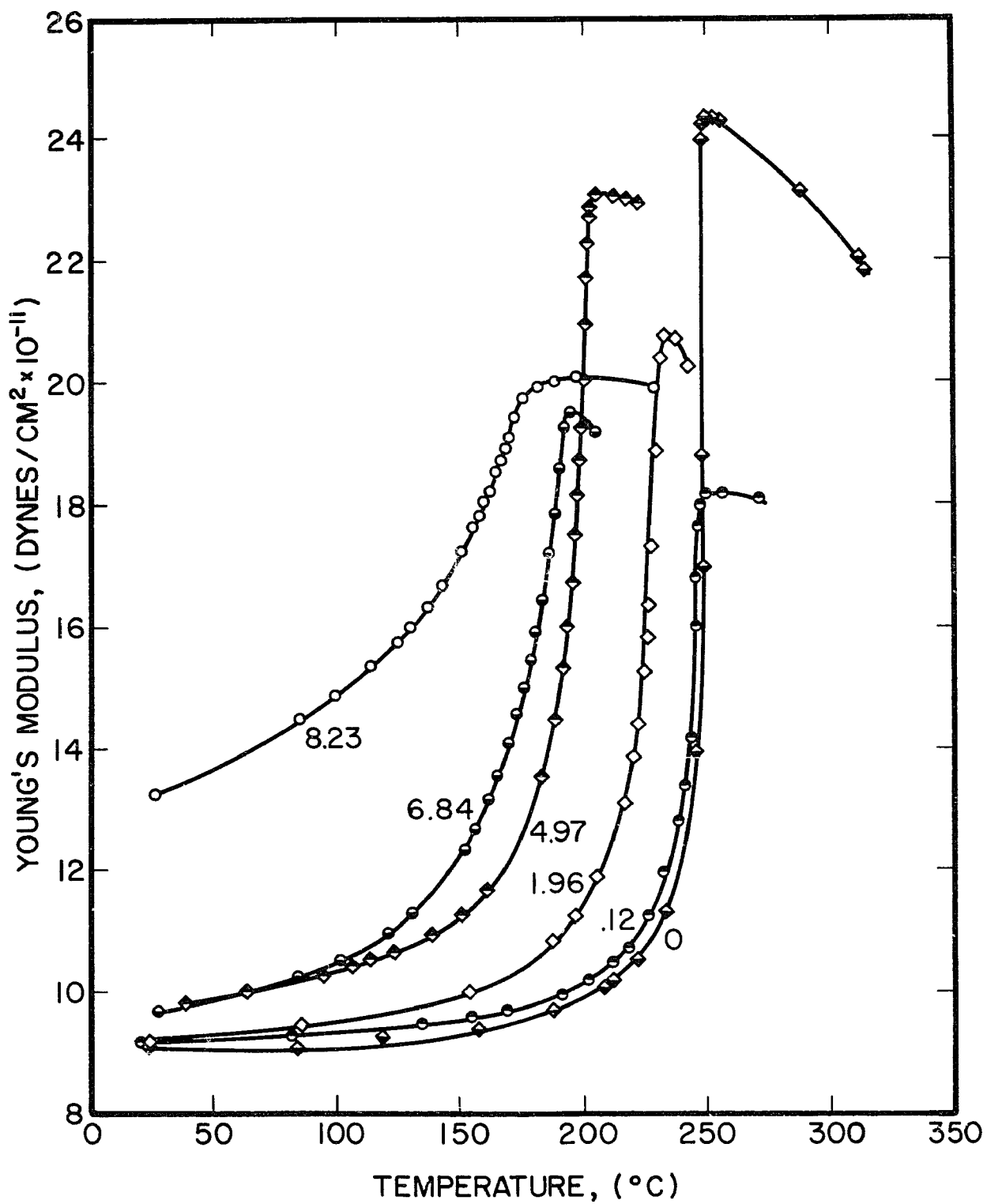


Figure 28

Young's Modulus as a Function of Temperature for Each of the Lithium-Nickel Oxide Alloys Investigated. Each Curve is Identified by the Lithium Content (Atomic Percent) of the Sample. Measurements Taken With 118.5 KC Crystals (Decreasing Temperature).

