1978

Fracture resistance of eyebars on the liberty bridge, June 1978.

M. F. Trznadel
B. T. Yen
R. Roberts
A. W. Pense

Follow this and additional works at: http://preserve.lehigh.edu/engr-civil-environmental-fritz-lab-reports

Recommended Citation
http://preserve.lehigh.edu/engr-civil-environmental-fritz-lab-reports/2192
This study is based on the Liberty Bridge which is in Pittsburgh, Pennsylvania and crosses the Monongahela River. The bridge is being evaluated for rehabilitation and the progress to date is summarized in this report. Both field and laboratory studies were made and special attention is given to the fracture resistance and fatigue strength of the eyebars.

Field work included inspection of eyebar heads, live load and dead load stress measurements, and removal of two existing eyebars which were replaced by new ones. Material properties and stresses in the bridge members were evaluated. The distribution and magnitude of stresses in the eyebar heads were examined by a finite element procedure. The possibility of fatigue crack growth from flaws at eyebar head pin holes and the critical crack size which would cause brittle fracture were investigated.

Analysis shows the maximum stress concentration factor at the edge of the pin hole for eyebars designed by the specifications to be around 3.5. Under the existing and anticipated loads, the stresses in eyebars were found to be very low and as a result the possibility of fatigue crack growth and brittle fracture is remote. Based on these findings the planned rehabilitation of the Liberty Bridge is recommended.
Submitted to

SALVUCCI AND ASSOCIATES, INC.

FRACTURE RESISTANCE OF
EYEBARS ON THE LIBERTY BRIDGE
INTERIM REPORT

by

M. F. Trznadel, Jr.
B. T. Yen
R. Roberts
A. W. Pense
J. W. Fisher

LEHIGH UNIVERSITY
Office of Research
Bethlehem, Pennsylvania
June 1978

Fritz Engineering Laboratory Report No. 420.1
# TABLE OF CONTENTS

<table>
<thead>
<tr>
<th>Section</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>ABSTRACT</td>
<td>1</td>
</tr>
<tr>
<td>1. INTRODUCTION</td>
<td>2</td>
</tr>
<tr>
<td>1.1 Historical Background</td>
<td>2</td>
</tr>
<tr>
<td>1.2 Description of the Liberty Bridge</td>
<td>3</td>
</tr>
<tr>
<td>1.3 Objectives and Approach</td>
<td>4</td>
</tr>
<tr>
<td>2. PRELIMINARY RESULTS</td>
<td>7</td>
</tr>
<tr>
<td>2.1 Field Inspection of Eyebars</td>
<td>7</td>
</tr>
<tr>
<td>2.2 Live Load Stresses in Eyebars</td>
<td>8</td>
</tr>
<tr>
<td>2.3 Dead Load Stresses in Eyebars U 35 – U 36</td>
<td>10</td>
</tr>
<tr>
<td>2.4 Material Properties</td>
<td>12</td>
</tr>
<tr>
<td>3. STRESS DISTRIBUTION IN EYEBAR HEADS</td>
<td>13</td>
</tr>
<tr>
<td>3.1 Design Parameters and Assumptions</td>
<td>13</td>
</tr>
<tr>
<td>3.2 Finite Element Model</td>
<td>16</td>
</tr>
<tr>
<td>3.3 Comparison with Test Results</td>
<td>19</td>
</tr>
<tr>
<td>3.4 Stress Concentration Factor at Eyebar Pin Holes</td>
<td>21</td>
</tr>
<tr>
<td>4. FRACUTRE RESISTANCE AND FATIGUE STRENGTH</td>
<td>23</td>
</tr>
<tr>
<td>4.1 Fracture Resistance</td>
<td>23</td>
</tr>
<tr>
<td>4.1.1 Approximations in Correction Factors</td>
<td>24</td>
</tr>
<tr>
<td>4.1.2 Stress Intensity Factor and Critical Crack Size</td>
<td>26</td>
</tr>
<tr>
<td>4.2 Fatigue Strength</td>
<td>27</td>
</tr>
<tr>
<td>Section</td>
<td>Page</td>
</tr>
<tr>
<td>----------------------------------------------</td>
<td>------</td>
</tr>
<tr>
<td>5. DISCUSSION</td>
<td>30</td>
</tr>
<tr>
<td>5.1 Stress Evaluation</td>
<td>30</td>
</tr>
<tr>
<td>5.2 Bonded Eyebar Heads</td>
<td>31</td>
</tr>
<tr>
<td>5.3 Anticipated Conditions</td>
<td>32</td>
</tr>
<tr>
<td>6. CONCLUSIONS AND RECOMMENDATIONS</td>
<td>33</td>
</tr>
<tr>
<td>ACKNOWLEDGMENTS</td>
<td>36</td>
</tr>
<tr>
<td>TABLES</td>
<td>37</td>
</tr>
<tr>
<td>FIGURES</td>
<td>40</td>
</tr>
<tr>
<td>REFERENCES</td>
<td>77</td>
</tr>
</tbody>
</table>
## LIST OF TABLES

<table>
<thead>
<tr>
<th>Table</th>
<th>Description</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Maximum Measured Stress Range in Eyebar Shanks</td>
<td>37</td>
</tr>
<tr>
<td>2</td>
<td>Tensile Properties of Eyebar Material - AISI - 1035 Steel Heat Treated</td>
<td>38</td>
</tr>
<tr>
<td>3</td>
<td>Chemical Analysis</td>
<td>38</td>
</tr>
<tr>
<td>4</td>
<td>Design Criteria for Proportioning Eyebar Heads</td>
<td>39</td>
</tr>
<tr>
<td>Figure</td>
<td>Description</td>
<td>Page</td>
</tr>
<tr>
<td>--------</td>
<td>------------------------------------------------------------------------------</td>
<td>------</td>
</tr>
<tr>
<td>1</td>
<td>Elevation of Liberty Bridge Looking West (Downstream)</td>
<td>39</td>
</tr>
<tr>
<td>2</td>
<td>Locations of Eyebars on the Main Spans Over the River</td>
<td>40</td>
</tr>
<tr>
<td>3</td>
<td>Typical Cross Section of the Liberty Bridge</td>
<td>41</td>
</tr>
<tr>
<td>4</td>
<td>Eyebar Head U 36A with Pin Cap Removed</td>
<td>42</td>
</tr>
<tr>
<td>5</td>
<td>Sandblasted Eyebar Head Showing Forging Marks</td>
<td>42</td>
</tr>
<tr>
<td>6</td>
<td>Variation in Live Load Stress versus Time For Truck in Different Lanes</td>
<td>43</td>
</tr>
<tr>
<td>7</td>
<td>Measured Stress Ranges for Test Truck in Curb Lane, Northbound</td>
<td>44</td>
</tr>
<tr>
<td>8</td>
<td>Dimensions of Eyebars at U 35 - U 36</td>
<td>45</td>
</tr>
<tr>
<td>9</td>
<td>Typical arrangement of Strain Gages for Live Load and Dead Load Study</td>
<td>46</td>
</tr>
<tr>
<td>10</td>
<td>Non-dimensionalized Measured Stress Distribution - U 36A Dead Load</td>
<td>47</td>
</tr>
<tr>
<td>11</td>
<td>Non-dimensionalized Measured Stress Distribution - U 36A Partial Load</td>
<td>48</td>
</tr>
<tr>
<td>12</td>
<td>Non-dimensionalized Measured Stress Distribution - U 35A Dead Load</td>
<td>49</td>
</tr>
<tr>
<td>13</td>
<td>Non-dimensionalized Measured Stress Distribution - U 35A Partial Load</td>
<td>50</td>
</tr>
</tbody>
</table>
### LIST OF FIGURES (continued)