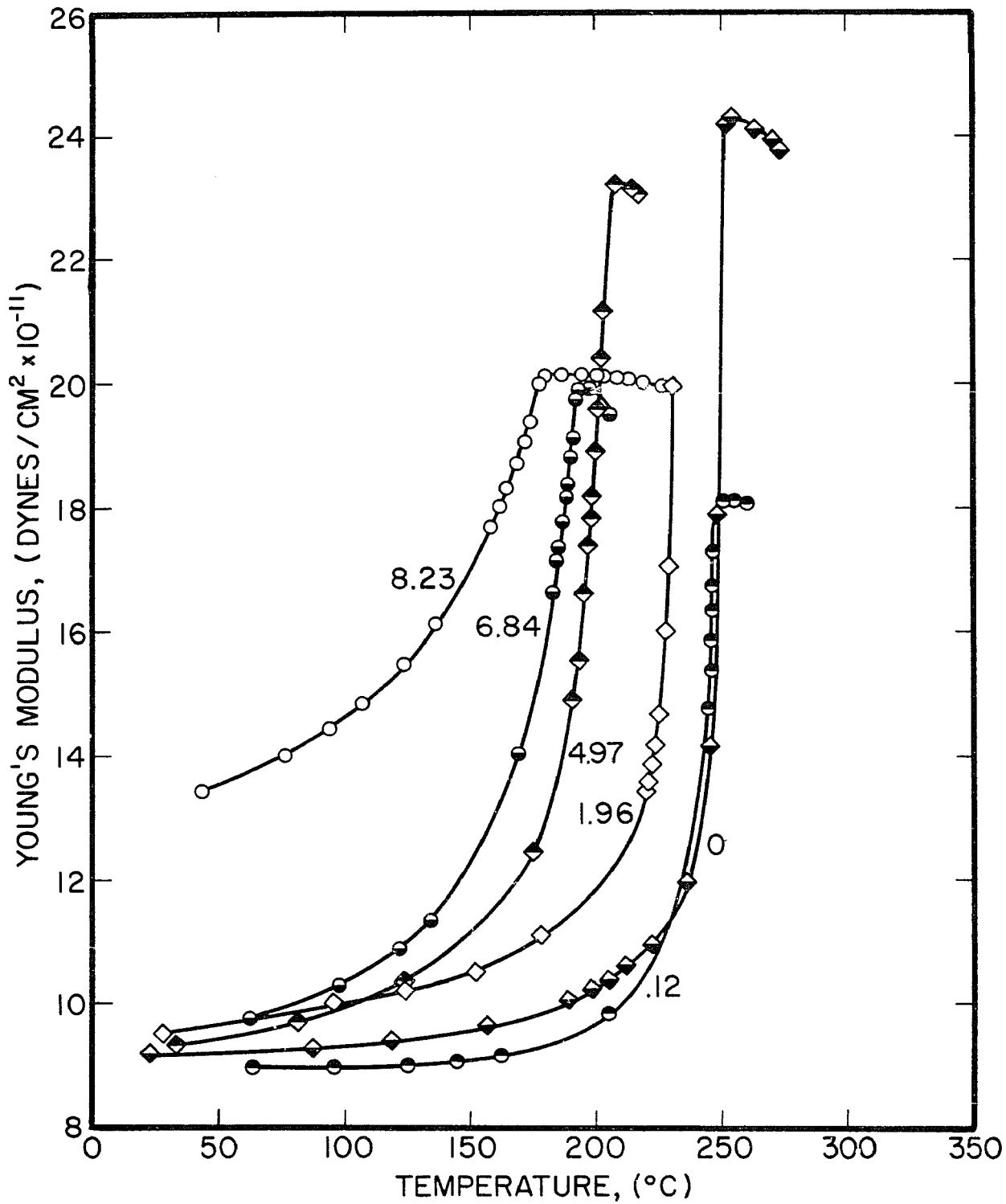


Figure 29

Relative Acoustic Loss as a Function of Temperature for Each of the Lithium-Nickel Oxide Alloys Investigated. Each Curve is Identified by the Lithium Content (Atomic Percent) of the Sample. Measurements Taken With 118.5 KC Crystals (Increasing Temperature). The Flat Response of the 1.96, 6.84 and 8.23 Atomic Percent Lithium Alloys is Caused by the Peak Amplitude at Resonance Going to Zero Above the Néel Temperature.

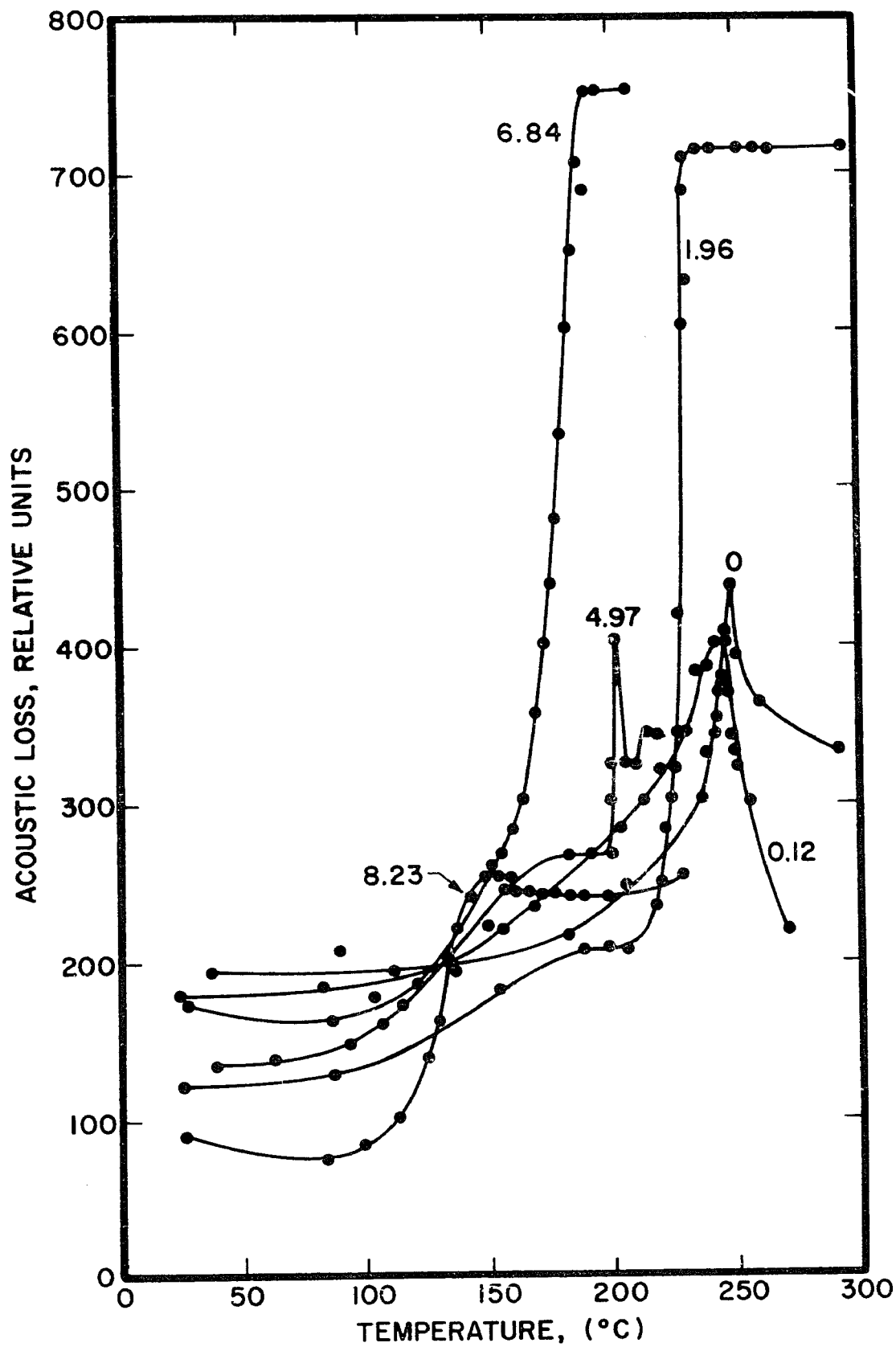


Figure 30

Young's Modulus as a Function of Temperature for a 1 Percent Lithium-11.5 Percent Magnesium-Nickel Oxide Alloy. Measurements Taken With 118.5 KC Crystals. Open Circles are Data Taken With Increasing Temperature, Closed Circles are Data Taken With Decreasing Temperature.