<table>
<thead>
<tr>
<th>Figure</th>
<th>Description</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>14</td>
<td>Non-dimensionalized Measured Stress Distribution - U·36 D Dead Load</td>
<td>52</td>
</tr>
<tr>
<td>15</td>
<td>Non-dimensionalized Measured Stress Distribution - U·36D Partial Load</td>
<td>53</td>
</tr>
<tr>
<td>16</td>
<td>Dead Load Stresses in Shanks of Eyebars</td>
<td>54</td>
</tr>
<tr>
<td>17</td>
<td>Test Results of $K_{IC}$ for Eyebar Material (AISI 1035 Heat-Treated Steel)</td>
<td>55</td>
</tr>
<tr>
<td>18</td>
<td>Variation of $K_{ID}$ with Temperature</td>
<td>56</td>
</tr>
<tr>
<td>19</td>
<td>Charpy V-Notch (CVN) Test Results</td>
<td>57</td>
</tr>
<tr>
<td>20</td>
<td>Fracture Toughness Converted from CVN Results (U·35 - U·36A)</td>
<td>58</td>
</tr>
<tr>
<td>21</td>
<td>Fracture Toughness Converted from CVN Results (U·35 - U·36D)</td>
<td>59</td>
</tr>
<tr>
<td>22</td>
<td>Symbols Used to Describe Eyebar Geometry</td>
<td>60</td>
</tr>
<tr>
<td>23</td>
<td>Discretization of Eyebar Head With Curved Transition</td>
<td>61</td>
</tr>
<tr>
<td>24</td>
<td>Discretization of Eyebar Head With Straight Line Approximation</td>
<td>62</td>
</tr>
<tr>
<td>25</td>
<td>The Effect of Curved and Straight Line Transition on the Stress Distribution</td>
<td>63</td>
</tr>
<tr>
<td>26</td>
<td>Discretization and Boundary Conditions of Substructure for a Fine Mesh Analysis</td>
<td>64</td>
</tr>
<tr>
<td>Figure</td>
<td>Description</td>
<td>Page</td>
</tr>
<tr>
<td>--------</td>
<td>------------------------------------------------------------------------------</td>
<td>------</td>
</tr>
<tr>
<td>27</td>
<td>Effect of Finite Element Size on Stress Distribution</td>
<td>65</td>
</tr>
<tr>
<td>28</td>
<td>Comparison of Finite Element Analysis Results and Measured Values</td>
<td>66</td>
</tr>
<tr>
<td>29</td>
<td>Results of Gross Mesh Analysis of Eyebar U 35 - U 36 on the Liberty Bridge</td>
<td>67</td>
</tr>
<tr>
<td>30</td>
<td>Comparison of Measured and Theoretical Stress Distributions for U 36A</td>
<td>68</td>
</tr>
<tr>
<td>31</td>
<td>Enlarged Plot of Gross and Fine Mesh Analysis Results</td>
<td>69</td>
</tr>
<tr>
<td>32</td>
<td>Stress Distribution for Eyebar Heads with Different Width Ratios, Gross Mesh</td>
<td>70</td>
</tr>
<tr>
<td>33</td>
<td>Effect of Pin Hole Size on the SCF, Gross Mesh</td>
<td>71</td>
</tr>
<tr>
<td>34</td>
<td>Effect of Shank Width on the SCF, Gross Mesh</td>
<td>72</td>
</tr>
<tr>
<td>35</td>
<td>Front Free Surface Correction Factor, $F_s$</td>
<td>73</td>
</tr>
<tr>
<td>36</td>
<td>Assumed Crack Shape at Edge of Pin Hole</td>
<td>74</td>
</tr>
<tr>
<td>37</td>
<td>Stress Concentration Factor $K_t$ and Stress Gradient Correction Factor, $F_g$ as a Function of Crack Size</td>
<td>75</td>
</tr>
<tr>
<td>38</td>
<td>Stress Intensity Factor as a Function of Crack Size</td>
<td>76</td>
</tr>
</tbody>
</table>
This study is based on the Liberty Bridge which is in Pittsburgh, Pennsylvania and crosses the Monongahela River. The bridge is being evaluated for rehabilitation and the progress to date is summarized in this report. Both field and laboratory studies were made and special attention is given to the fracture resistance and fatigue strength of the eyebars.

Field work included inspection of eyebar heads, live load and dead load stress measurements, and removal of two existing eyebars which were replaced by new ones. Material properties and stresses in the bridge members were evaluated. The distribution and magnitude of stresses in the eyebar heads were examined by a finite element procedure. The possibility of fatigue crack growth from flaws at eyebar head pin holes and the critical crack size which would cause brittle fracture were investigated.

Analysis shows the maximum stress concentration factor at the edge of the pin hole for eyebars designed by the specifications to be around 3.5. Under the existing and anticipated loads, the stresses in eyebars were found to be very low and as a result the possibility of fatigue crack growth and brittle fracture is remote. Based on these findings the planned rehabilitation of the Liberty Bridge is recommended.
1. INTRODUCTION

1.1 Historical Background

Bridges which utilize eyebars as primary tension members date back to the old Budapest Suspension Bridge, built in 1849 by W. Tierney Clark. The eyebars of this bridge are believed to be made of an iron alloy. Steel eyebars were first introduced, for use in bridges, around the year 1880 and heat-treated carbon steel eyebars were developed in 1914.\(^1,2\)

With the advent of high strength wire rope and new construction methods the eyebar was not used as often in the design of bridges after the early 1930's.

The designers of eyebar bridges during the late 1800's and early 1900's did not have the benefit of considering stress corrosion cracking, corrosion fatigue, or fatigue crack growth in their analysis since these considerations were not sufficiently developed. After the recent (1967) collapse of the Point Pleasant Bridge connecting Point Pleasant, West Virginia, and Kanauga, Ohio the possibility of other eyebar bridge failures became a major concern.\(^3\) The failure of this bridge cost the lives of 46 persons. The bridge was an eyebar cable suspension type and the material used for the eyebars was a heat-treated carbon steel conforming to the specifications for AISI 1060 steel. The National Transportation Safety Board Report on the
Point Pleasant Bridge\textsuperscript{3} indicates that collapse of the bridge structure was attributed to failure of an eyebar caused by stress corrosion and/or corrosion fatigue resulting in growth of a flaw to a critical size.

The failure of the Point Pleasant Bridge immediately made suspect other eyebar bridges to fatigue crack growth and brittle fracture. Most of the eyebar bridges in the United States were constructed in the early 1900's and the materials used for the eyebars were primarily heat-treated carbon steels. The Liberty Bridge is one such bridge that utilized eyebars as primary tension members and is the subject of this study.

1.2 Description of the Liberty Bridge

The Liberty Bridge is a deck type continuous truss structure as shown in Fig. 1. It has a four lane roadway which carries northbound and southbound traffic to and from Pittsburgh, Pennsylvania over the Monongahela River. The total length of the bridge is about 794 meters (2605 feet) with two main truss spans of 143.4 meters (470.5 feet) over the river. There are three short girder spans and three truss spans over the railroad tracks and streets at the south end, and two girder spans and three truss spans over the parkway, railroad and avenue at the north end.

The top chords of the trusses in the negative moment regions over the piers are tension members and utilize eyebars. (See Fig. 2) The eyebars are made of AISI 1035 heat-treated carbon steel.
The bridge has a floor beam and stringer system with a non-composite concrete deck and an asphalt wearing surface. A typical cross section of the bridge is shown in Fig. 3. Construction of the bridge was finished in 1928.

In 1974 all top chord tension members consisted of two eyebars strengthened by the addition of two reinforcing eyebars fabricated from ASTM A588 structural steel. This increased the redundancy of the two eyebar systems and the safety of the bridge in the event of fracture of any one eyebar.

1.3 Objectives and Approach

The objective of the overall study on the Liberty Bridge is to evaluate the safety and integrity of the bridge for continued service and the planned life of the structure. The bridge is to be rehabilitated with a widened deck replacing the present deteriorated one.

The specific goal of this study, of which some preliminary results are reported herein, is to investigate the fatigue strength and fracture resistance of the eyebars. The approach to achieve this goal consists of the following steps.

1. Inspection of the eyebars, particularly the eyebar heads: This work was carried out in the field and in the laboratory, when a couple of eyebars removed from the bridge were examined.
2. Measurement of live load stresses: - Since a vehicular weight limit has been posted for the bridge, a special test truck was employed. Stresses in eyebar shanks and heads were monitored using electrical resistance strain gages.

3. Measurement of dead load stresses in eyebars: - Dead load stresses can only be measured by relieving the loads in eyebars. Mechanical devices and hydraulic jacks were used to accomplish this. Two eyebars were removed from the bridge for studies in the laboratory.

4. Determination of material properties of eyebars: - Of primary concern is the fracture toughness of the eyebar material. Standard specimens for evaluating this material property have been fabricated from the eyebars which were removed from the bridge.

5. Analysis and evaluation of stress distribution in eyebars and eyebar heads: - The stress distribution among eyebar groups, within each shank and in the eyebar heads, were evaluated using measured stress values. The finite element procedure was utilized to analyze stress distributions in eyebar heads with different dimensions.

6. Evaluation of fatigue strength and fracture resistance of eyebars: - The fatigue strength is estimated in terms of the nominal live load stress in eyebar shanks and the anticipated number of load cycles to failure.
The stress range corresponding to the crack growth threshold was also evaluated for the conditions observed. Failure is when a fatigue crack would have grown in size to the critical dimensions which would cause sudden brittle fracture under adverse conditions.

While work is still in progress, some preliminary results have been obtained and are summarized briefly in this report. Some preliminary conclusions are also drawn. More comprehensive conclusions and recommendations will be made when all phases of the study have been completed.
2. PRELIMINARY RESULTS

2.1 Field Inspection of Eyebars

Eyebar pin caps were removed from panel points U 35, U 36 and U 47 of the upstream truss for inspection of the eyebar holes. The locations of these panel points are shown in Fig. 2. For identification purposes, eyebars in a group were arbitrarily designated A, B, C and D from upstream towards downstream. Eyebars U 35 - U 36A and D were originals whereas U 35 - U 36B and C are reinforcing eyebars which were added in 1974 to eliminate any two-eyebar panels in the bridge.

The exposed eyebar head U 36A is shown in Fig. 4. Visual inspection with a magnifying glass did not reveal any cracks or sharp notches at eyebar heads U 35A, U 35D, U 36A, U 36 D and U 47A. The Acoustic Crack Detector (ACD) with special eyebar probe of the Federal Highway Administration was also used and did not indicate any cracks or flaws in the same eyebar heads. The eyebar head faces, however, had forging marks which could be seen after the faces were sandblasted clean. An example is shown in Fig. 5. These forging marks were not situated at the crucial points, nor were the directions of the marks perpendicular to the primary stresses in the heads. Since the ACD could not detect their presence, the depth of these marks were assumed to be shallow. Later examinations in the laboratory did not reveal any adverse condition and verified that no sharp, crack-like condition existed.
The pins and pin holes at U 35 and U 36 appeared to be in fairly good condition by visual inspection after the eyebars were removed from the panel. The holes were slightly larger than the pins and were very slightly elongated under the dead weight of the bridge. When the dead loads were removed from eyebars U 35 - U 36A and D, there was no apparent permanent deformation at the holes. There was some indication of corrosion in the pins between eyebars at these two panel points, but the corrosion was quite moderate when compared to the corroded condition of some steel parts of the deck system. The eyebar shanks generally were in good condition except for the existence of bird droppings. Some eyebar heads, such as U 35 and U 36, have also been subjected to excessive moisture due to the deteriorated condition of the deck above. The pin caps, bolts and nuts, however, were in excellent condition.

2.2 Live Load Stresses in Eyebars

Live load stresses correspond to vehicular loads. Since the bridge was closed to vehicles weighing 89 kN (20 kips) or heavier, the live load stresses were expected to be small. This was confirmed in 1974 and reconfirmed during the 1977 field study. All measured stresses by passenger cars and buses were less than 3.45 MPa (0.5 ksi) in the shanks of the eyebars.

To examine the possible live load stresses in the eyebars, a test truck and the snooper from the Pennsylvania Department of Transportation, weighing approximately 351 kN (79.0 kips) and 200 kN (45.0 kips) respectively, were driven back and forth over the bridge.
The truck and the snooper traveled alone, side by side, or in tandem. The recorded maximum stress ranges (live load stresses) at various eyebar shanks are summarized in Table 1. The highest maximum stress range was 10.0 MPa (1.45 ksi) in eyebar U 46 - U 47B and occurred when the trucks were traveling abreast near the eyebar.

The position of trucks influence the live load stress magnitude in structural elements. Traces of time variation of stresses in eyebar U 34 - U 35A are presented in Fig. 6 for the situation of the test truck traveling in different lanes. Lane 1 is the north-bound curb lane adjacent to the eyebar in the upstream truss. These traces are analogous to influence lines for a load of 351 kN (79.0 kips) over a length of approximately 30 meters (98 ft.). Because the bridge has only two trusses, trucks traveling south, in lane 4, adjacent to the downstream truss, also generate stresses in the eyebars of the north truss, as is evident from Fig. 6. For the evaluation of fatigue strength of the eyebars and other components, traffic in both directions must be considered.

The distribution of loads among a group of eyebars were monitored with strain gages. Figure 7 compares the live load stresses in two eyebar groups for the same truck run. Stresses were not equal in each eyebar, implying an unequal load distribution among the eyebars. Furthermore, the stresses were slightly different between the top and bottom of the eyebars. This small but noticeable difference occurred on almost all eyebars. It appears that the eyebars were subjected to some bending such that the top of the eyebars sustained slightly higher tension.
2.3 Dead Load Stresses In Eyebars U 35 - U 36

The two original eyebars between panel points U 35 and U 36 were removed for laboratory studies and were replaced by two new eyebars of the same dimensions fabricated from A588 steel plate. The dimensions are shown in Fig. 8. Strain gages were mounted on the original eyebars as shown in Fig. 9 to monitor the change of strains during removal. During the process, hydraulic jacks transferred the dead load forces from eyebars U 35 - U 36A and D to the reinforcing bars U 35 - U 36B and C. For the purpose of strain measurement, forces were transferred back to the original bars, and then completely relieved thereafter so that the eyebars could be removed from the pins. The total change of loads between two original and two reinforcing eyebars was 4270 kN (960 kips), calculated from strain measurements on the jacking plates attached to the reinforcing eyebars. The design dead load force in the original eyebars was 3110 kN (700 kips). An estimated 20 percent increase of deck weight was added in the years, making the dead load force 3740 kN (840 kips). Higher jacking force was anticipated to overcome frictional forces at the truss panel points.

Difficulties were encountered in sliding the eyebars off the pins when there was apparently no load in eyebars U 35 - U 36A and D. Upon inspection, it was found that the eyebar head faces had adhered to each other at panel points because of corrosion. The adhesive force was very strong at U 35A. Repeated lifting of U 35 - U 36A at the freed U 36A, by a hoist, could not break the adhesive bond at the other end of the eyebar. It was slid off the pin only after wedges
were driven between the eyebar head faces and torches were used to burn off the corroded material.

The measured stresses in the eyebar heads confirmed the condition of adhesion between eyebar head faces. The measured stress distribution at U 36A, as shown in Figs. 10 and 11 agrees well with that obtained by stress analysis\(^4\). On the other hand, the recorded stress distribution in U 35A indicated a very moderate stress gradient and is shown in Figs. 12 and 13. The magnitude of stress at the pin hole was about the same as that in the shank of the eyebar. This condition implies that the force transmitted at U 35A was not through the pin, rather it was through the bond between the faces of joining eyebars U 34 - U 35A and U 35 - U 36A in adjacent panels.

The measured stresses from the limited number of strain gages at eyebar head U 36D also revealed the same condition of force transmitted through surface bond. The stress distribution in this eyebar head is given in Figs. 14 and 15 for the same jacking force as for Figs. 10 to 13. The values presented are the stresses nondimensionalized by the average stress in the eyebar shank.

The distribution of stresses in the shanks of eyebars U 35 - U 36 are depicted in Fig. 16. During removal (unloading) of forces from eyebars U 35 - U 36A and D, stresses decreased in A and D while they increased in reinforcing bars U 35 - U 36B and C. These stresses provided an on-the-spot monitoring of the eyebar removal operation. The most important stresses were in the heads of the eyebars.
It is interesting to note that the average measured dead load stresses in eyebars U 35 - U 36A and D was 127 MPa (18.4 ksi), which is almost the design dead load stress of 129 MPa (18.7 ksi).

2.4 Material Properties

Standard (ASTM) specimens were fabricated from the shanks of the two eyebars removed from the bridge. The specimens were cut along the longitudinal direction of the eyebars. The results of testing are presented in Table 2. The mean yield stress of six tensile specimens is 365.8 MPa (53.0 ksi) for the eyebars of AISI 1035 steel.

The results of chemical analyses are listed in Table 3. Materials were taken from the eyebar heads. Carbon contents are found to be higher than 0.35 percent; it is in the order of 0.43 - 0.46 percent.