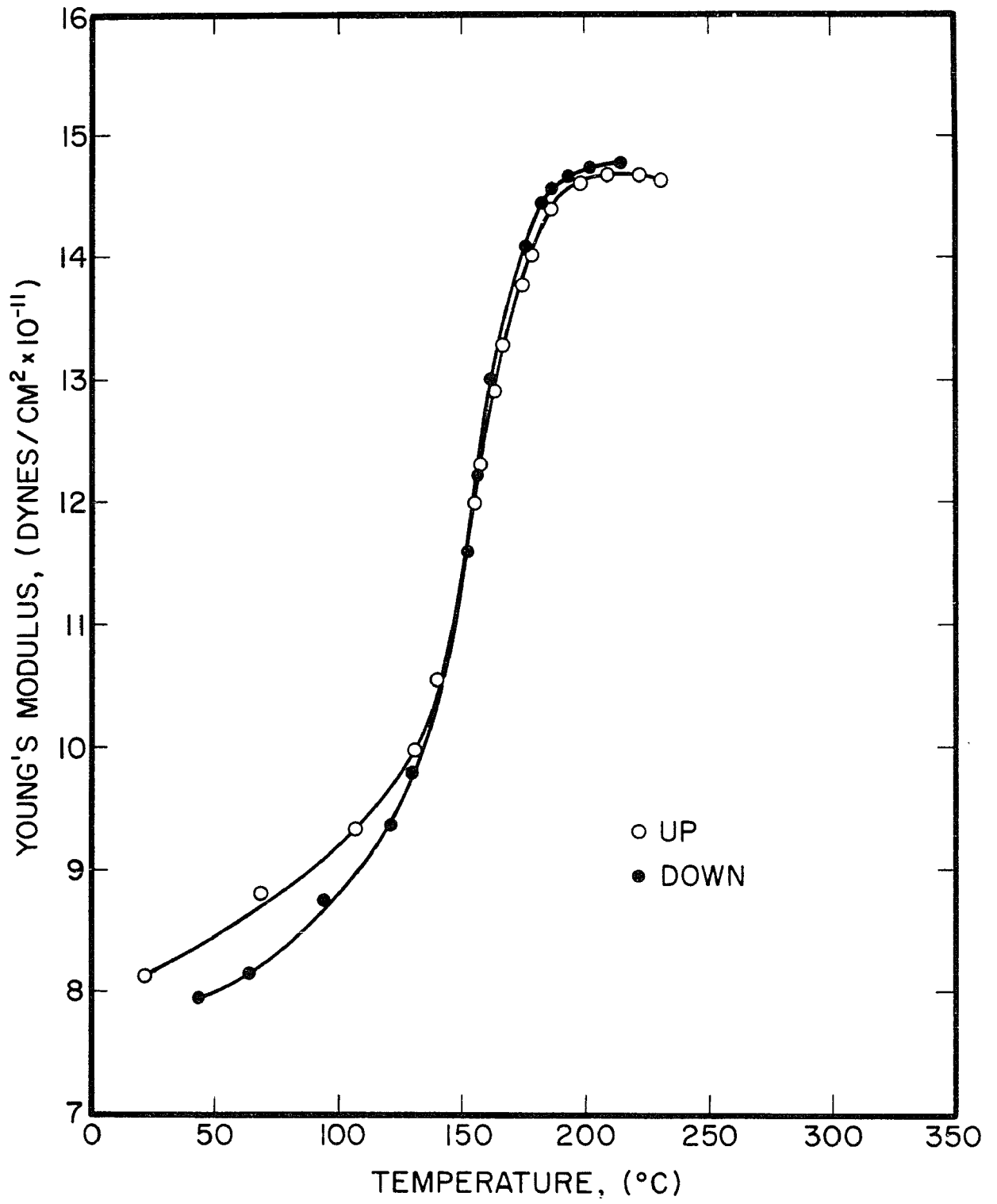


Figure 31

Neel Temperature as a Function of Atomic Percent Lithium as Determined From the Maximum Slope of the Modulus Versus Temperature Curve of Figure 27. The Line was Determined by Least-Squares Analysis.