Specimens for fracture toughness tests were also cut from eyebar heads. Slow bend and dynamic tests as well as Charpy V-notch (CVN) tests were conducted. Figures 17 and 18 summarize the results of $K_{IC}$ and $K_{ID}$ values against the test temperatures for slow bend and dynamic tests, respectively. The CVN data are plotted in Fig. 19. These CVN data are converted to dynamic fracture toughness ($K_{ID}$) using the relations

$$\frac{K_{ID}^2}{E} = 5 \text{(CVN)}$$  \hspace{1cm} (2.1)

$$\left(\frac{K_{ID}}{\sigma_{YS}}\right)^2 = \frac{5}{\sigma_{YS}} \left[ (\text{CVN}) - \frac{\sigma_{YS}}{20} \right]$$ \hspace{1cm} (2.2)
where $E$ is the modulus of elasticity and $\sigma_{ys}$ is the yield stress from static test. The resulting values are presented in Figs. 20 and 21. From these dynamic fracture toughness values the static fracture toughness values are estimated by a temperature shift\textsuperscript{18},

$$T_s = 215 - 1.5 \sigma_{ys}$$

(2.3)

and are also presented in Figs. 20 and 21. The static values from these figures are about 55 MPa $\sqrt{m}$ (50 ksi $\sqrt{in}$) at $-34.4^\circ C$ ($-30^\circ F$). The fracture toughness from slow bend tests appear to be slightly higher.
3. STRESS DISTRIBUTION IN EYEBAR HEADS

3.1 Design Parameters and Assumptions

Because maximum stresses are higher in the heads than in the shank of eyebars, and the distribution of these stresses are not uniform, it is necessary to evaluate the maximum stresses in the heads of eyebars. In the design of eyebars in the past, however, the stress distribution analysis was usually omitted when the eyebars were proportioned according to design specifications.

Table 4 lists the design criteria for eyebars set forth by the American Institute of Steel Construction\(^5\) (AISC), American Association of State Highway and Transportation Officials\(^6\) (AASHTO) and the American Railway Engineering Association\(^7\) (AREA) specifications. These specifications have been established based on experimental and analytical data. In all three specifications the proportioning of the head of an eyebar is determined from the required net section of the shank. The net section of the shank is determined from the allowable stress in a tension member. The resulting design is such that the average stress is higher in the shank than in the head of an eyebar.

For the evaluation of fatigue strength and fracture resistance, the maximum stress in the head must be considered. The maximum stress could be at the circumference of the pin hole on a transverse diameter, or at the edge of the eyebar at the transition...
from the shank to the head. The magnitude of this stress depends on the relative dimensions such as the width ratio and the diameter of the head, as listed in Table 4. The symbols are shown in Fig. 22.

There have been many different analytical methods of determining the stress distribution in tension members with eye-shaped heads. In this study the finite element method was chosen for its versatility and reliability of results in determining stress distributions in solid continuum.

One of the most crucial assumptions in modeling eyebars is the distribution of bearing pressure between the pin and pin hole. Blumenfeld distributed the load uniformly over the interface at the top half of the ring while Beke assumed the bearing pressure to be proportional to the cosine of the angle measured from the longitudinal axis. Reissner and Strauch also used a cosine distribution but included a shear stress as an external reaction caused by friction. Timoshenko and Goodier used a cosine function but made refinements in the stress function to satisfy the compatibility relations. Poletto achieved very good correlation between a finite element analysis and test data by assuming a non-uniform cosine bearing pressure varying from the vertical to horizontal sections on the top half of the pin hole. Fisher and Daniels modeled the bearing of a pin-plate on a pin by connecting radial and tangential supports to nodes at the pin surface in a finite element analysis. A more complete coverage and bibliography can be found in Ref. 4.
The method of modeling the pin with elastic supports in the radial and tangential directions was adapted for this study. The radial and tangential stiffness of the elastic supports were taken as:

\[ K_r = A \frac{E}{d} \]
\[ K_t = 0.3 K_r \]

where:
- \( K_r \) = radial stiffness
- \( K_t \) = tangential stiffness
- \( A \) = bearing area between pin and pin hole
- \( d \) = pin diameter
- \( E \) = modulus of elasticity.

The tangential supports simulate the effects of friction between the pin and pin hole interface. Results from trial analysis showed that the elastic supports should be spread over a 90° angle, 45° to each side of the longitudinal axis, on the top side of the pin hole.

3.2 Finite Element Model

The finite element program used in this study was SAP IV, a structural analysis program for static and dynamic response of linear elastic systems.

By taking advantage of the symmetry of the eyebar about its major axis, only one-half of an eyebar head was discretized with appropriate boundary conditions along the centerline. Plane stress finite elements were used.
Because the influences of eyebar geometry on the stress distribution in eyebar heads were to be examined, large amounts of input data were required for the computer program even when plane stress elements were adapted. In view of this, stress distributions in eyebar heads were examined for possible simplification in input data. It was found that for eyebar geometry similar to that of Liberty Bridge eyebars, the maximum stress in the heads was at the pin holes, not at the transition from the shank to the head. Consequently, the curved transition from eyebar head to eyebar shank was approximated by a straight line. Figure 23 shows the discretization of the model with the curved transition and Fig. 24 shows that with the straight line approximation. This modification enabled the formulation of a computer program which would provide stress distribution output for different geometry with only slight changes in input data.

For two eyebar heads of the same loading conditions and geometry, except the transition curve, the results from the finite element analysis are given in Fig. 25. In the figure the stress distributions along a transverse diameter at the pin hole are compared. The ordinates are the stresses non-dimensionalized by the shank stress. The abscissa is the distance from the edge of the pin hole. This plot demonstrates that the effect of the straight line approximation is very small and its use has been incorporated into this investigation.
The finite element model of Fig. 24 gives the location of the maximum stress and stress distribution in a eyebar head. From the experience of the failure of the Point Pleasant Bridge\textsuperscript{3} and from results of other investigations\textsuperscript{14,15}, it can be concluded that, if a crack would develop, it would originate at the location of the maximum stress. The crack would then propagate along a path perpendicular to the maximum principle tensile stress in the eyebar head. This path coincides with the transverse diameter of the head.

For a fracture analysis of eyebar heads with a high stress gradient along the most probable crack path, an estimate of stresses more accurate than those given by the model in Fig. 24 is necessary. The cross hatched area of the discretization shown in the figure was used as the substructure in a fine mesh analysis. The discretization and boundary conditions for this fine mesh substructure is sketched in Fig. 26. The size of the smallest elements was 2.29 mm (0.09 in.). Plane stress elements were again used so as to conform with the overall gross mesh structure model. From the gross mesh analysis the stresses were taken along the perimeter of the substructure and converted to equivalent forces. These forces were then applied to the respective nodes at the boundary of the fine mesh substructure.

The computed stress distributions from the gross mesh and fine mesh analyses are presented in Fig. 27 for an eyebar of the Liberty Bridge. The fine mesh model gives higher maximum stress at the edge of the pin hole. Obviously, further decrease in mesh size
would result in higher stress at the point and a steeper stress gradient along the transverse diameter (the abscissa) until the "true" magnitude is reached. Results from fracture resistance analysis (Chapter 4) indicated that the chosen mesh size was adequate and thus considered sufficiently accurate.

3.3 Comparison with Test Results

To examine the validity of the finite element model used in this study, a comparison was made between the computed stresses and measured test data of Poletto on a full size eyebar from the collapsed Point Pleasant Bridge. The eyebar tested was gaged extensively on the head to determine the stress distribution. Figure 28 shows in non-dimensionalized ordinates the distribution of stresses across the width, a, of the eyebar head on the transverse diameter. The measured results and the finite element solution values agree very well except near the outside edge of the head, where the theoretical stresses are in compression. At the pin hole, the maximum computed stress is higher than that from measurement at the specific load of Fig. 28. However, at other load magnitudes during testing, the non-dimensionalized stress (or the stress concentration factor) at the pin hole varied from 2.27 to 3.15. This range is also indicated in the figure on the ordinate. This condition points out the difficulty of actual stress measurement at the pin hole, even under controlled conditions in a laboratory.
For the Liberty Bridge stress distribution in the heads of eyebars U 35 - U 36 were computed. The stresses along the transverse diameter through the pin hole and along the eyebar axis in the eyebar head are plotted in Fig. 29. Nominal dimensions of the eyebars were used with the finite element discretization model of Fig. 24. The computed stress distribution as shown in Fig. 29 confirms those obtained from measurements at eyebar head U 36A after the breaking of bonds (Figs. 10 and 11). A direct superposition is given in Fig. 30. The distributions corresponding to two load levels are provided. These loads were calculated from strains on the jacking plates after the bond condition was released. The excellent agreement between computed and measured stresses is evident in Fig. 30.

It must be pointed out that higher stresses at pin holes resulted from computation when the fine mesh substructure (Fig. 26) was used. The comparison of stresses along the transverse diameter of the pin hole of U 35 - U 36 is given in Fig. 27 for the overall model and the fine mesh sub-structure. An enlarged plot is given in Fig. 31. The stress concentration factor from the sub-structuring model is 3.47 at the edge of the pin hole. It was, however, impossible to measure stress at this point due to the physical width of the electrical resistance strain gage. Judged by the excellent agreement between computed and measured stress distribution over the entire eyebar head, it is considered that the finite element model is adequate for analyzing stress distributions in eyebar heads.
3.4 Stress Concentration Factor at Eyebar Pin Holes

Because the most likely crack path is along the transverse diameter of a pin hole, the maximum stress at the edge of the pin hole on this diameter is most important. The magnitude of this stress is a function of the average stress in the shank of the eyebar and the geometry of the eyebar head. By using the finite element model, stresses for different geometries can be calculated.

Figure 32 depicts the stress distribution from the pin hole to the outside edge for two eyebar heads. The pin hole diameter \(d\) is arbitrarily taken as \(7/8\) times the width of the shank \(b\), and the width \(a\) of the rim of the eyebar head is \(0.665b\) and \(0.75b\) respectively. These are the specified limits as summarized in Table 4. Other dimensions being the same, the head with a wider width \(a\) or a higher value of width ratio \(a/b\) has lower stresses. The pattern of stress distribution is identical and is also the same as those shown in Figs. 10 and 29 for the Liberty Bridge.

Because the width ratio \(a/b\) affects the stress magnitude, its influence on the stress concentration factor (SCF) at the pin hole is examined. Figure 33 shows the variation of SCF with \(a/b\) for two eyebars of different pin hole sizes \(d\), but the same width \(b\). Figure 34 shows the change of SCF with \(a/b\) for two different eyebar widths \(b\) but the same pin hole size \(d\). For all cases the width ratio \(a/b\) is the dominant controlling parameter. The SCF decreases with higher values of \(a/b\).
The stress concentration factors in Figs. 33 and 34 were computed using a gross mesh finite element model. More accurate values can be obtained from a fine mesh analysis or substructuring technique. Coupled with the practical limits of geometry (Table 4) some guidelines could be established for eyebar design.
4. FRACTURE RESISTANCE AND FATIGUE STRENGTH

4.1 Fracture Resistance

Under an adverse combination of unfavorable conditions, sudden fracture of an eyebar or structural member may occur. The controlling factors include the stress magnitude, material properties, and flaw size, among others. In cases of structural member failure which were studied, often small flaws were found to grow, as fatigue cracks, to a critical size and triggered fracture. The concepts of linear elastic fracture mechanics have been used successfully in the evaluation of these failures.

The fracture resistance of an eyebar is associated with the stress intensity factor, $K^{17,18}$. This factor can be expressed as

$$K = F_s \times F_w \times F_e \times F_g \times \sigma \times \sqrt{\pi a} \quad (4.1)$$

where

- $F_s$ = front free surface correction
- $F_w$ = finite width correction
- $F_e$ = crack shape correction
- $F_g$ = stress gradient correction
- $\sigma$ = nominal stress in the shank
- $a$ = flaw size
When the stress intensity factor with a flaw or crack in a structural detail is higher than the fracture toughness property of the material fracture will occur.

Equation 4.1 is an approximation of more exact expressions. It renders a possible simplified solution with reasonable accuracy through approximation of the individual correction factors.

4.1.1 Approximations In Correction Factors

The front free surface correction factor, $F_s$, accounts for the effects due to a free surface at the crack origin. The most likely position of crack initiation, in an eyebar head, is at the edge of the pin hole. Figure 35 shows the front free surface correction factors for an edge crack in a semi-infinite plate under uniform tension and under tension which varies linearly from the crack origin to the crack tip\textsuperscript{19}. As the stress distribution for the eyebar lies between these two cases, a value of 1.15 was used for $F_s$ as suggested by Tada and Irwin\textsuperscript{20}.

The finite width or back free surface correction, $F_w$, amplifies the stress intensity factor as the crack approaches a back free surface. Zettlemoyer\textsuperscript{14} suggested that if the displacements normal to the back free surface are zero the finite width correction factor can be computed by:

$$F_w = \sqrt{\frac{2w}{\pi a}} \tan \frac{\pi a}{2w}$$ (4.2)
If, on the other hand, the stresses are zero normal to the back free surface then:

\[ F_w = \sqrt{\sec \frac{\pi a}{2w}} \]  \hspace{1cm} (4.3)

In both equations 4.2 and 4.3 \( a \) is the crack length and \( w \) is the width of the structural member or detail. Equation 4.2 is adopted in this investigation.

There has been little study to date on the crack shape variation in eyebar heads. An upper bound and a lower bound are assumed here for the crack shape correction factor, \( F_e \). The lower bound corresponds to a circular corner crack as shown in Fig. 36a. The upper bound is derived from a through-the-thickness crack as shown in Fig. 36b. The corner crack is more realistic since corrosion cracks are more likely to initiate at the edge of a pin hole on the eyebar head surface where a corrosive environment would attack first. In the Point Pleasant Bridge investigation\(^3\) elliptical surface corrosion flaws at the pin hole were found on the fractured surface of the eyebar. This condition was between the lower and upper bound assumed here.

The stress gradient correction factor, \( F_g \), accounts for the effects of non-uniform stress fields acting on the assumed crack path. Albrecht\(^{21}\) developed a formula for the stress gradient correction factor for cases where the stress concentration decay is known for discrete points from analysis.
where $K_{tj}$ is the average stress concentration over the interval from $y_j$ to $y_{j+1}$, $a$ is the crack length and $y$ is the distance from the crack origin to a point on the crack surface.

Figure 37 shows a plot of stress concentration factor, $K$, and the associate stress gradient correction factor, $F_g$, as a function of crack size. The stress gradient correction factor, $F_g$, decreases at a slower rate than does the stress concentration factor, $K$, as the crack grows in size.

4.1.2 Stress Intensity Factor and Critical Crack Size

By using the assumptions for the correction factors $F_s$, $F_w$, $F_e$ and $F_g$, the stress intensity factor of a crack can be estimated for any nominal stress and crack length.

For eyebar U 35 - U 36 the measured dead load stress was 127 MPa (18.4 ksi) and the maximum measured live load stress was less than 7 MPa (1.0 ksi). The maximum total nominal stress was therefore 134 MPa (19.4 ksi). Figure 38 shows a plot of the stress intensity factor versus the size of a through crack (upper bound) and a corner crack (lower bound) in eyebar U 35 - U 36 if such cracks ever occur.

The critical crack size that could cause sudden brittle failure of the eyebar is that when the stress intensity factor, $K$, is equal to the fracture toughness, $K_{ic}$, of the eyebar material. The
results of fracture toughness tests to date were presented in Chapter 2. At a temperature of \(-34.4^\circ\) C \((-30^\circ\) F) the average value for the fracture toughness of the Liberty Bridge eyebars is estimated to be 55 MPa \(\sqrt{\text{m}}\) (50 ksi \(\sqrt{\text{in}}\)). The corresponding critical crack size for brittle failure is calculated to be 3.6 mm (0.14 in.) for the through crack and 11.2 mm (0.44 in.) for a corner crack under a tensile stress of 134 MPa (19.4 ksi) in the eyebars.

4.2 Fatigue Strength

The brittle fracture critical crack size in eyebar heads could be arrived at through fatigue crack growth, stress corrosion or corrosion fatigue. While work is in progress to study the sensitivity of the eyebar material to stress corrosion and corrosion fatigue, preliminary evaluations based on results from related studies indicated that these would not be the governing factors. The behavior of fatigue crack growth in eyebar heads when subjected to traffic loading is therefore of primary concern.

The fracture mechanics approach to fatigue crack growth relates the crack growth rate, \(\frac{\text{da}}{\text{dN}}\), to the stress intensity factor \(K\). The governing equation is of the form:

\[
\frac{\text{da}}{\text{dN}} = C (\Delta K)^n
\]

where \(C\) and \(n\) are empirical constants for a given material and \(\Delta K\) is the range of stress intensity factor. This model has been shown to describe fatigue crack growth in structural members in the range of \(10^{-7} < \frac{\text{da}}{\text{dN}} < 10^{-3} \) mm/cycle. In practical applications,
Eq. 4.5 is rearranged to give the number of cycles for an initial flaw of size \(a_i\) to reach a critical or final flaw size, \(a_f\).

\[
N = \frac{1}{C} \int_{a_i}^{a_f} \frac{da}{(\Delta K)^n} \tag{4.6}
\]

or for numerical integration\textsuperscript{14,21,29}:

\[
N = \frac{1}{C} \sum_{j=1}^{m} \frac{1}{(\Delta K)^n} \Delta a_j \tag{4.7}
\]

The range of the stress intensity factor, \(\Delta K\), is given by:

\[
\Delta K = F_s \times F_w \times F_e \times F_g \times S_r \times \sqrt{\pi a} \tag{4.8}
\]

where \(F_s\), \(F_w\), \(F_e\) and \(F_g\) are the individual correction factors as described before, \(S_r\) is the nominal stress range corresponding to the live load stress variation, and \(a\) is the crack length. The constants \(C\) and \(n\) can be taken as \(C = 2.0 \times 10^{-10}\) and \(n = 3\) with \(da/dN\) in inches per cycle\textsuperscript{25}.