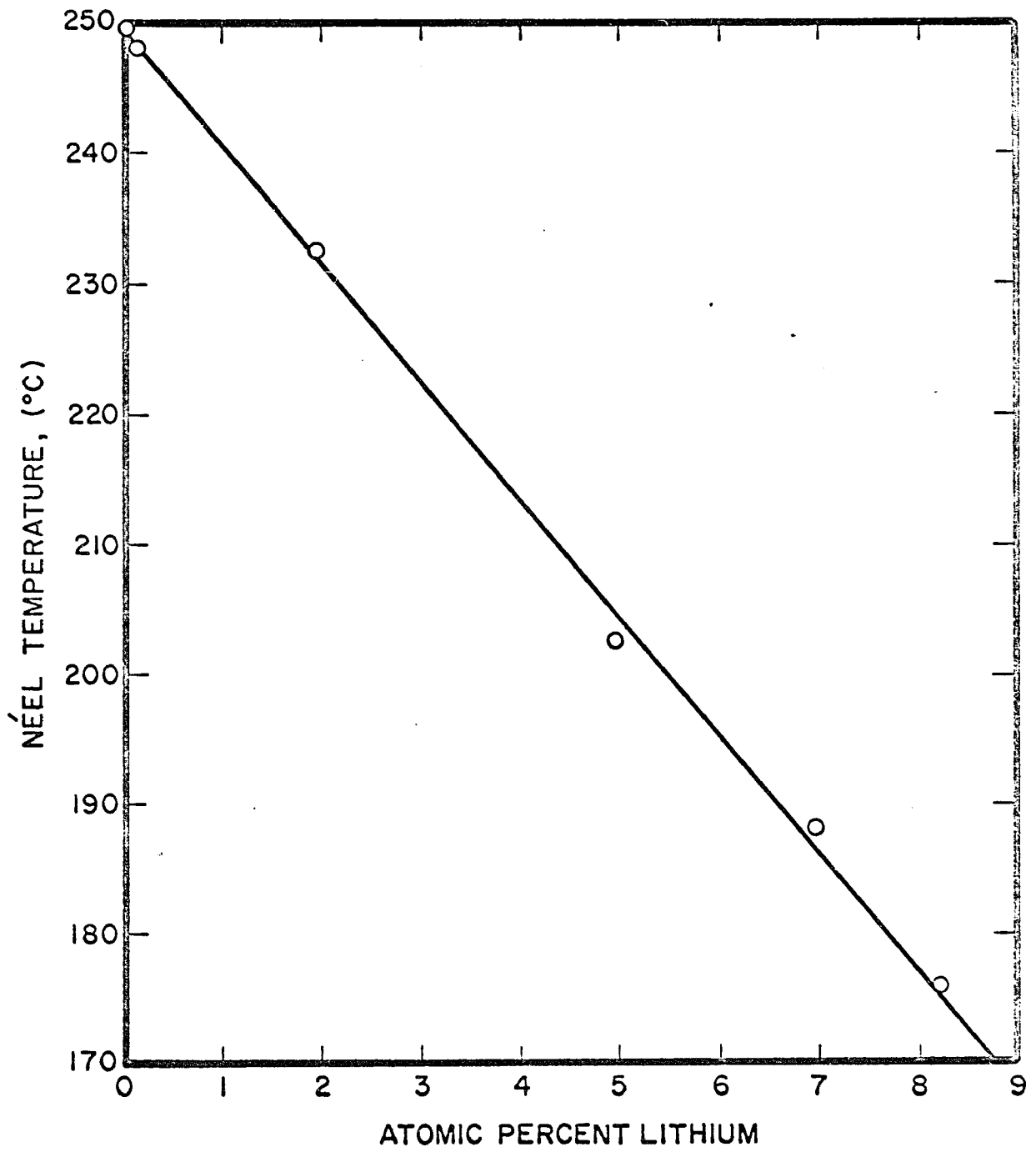


Figure 32

Resistivity as a Function of Temperature for Each of the Lithium-Nickel Oxide Alloys Investigated. Each set of Points is Identified by the Lithium Content (Atomic Percent) of the Sample. Closed Symbols are Data Taken With Increasing Temperature, Open Symbols are Data Taken With Decreasing Temperature.