Equations 4.6, 4.7 and 4.8 apply only to constant amplitude cyclic loads in the range of crack growth rates of \(10^{-7}\) to \(10^{-3}\) mm/cycle (4 x \(10^{-9}\) to 4 x \(10^{-5}\) in/cycle). In the range of very low crack growth rates, it is generally recognized that there exists a threshold stress intensity factor below which cracks would not grow. While there are various suggested threshold values for ferrite-pearlite structural steels\textsuperscript{15,18,27} a value of 3.3 MPa \(\sqrt{m}\) (3.0 ksi \(\sqrt{\text{in.})\) is chosen for the Liberty Bridge material.
For the eyebars on the Liberty Bridge the highest live load stress is below 10 MPa (1.5 ksi) which was measured at the most highly stressed eyebars, U 46 - U 47, under a very high live load of 552 kN (124 kips). For an assumed through-the-thickness flaw of 1.14 mm (0.045 in.) and a 10 MPa (1.5 ksi) stress range, the computed stress intensity factor range is 2.47 MPa $\sqrt{m}$ (2.25 ksi $\sqrt{in}$). This is below the threshold value, therefore, no crack growth would be anticipated.

If stress corrosion would develop flaws in the eyebar heads, a through-the-thickness flaw corresponding to the threshold of fatigue crack growth for a live load stress range of 10 MPa (1.5 ksi) would be 3.18 mm (0.125 in.) in size. This would take many years for serious corrosion to develop, as judged by the conditions of eyebar heads U 35 - U 36A and D from the bridge. Furthermore, corrosion does not result in a sharp through-the-thickness flaw. More possibly would be surface elliptical flaws, close to the condition of circular flaws, which would require even more years to reach the size of fatigue crack growth threshold. Thereafter, hundreds of millions of cycles of maximum live load stress would be needed to grow the crack to the critical crack size for brittle failure. All these conditions of corrosion and repeated maximum live loads are, although possible, not probable.

More realistically, because the most conservatively estimated stress intensity factor range is below the fatigue crack growth threshold value, no cracks would be anticipated to grow in the eyebar heads of the Liberty Bridge.
5. DISCUSSION

5.1 Stress Evaluation

In order to evaluate the fracture resistance and fatigue strength of the bridge, dead load and live load stresses in the most critical members must be accurately calculated. Accuracy is, however, difficult to achieve because of the necessary approximations in the stress analysis. The assumption of point loads (dead load and live load), frictionless joints, and planar trusses all contribute to the uncertainty. Furthermore, the computation of local stresses from nominal member forces relies on the adequacy of proper modelling.

While the local stress concentrations in eyebar heads were correlated for computed and measured values, the forces in the eyebars due to live load and dead load have not yet been computed very satisfactorily. It appears that the consideration of the continuous deck and the lateral bracing system in a three dimensional structural analysis is necessary.

During the removal of eyebars U 35 - U 36A and D, strain measurements were taken at the adjacent floor beams and stringers. Results showed little stress transfer between eyebars, deck and stringers, but the floor beam was subjected to lateral bending. Although this condition does not exist when the bridge is under vehicular load, an analysis of the load transfer in eyebar removal
would provide some information for an overall stress analysis of the bridge.

5.2 Bonded Eyebar Heads

During the removal of eyebars U35 - U36A and D it was found that forces in eyebar heads on lapping eyebars were bonded together because of corrosion. Indication of this bonding condition include the appearance of the contacting surfaces, the relatively loud noise when the lapping heads separate under load, the difficulties in separating some of the heads, and the measured stress distribution pattern in the heads.

The bonding of eyebar head faces rendered the adjoining eyebars, such as U34 - U35 and U35 - U36, continuous members similar to lap joints. The tension force in one eyebar could be transferred through shear to the other. The result was a decrease in stress concentration at the pin hole. The stress magnitudes in the eyebar heads were about the same as in the eyebar shanks. This condition was observed in all the eyebar heads where strains were measured.

Reduction of the stress concentration in eyebar head pin holes due to bond decreased the stress magnitude at the pin hole edge. First the maximum stress corresponding to dead load plus live load and impact would be smaller, resulting in a larger tolerable flaw size of brittle failure. Second, the live load stress range was lower. The corresponding stress intensity factor range, $\Delta K$, was found to be much below the threshold value of $3.3 \text{ MPa} \sqrt{\text{m}}$ $(3.0 \text{ ksi} \sqrt{\text{in.}})$ for an assumed initial
through-the-thickness flaw of 1.14 mm (0.045 in.) and a 10 MPa (1.5 ksi) stress range in the shank of the eyebar. Such flaws would not be expected to propagate at all. With an estimated critical flaw size much larger than the possible size of non-propagating initial flaws, it is not likely that any danger of brittle fracture will result.

5.3 Anticipated Conditions

With the assumption that the dead weight of the deck system will not be increased, the members of the existing trusses will have sufficient capacity to carry the intended loads according to results of this analysis. The live load stresses were lower than computed values and are expected to remain so, since no change in traffic pattern is anticipated after rehabilitation of the bridge. Based on these loads, and the results of the fracture resistance, it can be stated that fracture will not occur.

Since all members which are made up of eyebars have four or more bars, there are no non-redundant eyebar members. Adding to this condition that there are no fracture critical eyebar heads, the fracture resistance and fatigue strength of the bridge are considered adequate for the projected life of the rehabilitated structure.
6. CONCLUSIONS AND RECOMMENDATIONS

Based on the results of eyebar head stress distribution analysis, by the finite element method, the following conclusions can be drawn:

1. Within the limits of design specifications (AISC, AASHTO, AREA) eyebars with moderate transition from the head to shank have the highest stress at the pin hole edge on a transverse diameter at the pin hole.

2. The computed stress distribution in the head of a test eyebar correlated very well with measured values, confirming the accuracy of the analysis (Fig. 30).

3. The dominate factor governing the stress concentration at the pin hole is the ratio of $a/b$, $a$ being the width of the head rim and $b$ the width of the eyebar shank. (Figs. 33 and 34). Other factors such as the ratio of pin hole diameter to eyebar width $(d/b)$ and the ratio of width to thickness $(b/t)$, only affect the stress concentration factor slightly.

4. Within the specified width ratios $a/b = 0.665$ to $0.75$, the highest stress concentration factor is about 3.5, calculated against the nominal stress in the shank and from a fine mesh finite element analysis. This value could be used as a nominal value of SCF for the design of eyebars against fatigue and fracture.

-33-
From the field studies on the Liberty Bridge, the following can be summarized:

5. The eyebar head pin holes appeared to be in good condition. No cracks or severe notches were found in the eyebar heads which were inspected. However, there were some corroded spots in the pins between eyebar heads.

6. Live load stresses were very low in all eyebars on which strain gages were mounted. The highest magnitude under a live load of 552 kN (124 kips) was less than 10 MPa (1.5 ksi), Table 1.

7. The live load strain rate for the eyebars was in the order of 5 to 10 seconds, from zero to maximum strain, Fig. 6, corresponding to a static condition.

8. Live load stress distributions within eyebar groups were not exactly uniform among the bars, Fig. 7.

9. Stress distribution in eyebar heads agreed with the computed pattern in one case, Fig. 30. In all other cases the actual stress concentration was much lower than predicted, Figs. 12 through 15.

10. Eyebar head faces were found to adhere to each other due to corrosion. This condition made the removal of eyebars difficult. It also permitted transfer of forces directly from one eyebar to the adjacent eyebar in the manner of a lap-joint. The consequence was the reduced stress concentration at pin holes.
From the fracture resistance and fatigue strength evaluation a few conclusions are made:

11. A through-the-thickness crack at the pin hole is more serious than a corner crack at the edge of the pin hole, Fig. 36. Due to the corrosion effect, flaws would more likely develop at the corners first.

12. The average fracture toughness, $K_{ic}$, of the eyebars (AISI 1035 heat-treated steel) is $55 \text{ MPa} \sqrt{\text{m}}$ (50 ksi $\sqrt{\text{in.}}$) at $-34.4^\circ \text{C}$ ($-30^\circ \text{F}$) converted from CVN test results. Results from slow bend tests are slightly higher. More tests are to be conducted.

13. Based on this fracture toughness value, the critical through-crack which would cause brittle fracture of the eyebars at $-34.4^\circ \text{C}$ ($-30^\circ \text{F}$) was found to be 3.6 mm (0.14 in.) under a shank stress of 134 MPa (19.4 ksi). The corresponding corner crack would be 11.2 mm (0.44 in.).