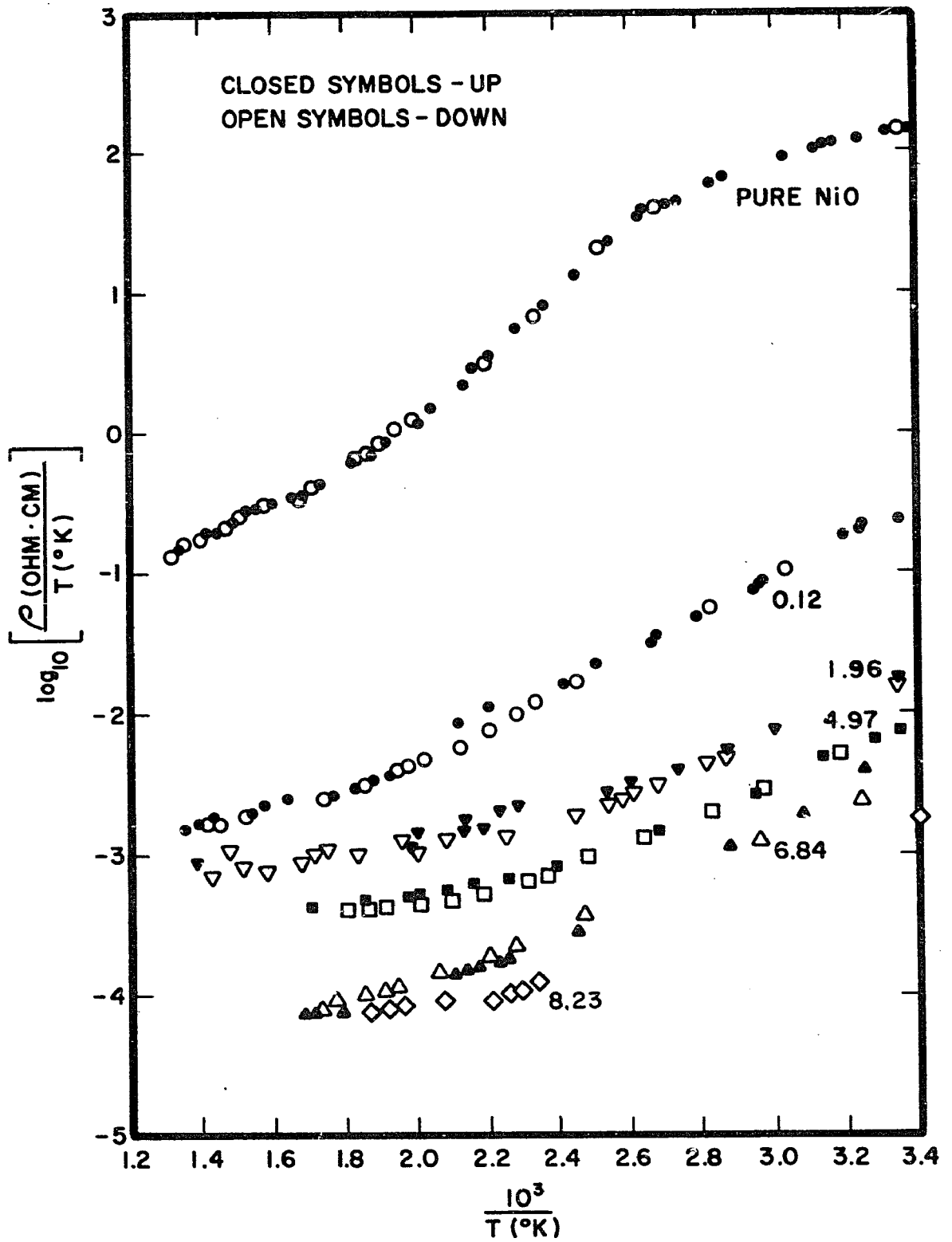
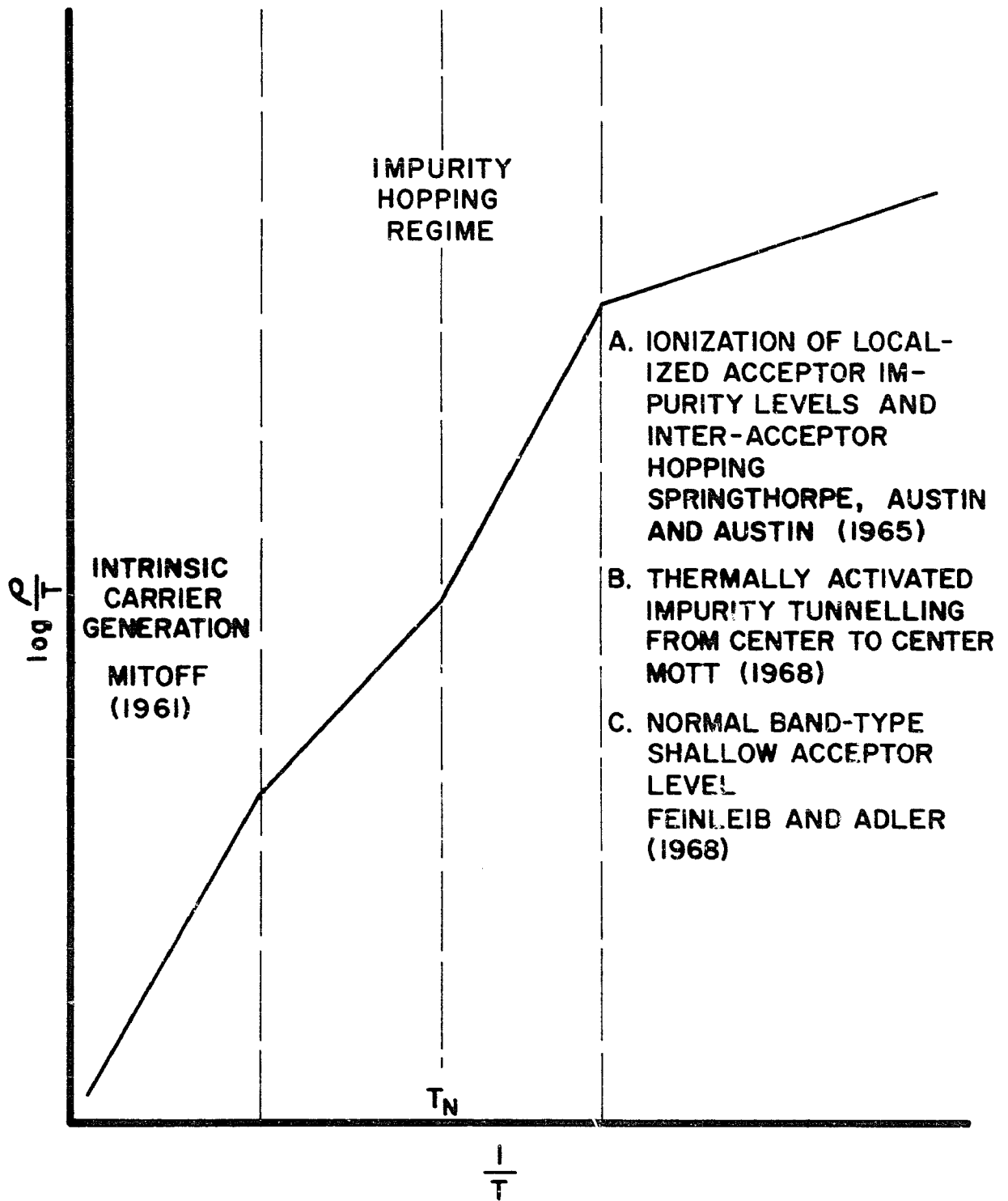