14. The stress intensity factor ranges are below the threshold value for assumed initial flaw sizes and anticipated live load stress range. For a 1.14 mm (0.045 in.) initial through-the-thickness flaw no crack growth would occur under a live load stress range of 10 MPa (1.5 ksi) in the eyebar shanks. No crack growth would be anticipated for through-the-thickness flaws of 3.18 mm (0.125 in.).

While analysis and evaluation are still in progress, it can be concluded, based on results to date, that the Liberty Bridge should be able to carry the anticipated loads. Rehabilitation of the bridge, as planned, is recommended.
ACKNOWLEDGMENTS

The work of this interim report is part of a study on the Fatigue and Fracture Resistance of Eyebars on the Liberty Bridge, sponsored by Salvucci Associates, Inc. and the Pennsylvania Department of Transportation (PennDOT) in conjunction with the Federal Highway Administration (FHWA).

The study was conducted at Fritz Engineering Laboratory and Department of Civil Engineering, Lehigh University, Bethlehem, Pa. The director of the laboratory is Dr. Lynn S. Beedle and the chairman of the department is Dr. David A. VanHorn.

The help of Messrs. Thomas Kylowski and Harry Laatz of Federal Highway Administration and Mr. Hugh T. Sutherland of Fritz Laboratory in acquiring the test data, is acknowledged. The use of the FHWA instrumentation equipment is highly appreciated.

Thanks are due Messrs. Roy Guenther, Clifford J. Shorts, Jr. and Larry Young of Salvucci Associates, Inc. for their participation in the field work. The constant help of PennDOT District 11-0 personnel, particularly Messrs. Nalin H. Udani and Carl Angeloff, is also acknowledged.

Appreciation is expressed to the staff of Fritz Engineering Laboratory for their support, to Mr. Gopal Krishna for his help in fracture toughness testing, to Mr. John M. Gera for tracing the figures, and, last but not least, to Mrs. Dorothy Fielding for her aid to the project and in typing this interim report.
# TABLE 1

**MAXIMUM MEASURED STRESS RANGE IN EYEBAR SHANKS**

<table>
<thead>
<tr>
<th>Gage</th>
<th>Location</th>
<th>Maximum Live Load Stress (ksi)</th>
<th>(MPa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>35</td>
<td>U 34 - 35A, Top</td>
<td>1.05</td>
<td>7.24</td>
</tr>
<tr>
<td>36</td>
<td>U 34 - 35A, Bottom</td>
<td>0.66</td>
<td>4.55</td>
</tr>
<tr>
<td>39</td>
<td>U 34 - 35B, Top</td>
<td>0.94</td>
<td>6.48</td>
</tr>
<tr>
<td>40</td>
<td>U 34 - 35B, Bottom</td>
<td>0.64</td>
<td>4.41</td>
</tr>
<tr>
<td>43</td>
<td>U 34 - 35C, Top</td>
<td>1.07</td>
<td>7.38</td>
</tr>
<tr>
<td>44</td>
<td>U 34 - 35C, Bottom</td>
<td>0.08</td>
<td>4.69</td>
</tr>
<tr>
<td>23</td>
<td>U 35 - 36A, Top</td>
<td>0.74</td>
<td>5.10</td>
</tr>
<tr>
<td>25</td>
<td>U 35 - 36B, Top</td>
<td>0.81</td>
<td>5.58</td>
</tr>
<tr>
<td>27</td>
<td>U 35 - 36C, Top</td>
<td>0.79</td>
<td>5.45</td>
</tr>
<tr>
<td>29</td>
<td>U 35 - 36D, Top</td>
<td>0.70</td>
<td>4.83</td>
</tr>
<tr>
<td>1</td>
<td>U 46 - 47A, Top</td>
<td>1.20</td>
<td>8.27</td>
</tr>
<tr>
<td>2</td>
<td>U 46 - 47A, Bottom</td>
<td>1.05</td>
<td>7.24</td>
</tr>
<tr>
<td>3</td>
<td>U 46 - 47B, Top</td>
<td>1.45</td>
<td>10.00</td>
</tr>
<tr>
<td>4</td>
<td>U 46 - 47B, Bottom</td>
<td>1.18</td>
<td>8.14</td>
</tr>
<tr>
<td>5</td>
<td>U 46 - 47C, Top</td>
<td>1.22</td>
<td>8.41</td>
</tr>
<tr>
<td>6</td>
<td>U 46 - 47C, Bottom</td>
<td>1.16</td>
<td>8.00</td>
</tr>
<tr>
<td>23</td>
<td>U 47 - 48A, Top</td>
<td>1.07</td>
<td>7.38</td>
</tr>
<tr>
<td>24</td>
<td>U 47 - 48A, Bottom</td>
<td>0.57</td>
<td>3.93</td>
</tr>
<tr>
<td>25</td>
<td>U 47 - 48B, Top</td>
<td>0.92</td>
<td>6.34</td>
</tr>
<tr>
<td>26</td>
<td>U 47 - 48B, Bottom</td>
<td>0.58</td>
<td>4.00</td>
</tr>
<tr>
<td>29</td>
<td>U 47 - 48D, Top</td>
<td>0.95</td>
<td>6.55</td>
</tr>
<tr>
<td>30</td>
<td>U 47 - 48D, Bottom</td>
<td>0.59</td>
<td>4.07</td>
</tr>
<tr>
<td>7A</td>
<td>U 48 - 49A, Top</td>
<td>1.32</td>
<td>9.10</td>
</tr>
<tr>
<td>8A</td>
<td>U 48 - 49C, Top</td>
<td>1.09</td>
<td>7.52</td>
</tr>
<tr>
<td>22A</td>
<td>U 48 - 49C, Top</td>
<td>1.42</td>
<td>9.79</td>
</tr>
</tbody>
</table>
### TABLE 2

**TENSILE PROPERTIES OF EYEBAR MATERIAL**

**AISI - 1035 STEEL HEAT TREATED**

<table>
<thead>
<tr>
<th></th>
<th>Downstream Mean</th>
<th>Upstream Mean</th>
<th>Overall Mean</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Yield Stress, ( \sigma_{ys} )</strong> MPa (ksi)</td>
<td>374.4 (54.3)</td>
<td>357.2 (51.8)</td>
<td>365.8 (53.0)</td>
<td></td>
</tr>
<tr>
<td><strong>Tensile Strength, ( \sigma_{ult} )</strong> MPa (ksi)</td>
<td>572.3 (83.0)</td>
<td>517.1 (75.0)</td>
<td>544.7 (78.9)</td>
<td></td>
</tr>
<tr>
<td><strong>Elongation in 203.4 mm (8 in.) %</strong></td>
<td>23.8</td>
<td>24.3</td>
<td>24.1</td>
<td></td>
</tr>
<tr>
<td><strong>Area Reduction %</strong></td>
<td>54.7</td>
<td>55.8</td>
<td>55.3</td>
<td></td>
</tr>
</tbody>
</table>

### TABLE 3

**CHEMICAL ANALYSIS**

<table>
<thead>
<tr>
<th>Elements</th>
<th>Downstream</th>
<th>Upstream</th>
</tr>
</thead>
<tbody>
<tr>
<td>Carbon, C</td>
<td>0.50%*</td>
<td>0.43%</td>
</tr>
<tr>
<td>Silicon, Si</td>
<td>0.08%</td>
<td>0.06%</td>
</tr>
<tr>
<td>Manganese, Mn</td>
<td>0.59%</td>
<td>0.61%</td>
</tr>
<tr>
<td>Phosphorus, P</td>
<td>0.032%</td>
<td>0.034%</td>
</tr>
<tr>
<td>Sulfur, S</td>
<td>0.044%</td>
<td>0.048%</td>
</tr>
<tr>
<td>Nickel, Ni</td>
<td>0.012%</td>
<td>0.012%</td>
</tr>
<tr>
<td>Chromium, Cr</td>
<td>0.016%</td>
<td>0.016%</td>
</tr>
<tr>
<td>Molybdenum, Mo</td>
<td>Nil</td>
<td>Nil</td>
</tr>
</tbody>
</table>

*0.46% when retested.*
### TABLE 4
DESIGN CRITERIA FOR PROPORTIONING EYEBAR HEADS