Figure 33

General Form of the Resistivity Versus Temperature for Nickel Oxide.



## VITA.

Michael Richard Notis was born in Brooklyn, New York on August 6, 1938. He attended Far Rockaway High School and was awarded a Grumman Aircraft Engineering Scholarship upon graduation. He attended Lehigh University from 1956 to 1960 and received a B.S. degree in Metallurgical Engineering. During these years he was a summer employee at Grumman Aircraft Engineering Company where he worked in piece parts manufacture, hydraulic line assembly, tool design, and metallurgical quality control departments.

In 1960 Mr. Notis was employed by the Western Electric Company in Allentown, Pennsylvania. He was soon transferred to Bell Telephone Laboratories as a participant in the Western Electric Development Engineering Program and was then promoted to Planning Engineer in 1963. He received his M.S. degree in Metallurgical Engineering at Lehigh University in October 1963, and took a leave of absence from Western Electric Company in order to return to Lehigh in July 1967.

Papers published by Mr. Notis include the "Effect of Growth Rate on Stacking Fault Density in Epitaxial Silicon Layers" in the Journal of Applied Physics, 35 (3) 695-697 (1964), and the "Decarburization of an Iron-Nickel-Cobalt Glass Sealing Alloy" in the Journal of the American Ceramic

Society, 45 (9) 412-416 (1962). He is a member of the Newtonian Society, the Society of Sigma Xi, American Society for Metals, American Society for Testing Materials, and the Metallurgical Society of A.I.M.E.

Mr. Notis was married to the former Ruth Ellen Zwiebel on August 30, 1959 and has three children, Beth, age 8, Mark Ian, age 5, and Jennifer Lynn, age 1.