<table>
<thead>
<tr>
<th></th>
<th>AISC</th>
<th>AASHTO</th>
<th>AREA</th>
</tr>
</thead>
<tbody>
<tr>
<td>t</td>
<td>uniform</td>
<td>uniform</td>
<td>uniform</td>
</tr>
<tr>
<td></td>
<td>≥ 12.7 mm</td>
<td>12.7 to 50.8 mm</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.5 in.)</td>
<td>(0.5 to 2.0 in.)</td>
<td></td>
</tr>
<tr>
<td>a</td>
<td>0.667b to 0.75b</td>
<td>≥ 0.675b</td>
<td>≥ 0.7b</td>
</tr>
<tr>
<td>b</td>
<td>≥ 8t</td>
<td>≥ 8t</td>
<td></td>
</tr>
<tr>
<td>d_{pin}</td>
<td>≥ 0.875b</td>
<td></td>
<td></td>
</tr>
<tr>
<td>d_{pin hole}</td>
<td>≥ 0.794 mm + d_{pin}</td>
<td>(≥ 0.031 in. + d_{pin})</td>
<td></td>
</tr>
<tr>
<td>r_t</td>
<td>≥ 2 r_o</td>
<td>≥ 2 r_o</td>
<td></td>
</tr>
</tbody>
</table>
Fig. 1 Elevation of Liberty Bridge Looking West (Downstream)
Fig. 2 Locations of Eyebars on the Main Spans Over the River
Fig. 3 Typical Cross Section of the Liberty Bridge
Fig. 4  Eyebar Head U 36A with Pin Cap Removed

Fig. 5  Sandblasted Eyebar Head Showing Forging Marks
Fig. 6 Variation in Live Load Stress versus Time for Truck in Different Lanes
Fig. 7 Measured Stress Ranges for Test Truck in Curb Lane, Northbound
Fig. 8 Dimensions of Eyebars at U 35 - U 36

266.7 mm
(10.5")

311.15 mm
(12.25")

254.0 mm
(10.0")
Fig. 9 Typical Arrangement of Strain Gages for Live Load and Dead Load Study
Fig. 10  Non-dimensionalized Measured Stress Distribution - U 36A Dead Load
Fig. 11 Non-dimensionalized Measured Stress Distribution - U 36A Partial Load
Fig. 12 Non-dimensionalized Measured Stress Distribution -
U 35A Dead Load
Fig. 13 Non-dimensionalized Measured Stress Distribution - U 35A Partial Load

840 KN (188.9 kips)

Head U35

U35 - U36A
Fig. 14 Non-dimensionalized Measured Stress Distribution -
U 36D Dead Load

1317 KN  (296.0 kips)
Fig. 15 Non-dimensionalized Measured Stress Distribution -

U36D Partial Load

804KN (180.7 kips)
Unloading Eyebars

105.5 128.2
99.5 116.7

133.0
107.6
96.2 123.1 88.3

140.5 131.1 92.9

Unloading Eyebars

93.7 114.4
84.4 101.8

120.8
103.4
93.3 108.2 74.1

127.8
117.7 83.2

Loading Eyebars

78.6 125.1
70.3 115.2

118.9
101.4
93.3 109.2 81.9

129.1 121.4 88.1

Unloading Eyebars

All Values in MPa

1 ksi = 6.895 MPa

Fig. 16 Dead Load Stresses in Shanks of Eyebars

U 35 - U 36

-54-
Fig. 17 Test Results of $K_{ic}$ for Eyebar Material (AISI 1035 Heat-Treated Steel)
TEMPERATURE, °C

KID (ksi√in)

Upstream
Downstream

KID (MPa√m)

TEMPERATURE, °F

Fig. 18 Variation of $K_{ID}$ With Temperature
Fig. 19 Charpy V-Notch (CVN) Test Results
Fig. 20 Fracture Toughness Converted from CVN Results (U - 35 - U 36A)
Fig. 21 Fracture Toughness Converted from CVN Results (U 35 - U 36D)
Fig. 22 Symbols Used to Describe Eyebars Geometry
Fig. 23 Discretization of Eyebär Head With Curved Transition
Fig. 24 Discretization of Eyeball Head with Straight Line Approximation

251 NODES
212 ELEMENTS

PLANE STRESS ELEMENTS

STRAIGHT LINE TRANSITION
Fig. 25 The Effect of Curved and Straight Line Transition on the Stress Distribution
375 NODES
388 ELEMENTS

Fig. 26  Discretization and Boundary Conditions of Substructure for a Fine Mesh Analysis
Fig. 27 Effect of Finite Element Size on Stress Distribution
DISTANCE FROM PIN HOLE EDGE, PT. A

Fig. 28 Comparison of Finite Element Analysis Results and Measured Values
Fig. 29 Results of Gross Mesh Analysis of Eyebar U 35 - U 36

on the Liberty Bridge
Fig. 30 Comparison of Measured and Theoretical Stress Distributions for U 36A

- 1361 kN (305.9 kips)
- 840 kN (188.9 kips)
Fig. 31  Enlarged Plot of Gross and Fine Mesh Analysis Results
Fig. 32 Stress Distribution for Eyebar Heads with Different Width Ratios, Gross Mesh
Fig. 33  Effect of Pin Hole Size on the SCF, Gross Mesh
Fig. 34 Effect of Shank Width on the SCF, Gross Mesh

-72-
Fig. 35 Front Free Surface Correction Factor, $F_s$
$F_e = 0.6366$

$F_e = 1.0$

Fig. 36 Assumed Crack Shape at Edge of Pin Hole
Fig. 37 Stress Concentration Factor $K_t$ and Stress Gradient Correction Factor, $F_g$ as a Function of Crack Size
Fig. 38 Stress Intensity Factor as a Function of Crack Size
REFERENCES

   THE EYEBAR CABLE SUSPENSION BRIDGE AT FLORIANOPOLIS, BRAZIL,
   Transactions of the American Society of Civil Engineers,
   Vol. 92, 1928.

2. Steinman, D. B. and Watson, S. R.
   BRIDGES AND THEIR BUILDERS, Dover Publications, Inc.,
   New York, 1957.

3. National Transportation Safety Board Highway Accident Report,
   COLLAPSE OF U. S. 35 HIGHWAY BRIDGE, POINT PLEASANT,

4. Poletto, R. J.
   STRESS DISTRIBUTION IN EYEBARS, M.S. Thesis in Civil

5. American Institute of Steel Construction,
   SPECIFICATION FOR THE DESIGN, FABRICATION AND ERECTION
   OF STRUCTURAL STEEL FOR BUILDING, AISC, New York,

6. American Association of State Highway Officials
   STANDARD SPECIFICATIONS FOR HIGHWAY BRIDGES,

7. American Railway Engineering Association

8. Blumenfeld, R.
   BERECHNUNG VON GEKRÜMMTEN STUBEN, Zertsch, Ver
   Duetsch-Ing., Vol. 51, 1907.

9. Beke, J.
   A STUDY OF STRESSES IN EYEBAR HEADS, Engineering News-
   Record, Vol. 87, No. 4, 19

10. Reissner, H. J. and Strauch, F.
    RINGPLATTE UND AUGENSTAB, Ingemier Archiv., Vol. 4,
    No. 5, 193

11. Timoshenko, S. P. and Goodier, J. N.

-77-
REFERENCES (continued)

12. Fisher, J. W. and Daniels, J. H.
   AN INVESTIGATION OF THE ESTIMATED FATIGUE DAMAGE IN MEMBERS OF THE 380-FT.

13. Bathe, K. J., Wilson, E. L. and Peterson, F.
   SAP IV - A STRUCTURAL ANALYSIS PROGRAM FOR STATIC AND DYNAMIC RESPONSE OF LINEAR SYSTEMS,
   Earthquake Engineering Research Center Report No. EERC 73-11, University of California, Berkeley, California, June 1973 (Revised April 1974).

14. Zettlemoyer, N.
   STRESS CONCENTRATION AND FATIGUE OF WELDED DETAILS,


16. Fisher, J. W., Pense, A. W. and Roberts, R.
   EVALUATIONS OF FRACTURE OF LAFAYETTE STREET BRIDGE,

17. Hertzberg, R. W.

18. Rolfe, S. T. and Barsom, J. M.


20. Tada, H. and Irwin, G. R.
   K-VALUE ANALYSIS FOR CRACKS IN BRIDGE STRUCTURES,
   Fritz Engineering Laboratory Report No. 399.1, Lehigh University, Bethlehem, Pennsylvania, June 1975.
REFERENCES (continued)

21. Albrecht, P. and Yamada, K.

22. Roberts, R. and Krishna, G. V.


24. Paris, P. C.


26. Barsom, J. M.
FATIGUE CRACK PROPAGATION IN STEEL OF VARIOUS YIELD STRENGTHS, Applied Research Laboratory, United States Steel Corporation, 1971.

27. Paris, P. C.

28. Crooker, T. W. and Lange, E. A.

29. Batchler, B. P.